Microring-Based Optical Isolator and Circulator with Integrated Electromagnet for Silicon Photonics

Paolo Pintus, *Member, IEEE*, Duanni Huang, Chong Zhang, Yuya Shoji, *Member, IEEE*, Tetsuya Mizumoto, *Fellow, IEEE*, and John E. Bowers, *Fellow, IEEE*

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Abstract—In this study, we present optical isolators and circulators fabricated by bonding cerium-substituted yttrium iron garnet (Ce:YIG) on silicon microring resonators. A novel integrated electromagnet is fabricated by depositing a metal micro-strip on the bonded chip. We experimentally prove that it can be efficiently used to control the magnetic field needed to induce the nonreciprocal phase shift effect in the Ce:YIG. The fabricated devices exhibit extremely small footprint (<70 μ m) and can be packaged, eliminating the need of a large size permanent magnet. A large optical isolation of 32 dB and 11 dB is measured for the isolator and the circulator, respectively. Moreover, a two microring solution is also investigated to provide larger bandwidth and higher isolation. The proposed approach represents a promising solution for large-scale integration of nonreciprocal components in silicon photonics.

Index Terms—Integrated optoelectronics, magnetooptic devices, microresonators, optical circulators, optical isolators.

I. INTRODUCTION

N ONRECIPROCAL components, such as optical isolators and circulators, are fundamental building blocks in optics to block undesirable back-reflections and to separate counterpropagating optical signals. Optical isolators are especially important as silicon photonic integrated circuits (PIC) grow in complexity [1], potentially introducing strong reflections especially at mode conversion tapers and transitions. On the other hand, integrated circulators would enable bidirectional operation in optical interconnects [2]–[4] and optical sensors [5].

P. Pintus is with the Department of Electrical and Computer Engineering, University of California, Santa Barbara, CA 93106 USA and also with the TeCIP Institute, Scuola Superiore Sant'Anna Pisa 56124, Italy (e-mail: p.pintus@ssup.it; ppintus@ece.ucsb.edu).

D. Huang, C. Zhang, and J. E. Bowers are with the Department of Electrical and Computer Engineering, University of California, Santa Barbara, CA 93106 USA (e-mail: duanni@ece.ucsb.edu; czhang@ece.ucsb.edu; bowers@ece.ucsb.edu).

Y. Shoji and T. Mizumoto are with the Department of Electrical and Electronic Engineering/FIRST, Tokyo Institute of Technology, Tokyo 152-8552, Japan (e-mail: shoji.y.ad@m.titech.ac.jp; tmizumot@pe.titech.ac.jp).

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To date, several approaches to achieve nonreciprocity onchip have been proposed, although many challenges remain. Nonreciprocal devices are characterized by a symmetry breaking for the light that propagates from opposite directions, which results in an asymmetric scattering matrix. This is in contrast to optical diodes [6], which are completely comprised of purely reciprocal elements, and have the drawback of breaking down when forward and backwards propagating light are simultaneously passing through the structure [7]. For truly nonreciprocal devices, three different approaches have been proposed: i) nonlinear materials, ii) temporal-based modulation of the refractive index, and iii) magneto-optic (MO) materials [8], [9]. However, only a few nonlinear optical phenomena such as Brillouin scattering can be effectively used to break the symmetry [10], [11]. Some nonlinear effects such as the Kerr effect are currently under scrutiny over whether they truly provide isolation [12], [13]. Pairs of electro-optic modulators operating in tandem can also be used to induce nonreciprocity, although multiple pairs are needed for effective isolation, which greatly increases the complexity of the device [14], [15].

On the other hand, MO material can be effectively bonded on silicon-on-insulator (SOI) wafer, and both isolators and circulators can be realized with relatively simple design. The MO material becomes nonreciprocal when it is magnetized in a quasi-static magnetic field. Optical isolation using MO garnet can be performed using two configurations named Faraday and Voigt, respectively. In the former case, an external magnetic field is applied parallel to the wave propagation direction such that the polarization of light shows different rotation angle while it propagates forward or backward. In the latter one, the magnetic field is perpendicular to the propagating direction of light, which exhibits a different phase velocity according to the propagation direction [16], [17]. Properly designed interferometric devices generate constructive interference for forward light and destructive interference for backward light achieving the isolating function. These devices are often designed in an unbalanced Mach-Zendner interferometer [18]-[21] or microring configuration [22]-[24]. However, the large absorption loss (e.g., 60 dB/cm) in MO material like cerium-substituted yttrium iron garnet (Ce:YIG) and the use of a permanent magnet for applying an external magnetic field are two important aspects that limit the performance and the integration of those devices moving forward. While the propagation loss can be greatly reduced

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Fig. 1. (a) Top view of the isolator. (b) Cross-section of the microring resonator. The cylindrical coordinate system is shown in (b) as a reference frame. Pictures are not to scale.

in a device with small footprint, the external biasing magnet is still a significant limiting factor due to possible magnetic field interference with electronics and its large footprint (size>1mm²).

