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**Heterostructure Integrated Thermionic  
Cooling of Optoelectronic Devices**

by

Christopher LaBounty

Ph.D. Dissertation

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Department of Electrical and Computer Engineering  
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**Heterostructure Integrated Thermionic Cooling of Optoelectronic Devices**

A dissertation submitted in partial satisfaction of the  
requirements for the degree of

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in

Electrical Engineering

by

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by

Christopher John LaBounty

*This dissertation is dedicated to  
my wife to be, Colleen, for her enduring support,  
and my family  
who have always been there for me ...*

## ACKNOWLEDGEMENTS

As many can attest, time spent at UCSB seems to pass by so very fast. My enjoyment of these past years can be mostly attributed to the wonderfully talented and interesting people that I have had the pleasure to know. It is these individuals for which I would like to acknowledge.

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## **ABSTRACT**

Heterostructure Integrated Thermionic Cooling of Optoelectronic Devices

by

Christopher John LaBounty

Active refrigeration of optoelectronic components through the use of heterostructure integrated thermionic emission cooling is proposed and investigated. Enhanced cooling power compared to the thermoelectric effect of the bulk material is achieved through thermionic emission of hot electrons over a heterostructure barrier layer. These heterostructures can be monolithically integrated with other devices made from similar materials. The advantages of this type of integrated cooling as well as heterogeneous integration are discussed. From careful theoretical analysis, practical design guidelines are developed and applied to several thermionic cooler structures. Cooling performance is investigated for various device parameters and operating conditions. Several important non-ideal effects are identified such as contact resistance, heat generation and conduction in the wire bonds, and the finite thermal resistance of the substrate. These non-ideal effects are studied both experimentally and analytically, and the limitations induced on performance are considered. Full three-dimensional self-consistent thermal/electrical simulations are used to optimize the non-ideal effects. Several optoelectronic devices have been integrated with these coolers, and the results are presented. Thermionic emission cooling in

heterostructures is shown to provide cooling of several degrees Celsius and cooling power densities of several 100's W/cm<sup>2</sup>. These micro-refrigerators can provide control over device characteristics such as output power, wavelength, and maximum operating temperature.

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## **Chapter 1**

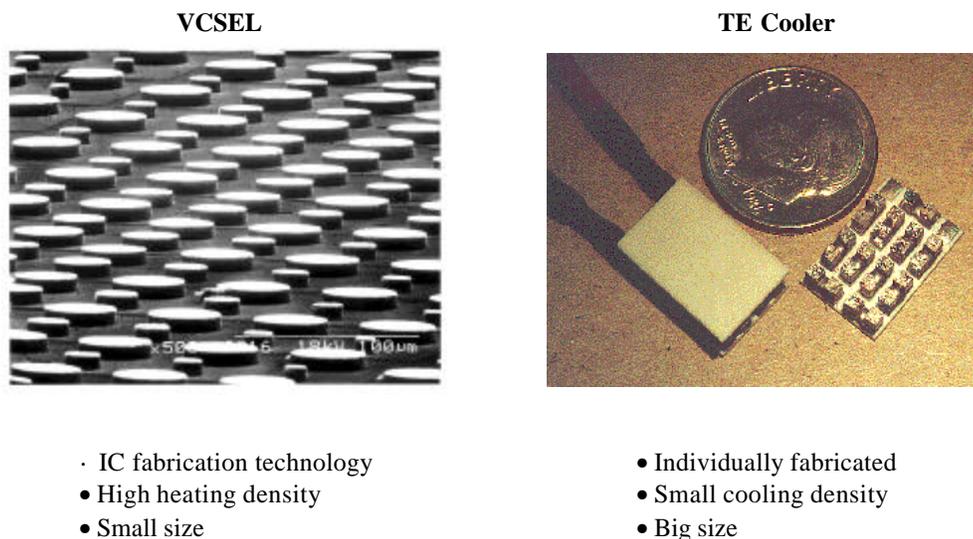
### **Introduction**

With the explosion in bandwidth of modern day and next generation high-speed optical networks, there is a definite demand for higher performance optoelectronic devices. The trend towards miniaturization, higher speed operation, and greater density of these devices has increased the need for efficient heat removal and thermal management.

During the growth of the telecommunications industry, conventional thermoelectric (TE) coolers quickly found applications in cooling and temperature stabilization for components such as laser sources, switching/routing elements, and detectors. This is especially true in current high speed and wavelength division multiplexed (WDM) optical communication networks. Long haul optical transmission systems operating around 1.55  $\mu\text{m}$  typically use erbium doped fiber amplifiers (EDFA's), and are restricted in the wavelengths they can use due to the finite bandwidth of these amplifiers. As more channels are packed into this wavelength window, the spacing between adjacent channels becomes smaller and wavelength drift becomes very important. Temperature variations are the primary cause in wavelength drift, and also affect the threshold current and output power in laser sources. Distributed feedback (DFB) lasers and vertical cavity surface emitting lasers (VCSEL's) can generate large heat power densities on the order of  $\text{kW}/\text{cm}^2$