In this work, exploiting Voigt configuration, we investigate integrated optical isolators and circulators using a planar spiral electromagnet that provides local control of the magnetic field, and can be easily integrated and packaged. This electromagnet should be placed in close proximity with the waveguide. We then experimentally verify our model by comparing it with fabricated isolators and circulators. A two-microring solution is also investigated to provide larger bandwidth and higher isolation.

II. DEVICE DESIGN AND MODELLING

In a magneto-optic garnet, an external magnetic field is always needed to induce the nonreciprocal phase shift effect (NRPS). To avoid bulky magnets, an electric current can be efficiently used as a magnetic field source.

Using the direct wafer bonding approach [24]–[27], optical isolators and circulators can be manufactured for the transverse magnetic (TM) mode. Before bonding the magneto-optic garnet on the SOI wafer, the waveguides and microring resonators are patterned on the silicon layer. Because the field decreases with the distance between the waveguide and the electromagnet, the substrate of the bonded chip (SGGG in Fig. 1) is thinned to few micrometers. Next, a metallic micro-strip, aligned with the device underneath, is fabricated above the chip. A schematic of the device is shown in Fig. 1.

In the following subsections, we present the modelling of the nonreciprocal magneto-optic split and the reciprocal thermal shift, the waveguide/microring cross-section optimization, and the electromagnet design.

A. Magneto-Optic Split and Thermal Shift Modelling

When a static radial magnetic field H_r is applied, the clockwise (CW) and the counter clockwise (CCW) transverse magnetic modes in the microring have a different effective index and a split between their resonance wavelengths occurs [28]. The value of the resonance wavelength split (RWS) is

$$\Delta \lambda_M^0 = \frac{\Delta n_{\rm eff}}{n_g} \lambda \tag{1}$$

where $\Delta n_{\rm eff}$ is the effective index difference between CW and CCW mode, and n_g is the average group index with respect to the two directions, both computed at room temperature (i.e., $T_{\rm amb} = 20 \,^{\circ}$ C).

The RWS is proportional to the Faraday rotation constant, which is equal to $-4500^{\circ}/\text{cm}$ at room temperature for an in-plane (radial) magnetic field larger than 50 Oe [24]. Below the magnetic saturation, its value can be approximated as a hyperbolic tangent. Moreover, as the device heats up, the Faraday rotation will change by $d\theta_F/dT = +44^{\circ}/\text{K}$ [29]. Combining these two effects, we have

$$\theta_F(H_r, T) = \left[\theta_F^0 + \frac{d\theta_F}{dT} \left(T - T_{\rm amb}\right)\right] \cdot \tanh\left(\frac{H_r}{H_r^0}\right) \quad (2)$$

where $\theta_F^0 = -4500 \,^{\circ}/\text{cm}$ and $H_r^0 = 24$ Oe [25]. As a result, below the saturation and for $T > T_{\text{amb}}$, the MO resonance wavelength split decreases and its value is rescaled as

$$\Delta\lambda_M(H_r, T) = \frac{\Delta\lambda_M^0}{\theta_F^0} \theta_F(H_r, T)$$
(3)

The DC current, used to generate the magnetic field, might also cause a local heating due to the Joule effect. From the electromagnetic modal analysis of the microring with respect to the temperature, the thermal (reciprocal) resonance wavelength shift is $\Delta \lambda_T$ valued as

$$\Delta \lambda_T = \frac{\lambda}{n_g} \left(\sum_i \frac{\partial n_{\text{eff}}}{\partial n_i} \frac{\partial n_i}{\partial T} \right) \Delta T \tag{4}$$

where the derivative $\partial n_i / \partial T$ depends on the materials with refractive index n_i , while $\partial n_{\text{eff}} / \partial n_i$ can be computed from the mode solver [30]. For the device under investigation, we computed a resonance wavelength shift of 71.6 pm/°C for the TM mode [25].

Including both thermal and MO contributions, the total resonance wavelength shift is

$$\Delta \lambda = \Delta \lambda_T(T) \pm \frac{1}{2} \Delta \lambda_M(H_r, T)$$
(5)

where \pm refer to the CW and CCW modes, respectively.

B. Waveguide Cross-Section Optimization

A fully etched silicon waveguide is assumed in our design. The device is shown in Fig. 1. A silicon microring resonator is fabricated on a SOI wafer, having refractive index $n_{Si} = 3.48$ and $n_{SiO2} = 1.46$ at $\lambda = 1550$ nm, respectively. The microring is bonded with a Ce:YIG garnet ($n_{Ce:YIG} = 2.22$) previously grown on a (Ca,Mg,Zr)-substituted gadolinium gallium garnet (SGGG), ($n_{SGGG} = 1.97$). The remaining space is filled by air. At the interface between the Ce:YIG and the silicon, a thin silica (SiO₂) layer is considered, which is a byproduct of the oxygen plasma assisted bonding of the Ce:YIG. All materials are low loss at $\lambda = 1550$ nm, with the exception of the Ce:YIG which has a propagation loss of about 60 dB/cm, included in the mode analysis.

The nonreciprocal behavior of the hybrid Ce:YIG/Si waveguide is analyzed using an accurate nonreciprocal mode solver based on the finite element method [30]. The silicon waveguide cross-section is designed to maximize the RWS in Eq. (1) [25], [28]. In [28] the waveguide cross-section has been optimized assuming $\theta_F = -4000$ °/cm and no SiO₂ bonding layer, while in [25] $\theta_F = -4500^\circ$ /cm and a 10 nm thick oxide layer are



Fig. 2. (a) RWS computed with respect to the Faraday rotation constant and the silica bonding layer thickness. (b) RWS variation with respect to the fabrication error for $\theta_F = -4500^{\circ}/\text{cm}$ assuming $h_{Si} = 230 \text{ nm}$, $w_{Si} = 600 \text{ nm}$, $h_{Ce:YIG} = 230 \text{ nm}$, and $h_{SiO2} = 10 \text{ nm}$.



Fig. 3. (a) Radial magnetic field at the silicon/Ce:YIG interface (b) average temperature variation in the silicon microring for a microring radius of 35 μ m. In both plots the current and the SGGG thickness are varied.

considered. Nevertheless, the optimum cross-sections in the two cases are very similar.

Assuming a 230 nm \times 600 nm silicon waveguide crosssection, and 400 nm thick Ce:YIG layer, we investigate the degradation of the RWS with respect to the bonding oxide layer thickness. As shown in Fig. 2(a), the oxide layer thickness must be precisely controlled in order to provide a large RWS. On the other hand, large variation on the silicon waveguide width ($\Delta w_{\rm Si}$), the silicon waveguide thickness ($\Delta h_{\rm Si}$), and the Ce:YIG thickness ($\Delta h_{\rm Ce:YIG}$) are less critical, as shown in Fig. 2(b) for a comparison with silica thickness ($\Delta h_{\rm SiO2}$).

C. Single and Multi-Coil Electromagnet

The electromagnet can be fabricated on the back-side of the SGGG substrate, which has been thinned to reduce the distance between the current and the Ce:YIG layer. In order to provide a large magnetic field while limiting the heating, a large current and a small resistance are required. For this purpose, a single gold microstrip coil is designed with a 3 μ m wide and 1.5 μ m thick cross-section [25].

The radial magnetic field and the temperature distribution have been computed using COMSOL Multiphysics software. In Fig. 3(a), the intensity of H_r at the Si/Ce:YIG interface is shown as a function of the electromagnet current (*I*) and the SGGG thickness. For the same input values, the average temperature increment ($\Delta T = T - T_{amb}$) in the silicon microring is reported in Fig. 3(b).



Fig. 4. Multiphysics simulation results: (a) radial magnetic field (in Oersted) generated by the electric current I = 180 mA, (b) temperature distribution (in Celcius) in the device.



Fig. 5. Electromagnet comparison (a) radial magnetic field at the silicon-Ce:YIG interface (b) average temperature variation in the silicon microring.

From the numerical results in Fig. 3, for a fixed current value, the magnetic field is much more sensitive to the SGGG thickness than the temperature. Moreover, for a fixed SGGG thickness, the magnetic field scale linearly with the current while ΔT varies quadratically with the current, as expected. The same behaviour is better visible in Fig. 5.

To increase the radial magnetic field without further thinning the SGGG layer, which can be challenging to fabricate, a multiloop spiral solution is preferred [31]. For multiple-loop, two level of metal are needed. In Fig. 4, the numerical results are reported for the 3 loop spiral integrated planar electromagnet. The intensity of H_r at the Si/Ce:YIG interface is shown in Fig. 4(a) assuming I = 180 mA and 5 μ m-thick SGGG substrate. Under the same condition the temperature distribution ΔT is shown in Fig. 4(b). From both images, it is clear that the magnetic field and temperature variation are local and do not affect devices that are relatively far from it.

The performance of single loop, 3-loops and 5-loops are compared. In Fig. 5(a), the magnetic field in the Ce:YIG is computed as a function of the injected current for 5 μ m-thick SGGG layer. For the same value, the temperature in the silicon is reported in Fig. 5(b). Those simulation results can be effectively used to compute $\Delta \lambda_M$ and $\Delta \lambda_T$ described by Eq. (3) and Eq. (4), respectively. Those simulations are key to understanding the behavior of the device at different driving currents.

D. Model Validation

We experimentally validate the model by testing a nonreciprocal microring-based device with a single coil electromagnet.



Fig. 6. Experimental results showing both the MO nonreciprocal wavelength split as well as the reciprocal thermally induced redshift.

For a fixed DC current, we record the transmittance of the device as we sweep the tunable laser wavelength, and repeat the measurements for the backwards transmission. The split between the two resonances is measured directly from the forward and backward spectra, while $\Delta \lambda_T$ is computed as the average shift of the CW and CCW wavelength resonances with respect to the resonance at I = 0. In Fig. 6, we see a clear resonance split of roughly 0.32 nm for 140 mA of applied current (roughly 20 Oe of applied field) and a thermally induced redshift of 0.4 nm.

Reversing the direction of the current, produces a field with same amplitude but opposite direction while the heating is unchanged. As a result, we can write

$$\Delta\lambda(I) = \Delta\lambda_T(I) - \frac{1}{2}\Delta\lambda_M(I)$$
 (6a)

$$\Delta\lambda(-I) = \Delta\lambda_T(-I) + \frac{1}{2}\Delta\lambda_M(-I)$$
 (6b)

where *I* is the electromagnet current. From the previous relations, $\Delta \lambda_M$ are $\Delta \lambda_T$ can be easily derived. A comparison between the model and the experimental results is shown in Fig. 7 as a function of the coil-current for different layer thickness and microring radius. For 5 μ m-thick SGGG substrate and 35 μ m microring radius, the RWS and the thermal shift are shown in Fig. 7(a) and (c), respectively. Analogous results are shown in Fig. 7(b) and (d) for a SGGG layer of 8 μ m and R = 20 μ m. All the derived results show an excellent agreement between the experiments and simulations.

The thermal dissipation and consequent resonant wavelength shift $\Delta \lambda_T$ can be reduced by decreasing the spiral resistance, e.g. depositing a thicker metal trace or widening the microstrip footprint.

III. INTEGRATED OPTICAL ISOLATOR

An optical isolator can be fabricated using a straight waveguide coupled to a single microring resonator (all-pass microring filter) as shown in Fig. 1(a). In this case, the forward propagating light is coupled to the CW mode, while the backward light is coupled to the CCW mode. When the optical input is set off-resonance for the CW and on-resonance for the CCW, the forward light is transmitted while the backward light is filtered



Fig. 7. Experiment and simulation comparison of a single coil electromagnet (a) $\Delta\lambda_M$ for 5 μ m-thick SGGG and 35 μ m microring radius, (b) $\Delta\lambda_M$ for 8 μ m-thick SGGG and 20 μ m microring radius, (c) $\Delta\lambda_T$ for 5 μ m-thick SGGG and 20 μ m microring radius, (d) $\Delta\lambda_T$ for 8 μ m-thick SGGG and 20 μ m microring radius.



Fig. 8. Optical isolation as a function of the current (top-axes) and the nonreciprocal resonance wavelength split (bottom-axes).

and radiated out by the microring. To maximize the isolation, the coupling between the waveguide and the microring must have its critical value [28].

A. All-Pass Single Microring Isolator

Recently, we have experimentally demonstrated a large isolation in a nonreciprocal all-pass single microring isolator with a 35 μ m microring radius. A 32 dB of isolation is measured near 1555 nm with only 2.3 dB of excess loss to silicon [25].

Fig. 8 shows the measured optical isolation as a function of the injected current. The NRS is also reported at the bottom axis of the same figure. An optical isolation larger than 25 dB is measured for I between 40 mA and 180 mA. For small value of current (I < 40 mA), the resonances of the CW and CCW mode are too close. On the other hand, for larger values of current, the microring heats up and it moves out of the critical coupling condition, causing the isolation to drop. For I = 180 mA, a thermal shift up to 0.75 nm is reached (see Fig. 7(c)). This result suggests that the thermal effect can be used to finely tune the microring resonator in order to compensate unavoidable fabrication errors. However, further design optimization is needed.



Fig. 9. (left) Cascaded microring-based isolator. (right) Transfer functions of the first isolator, second isolator and final transfer function. Pictures are not to scale.



Fig. 10. Microscope image of the fabricated device with splits for various microring-waveguide coupling distances.

Resonant-based filters are highly selective in wavelength so a microring-based isolator can effectively isolate the narrowlinewidth output signal of a laser. For some applications (e.g., modulated signal or sensors), the bandwidth of a single microring can be too narrow and multi-microring isolators can successfully be used to enlarge the bandwidth and the isolation [32].

B. Cascaded Ring Isolator

The optical isolation bandwidth can be effectively enlarged by cascading two identical optical isolators, as shown in Fig. 9. To provide the largest isolation, the amplitudes of the currents in the two electromagnets are chosen such that the CCW resonances of the two microrings are aligned with the input signal wavelength (λ_{IN}), while the CW resonances fall apart, at higher and lower wavelength, respectively. A schematic plot of each isolator spectra and the cascaded transfer function are shown in Fig. 9. The light propagates from IN-port to OUT-port without obstacle, while in the opposite direction the light is coupled into the rings.

In the two electromagnets, the currents flow in opposite directions to provide the opposite nonreciprocal wavelength split direction shown in Fig. 9.

The fabricated devices are shown in Fig. 10, where the SGGG layer is 5 μ m thick, the radius of both microrings is 20 μ m, and the distance between their centers is set to 100 μ m. The microring-waveguide coupling distance is varied from 200 nm



Fig. 11. Experimental total resonance wavelength shift of the two microrings: (a) the current in the first isolator is swept while $I_2 = 0$, (b) the current in the second isolator is swept while $I_1 = 0$.



Fig. 12. (a) Nonreciprocal wavelength split and the thermal shift in the two microrings when the amplitude of I_1 varies from 0 to 240 mA and $I_2=0,$ (b) Nonreciprocal wavelength split and the thermal shift in the two microrings when the amplitude of $I_1=0$ and I_2 varies from 0 to 240 mA.

up to 260 nm, therefore different coupling coefficients are realized.

For a microring-waveguide coupling distance of 230 nm, the experimental total resonance wavelength shift of both microrings is shown in Fig. 11. In this device, the critical coupling condition is achieved for $\lambda \sim 1460$ nm. In Fig. 11(a) the current in the first isolator (I₁) is swept from -240 mA to 240 mA, while the current in the second isolator (I₂) is zero. Vice versa, in Fig. 11(b) I₁ = 0 and I₂ is swept from -240 mA to 240 mA.

Although the microrings are designed to be identical, when $I_1 = I_2 = 0$, the two resonances are not aligned due to small fabrication errors, and their values are $\lambda_{res,1} = 1460.54$ nm and $\lambda_{res,2} = 1460.40$ nm for microring 1 and microring 2, respectively. A slightly different current amplitude is injected so that the different thermal heating can be used to align the CCW-spectra and compensate the fabrication variation.

Considering the relations in Eq. (6), the nonreciprocal wavelength split and the thermal shift are derived for both microrings when $I_1 \neq 0$ and $I_2 = 0$, as shown in Fig. 12(a). The nonreciprocal phase shift of microring 1 reaches the maximum value of 0.302 nm for $I_1 = 200$ mA while the thermal shift is about 0.919 nm. Under this condition, the resonance of the second microring can slightly vary due to the thermal cross-talk (i.e., 0.075 nm) while the magnetic field cross-talk is negligible. Because the geometry of the devices is symmetric, very similar results can be obtained when $I_1 = 0$ and $I_2 \neq 0$, as shown in Fig. 12(b).

For $\lambda \sim 1500$ nm, the critical coupling condition is reached for a microring-waveguide coupling distance of about 200 nm. In this case, the optimal current values in the two electromagnet



Fig. 13. (a) Experimental forward and backward spectra of two-cascaded microring isolator. (b) Comparison of optical isolation in fabricated single and two-cascaded microring isolators with respect to the isolation bandwidth.

are $I_1 = 195$ mA and $I_2 = -170$ mA for the first and the second isolator, respectively. The experimental results are shown in Fig. 13(a), the CCW resonance of the two microrings are aligned and an isolation of about 28 dB is measured at $\lambda_{IN} = 1503.7$ nm. The measured isolation is slightly lower than the single microring isolator because both microrings must work at the critical coupling condition. However, the slight different temperature might affect this condition.

The isolation of a signal with a non-negligible bandwidth is computed as

$$IR = \int |S_{\rm CW}(\lambda)|^2 / |S_{\rm CCW}(\lambda)|^2 d\lambda \tag{7}$$

where $S_{\rm CW}(\lambda)$ and $S_{\rm CCW}(\lambda)$ are transition spectra of the whole device in the forward and backward direction, respectively. If $\lambda_{\rm IN}$ is the input wavelength and BW is the considered bandwidth, the integral is computed between $\lambda_{\rm IN} - BW/2$ and $\lambda_{\rm IN} + BW/2$. The optical isolations of fabricated single and two-cascaded microring isolator are plotted as a function of the signal bandwidth in Fig. 13(b), showing a larger isolation bandwidth for the cascaded-microring isolator.

IV. INTEGRATED OPTICAL CIRCULATOR

A microring-based optical circulator can be performed using a microring add/drop filter, as proposed in [33], [34]. In the following sections we present the experimental results for a single microring device and then the improvement can be achieved in term of bandwidth and isolation in a two-microring circulator.

A. Four-Port Add-Drop Microring Circulator

The optimization of a four-port microring circulator is detailed in [33]. Using the same design rules, an integrated optical circulator is fabricated and characterized for TM mode with bonded Ce:YIG. The device is schematically shown in Fig. 14(a). The fabricated devices are shown in Fig. 14(b), where the SGGG layer is 8 μ m thick and the microring radius is 20 μ m.

The closed four-port characteristics of the device can be easily verified. Indeed, when the CW and CCW resonances are differentiated and the input signal matches the CCW resonance of the nonreciprocal microring, the circulating direction is $P1\rightarrow P2\rightarrow P3\rightarrow P4\rightarrow P1$. Vice versa, when the signal wave-



Fig. 14. (a) Schematic structure of the TM-mode four-port optical circulator, pictures is not to scale, (b) microscope image of the fabricated device.



Fig. 15. Simulated (top) and measured (bottom) scattering coefficients of the single microring four-port optical circulator.

length matches the CW resonance wavelength, the circulating direction is reversed.

If the waveguide backscattering is negligible and the gaps between the microring and the two waveguides are the same [33], the input/output relation can be effectively described by the following simplified scattering matrix

$$\begin{pmatrix} A_1^-\\ A_2^-\\ A_3^-\\ A_4^- \end{pmatrix} = \begin{pmatrix} 0 & S_{12} & 0 & S_{14} \\ S_{21} & 0 & S_{41} & 0 \\ 0 & S_{14} & 0 & S_{12} \\ S_{41} & 0 & S_{21} & 0 \end{pmatrix} \begin{pmatrix} A_1^+\\ A_2^+\\ A_3^+\\ A_4^+ \end{pmatrix}$$
(8)

where A_i^+ (for i = 1, 2, 3, 4) is the field that travel toward the circulator from port Pi and A_j^- (for j = 1, 2, 3, 4) is the field that leaves the microring from port Pj. To perform the P1 \rightarrow P2 \rightarrow P3 \rightarrow P4 \rightarrow P1, $|S_{12}|$ and $|S_{41}|$ must be smaller compared to $|S_{21}|$ and $|S_{14}|$ [33].

The simulated and the experimental spectra are shown in Fig. 15. The plots show a very good agreement between theory and measurements. However, the unavoidable fabrication inaccuracy might cause small geometry variation and so a shift of the spectra with respect to the simulated ones. To better compare the spectra, the simulated ones have been blueshifted by 0.633 nm to be aligned with the experiments. The dashed line in the figure indicates the CCW resonance wavelength.

Because the bonded chip is 3.5 mm long, the propagation loss in the input/output waveguide is estimated to be 8.7 dB due to the large absorption of the Ce:YIG. Nevertheless, it can be



Fig. 16. Schematic structure of the two-microring four-port optical circulator. Pictures is not to scale.



Fig. 17. Simulated spectra of single and two- microring circulators.



Fig. 18. Comparison of simulated optical isolation in single and two- microring circulators with respect to the isolation bandwidth.

strongly reduced by removing the areas of the bonded chip that are not covering the microring. The measured optical isolation at $\lambda_{\rm res,ccw} = 1558.38$ between adjacent ports is 11 dB between port P1 and port P2 (i.e., IR₁₂ = $|S_{21}|/|S_{12}|$), and 6.7 dB between port P1 and P4 (i.e., IR₄₁ = $|S_{14}|/|S_{41}|$) [35]. The two isolation ratios IR_{12} and IR_{41} differ because the estimated coupling coefficient in the fabricated device (K = 10.45%) is larger than the optimum value for $\Delta\lambda_{\rm M}=0.35$, which is K = 9.0%. In Fig. 15, the simulated coefficients are computed in the former case.

B. Coupled Microring Circulator

A second order filter can be effectively used to enlarge the optical isolation and the isolation bandwidth. The schematic view of the two-microring circulator is shown in Fig. 16 and its scattering matrix is like the one of Eq. (8).

The light in the two microrings in Fig. 16 propagates in opposite directions. As a result, to properly align the miroring resonances, the current in the two electromagnet must have the same intensity but opposite direction.

The performance of the simulated two-microring isolator is compared with the simulated single-microring circulator. For the single microring, we assumed a waveguide-microring power coupling coefficient of 9%, while in the two-microring device the waveguide-microring and microring-to-microring power coupling coefficients are 13.16% and 0.5%, respectively [36]. For both devices the microring radius is 20 μ m and the SGGG is 8 μ m thick. The magnitude of the simulated scattering coefficients is shown in Fig. 17.

For the single microring circulator, the isolation ratio is $IR_{12} = IR_{41} = 9.15 \text{ dB}$ at $\lambda_{res,ccw} = 1550 \text{ nm}$, while double for the coupled microring device, $IR_{12} = IR_{41} = 18.3 \text{ dB}$. Similarly, the isolation bandwidth is double for a fixed isolation ratio, as shown in Fig. 18.

Note that the isolation of the simulated single-microring circulator is lower (i.e., 9 dB) than largest isolation in the fabricated one (i.e., 11 dB). However, in the former case all ports have the same isolation ratio, while in the latter case their values are quite unbalanced (i.e., 11 dB and 6.7 dB).

V. CONCLUSION

In this work, we present a comprehensive examination of the performance of single-microring and two-microring integrated optical isolators and circulators. The experimental results have been compared with a reliable mathematical model, showing excellent agreement. Some promising improvements, like the multi-coil electromagnet and the coupled-microring circulator, have been proposed and investigated. Although those devices work only for the TM polarized light, transverse electric isolator and circulator can be fabricated by adding polarization rotators at the input. The proposed approach represents a viable solution in integrated optics, proved by the large isolation and small footprint. Moreover, the proposed electromagnet can provide local control of the magnetic field, eliminating the need for a bulky permanent magnet and easing packaging requirements. Finally, the current induced magnetic field can be switched and modulated, leading to a new class of magneto-optic devices for silicon photonics.

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Duanni Huang received the B.S. degree in electrical engineering from the Massachusetts Institute of Technology, Cambridge, MA, USA, in 2013, the M.S. degree in electrical engineering, in 2015, from the University of California, Santa Barbara, CA, USA, where he is currently working toward the Ph.D. degree. His current research interest focuses on silicon photonics, with an emphasis on magneto-optic and other nonreciprocal phenomenon.

Paolo Pintus (S'10–M'11) was born in Cagliari, Italy, in 1983. He received the Bachelor's degree (with Hons.) and the Master's degree (with Hons.) in electronic engineering from the University of Cagliari, Cagliari, Italy, in 2005 and 2007, respectively, and the Ph.D. degree in innovative technologies of ICT and robotics from the Scuola Superiore Sant.Anna, Pisa, Italy, in 2012.

From 2012 to 2016, he was a Research Fellow at Scuola Superiore Sant'Anna, Pisa, Italy. He is currently a Project Scientist at the University of California, Santa Barbara, CA, USA. His research interests include integrated optics, silicon photonics, and numerical method for electromagnetism.

Dr. Pintus is a Member of the IEEE Photonic Society and the Italian Society for Industrial and Applied Mathematics.

Chong Zhang (S'13–M'16) received the B.S. degree in electrical science and technology from the Harbin Institute of Technology, Harbin, China, in 2007, the M.S. degree in optical engineering from Zhejiang University, Hangzhou, China, in 2010, and the Ph.D. degree in electrical and computer engineering from the University of California, Santa Barbara, CA, USA, in 2017. He is working at Hewlett Packard Labs since 2016. His research interests include epitaxial growth of III/V materials on silicon, heterogeneous silicon integration, and high speed photonic integration circuits in the applications of optical interconnects.

Yuya Shoji (M'09) received the B.E., M.E., and Ph.D. degrees in electrical engineering from the Tokyo Institute of Technology, Tokyo, Japan, in 2003, 2005, and 2008, respectively. He was a Postdoctoral Fellow with the National Institute of Advanced Industrial Science and Technology, Tsukuba, Japan, from 2008 to 2010. He has been an Assistant Professor with the Graduate School of Science and Engineering, Tokyo Institute of Technology, from 2011 to 2014. He is currently an Associate Professor with the Laboratory for Future Interdisciplinary Research of Science and Technology, Tokyo Institute of Technology. His current research interests include device designs and fabrication of magneto-optical devices, silicon nanophotonic devices, and the photonic integrated circuits. He is a member of the Optical Society of America, the Institute of Electronics, Information and Communication Engineers, the Japan Society of Applied Physics, and the Magnetic Society of Japan.

Tetsuya Mizumoto (S'81–M'84–F'12) received the B.Eng. degree in electrical and electronic engineering in March 1979, the M.Eng. degree in physical electronics in March 1981, and the Dr. Eng. degree in electrical and electronic engineering in March 1984, all from the Tokyo Institute of Technology (Tokyo Tech), Tokyo, Japan. He began working for Tokyo Tech in April 1984 as a Research Associate in the Faculty of Engineering and became an Associate Professor in March 1987. He was promoted to a Full Professor in the Graduate School of Engineering in April 2004. His research interests include applied optics and photonic circuits. His research activity has been concerned mainly with waveguide optical devices, especially magneto-optic devices and all-optical switching devices based on the third-order nonlinearity.

He received the Treatise Award in 1994 and the Best Letter Award of Electronics Society Transactions in 2007 from the Institute of Electronics, Information and Communication Engineers (IEICE). He was awarded the Institute of Electrical and Electronics Engineers (IEEE) Photonics Society Distinguished Lecturer Awards in July 2009, the IEEE Fellow grade for "Contributions to investigations of waveguide optical nonreciprocal devices for optical communications" in January 2012, and IEICE Achievement Award for "Pioneering work on optical nonreciprocal circuits" in May 2012. He is a fellow of IEICE, member of the Japan Society of Applied Physics, and the Magnetic Society of Japan.

John E. Bowers (F'93) received the M.S. and Ph.D. degrees from Stanford University, Stanford, CA, USA. He was with AT& Bell Laboratories and Honeywell before joining University of California, Santa Barbara (UCSB). He holds the Fred Kavli Chair in Nanotechnology, and is the Director of the Institute for Energy Efficiency and a Professor in the Departments of Electrical and Computer Engineering and Materials, UCSB. He has published 10 book chapters, 600 journal papers, 900 conference papers, and has received 54 patents. His research interests include optoelectronics and photonic integrated circuits. He is a cofounder of Aurrion, Aerius Photonics and Calient Networks. He is a member of the National Academy of Engineering and a Fellow OSA and the American Physical Society. He received the OSA/IEEE Tyndall Award, the OSA Holonyak Prize, the IEEE LEOS William Streifer Award, and the South Coast Business and Technology Entrepreneur of the Year Award. He and coworkers received the EE Times Annual Creativity in Electronics (ACE) Award for Most Promising Technology for the heterogeneous silicon laser in 2007.