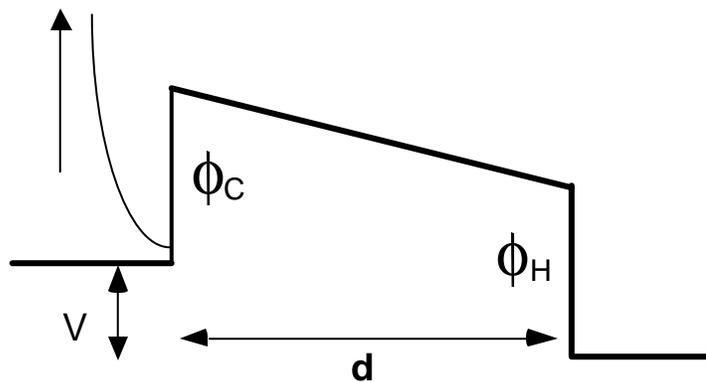
over areas as small as  $100 \mu\text{m}^2$  [1]. Typical temperature-dependent wavelength shifts for these laser sources are on the order of  $0.1 \text{ nm}/^\circ\text{C}$ . Therefore, a temperature change of only a few degrees in a WDM system with a channel spacing of  $0.2\text{--}0.4 \text{ nm}$  would be enough to switch data from one channel to the adjacent one, and even less of a temperature change could dramatically increase the crosstalk between two channels. More generally speaking, in many optoelectronic applications this temperature dependence is used to actively control the characteristics of the device as in tunable optical filters [2] or switches [3,4]. In other instances, large absolute cooling is desired as in IR photodetectors [5].

While TE coolers have sufficed for the time being, their integration with optoelectronic devices is difficult [6], increasing the component cost greatly because



**Figure 1.1** Characteristic incompatibilities between VCSEL's and TE coolers. [VCSEL SEM by N. Margalit et al. 1997]

of packaging. Figure 1.1 illustrates the incompatibilities between TE coolers and VCSEL's as an example. The reliability and lifetime of packaged modules can also in some cases be limited by the TE cooler [7]. An alternative solution to thermal management needs is to incorporate heterostructure integrated thermionic (HIT) refrigerators with optoelectronic devices [8,9]. These thin film coolers use the selective thermionic emission of hot electrons over a heterostructure barrier layer to increase the cooling power beyond what can be achieved with the bulk thermoelectric properties (see Figure 1.2). This enhanced evaporative cooling occurs since the hot electrons that are on one side of the Fermi energy are emitted. In order to maintain the quasi equilibrium Fermi distribution, lower energy electrons absorb thermal energy from the lattice at the junction. The emitted electrons then redeposit their energy after passing over the barrier. Since these thin film coolers can be made with conventional III–V semiconductor materials, low-cost monolithic-integration



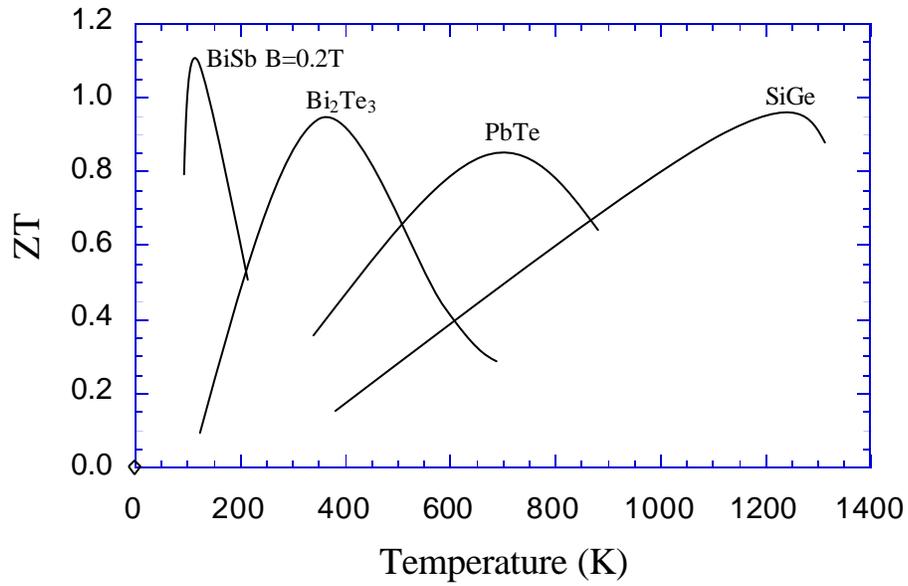
**Figure 1.2** Conduction band diagram of a heterostructure integrated thermionic (HIT) cooler under an applied bias.

with optoelectronics is possible. Furthermore, standard integrated-circuit batch-fabrication techniques can be used to manufacture these coolers, whereas TE coolers use a bulk fabrication process.

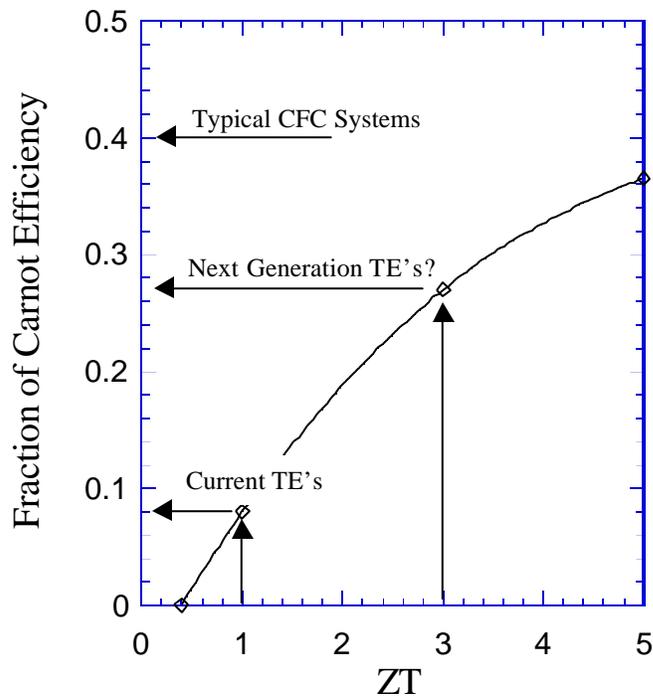
In this chapter, current solid state cooler technology is first reviewed to illustrate the merits of various approaches to increasing cooling capabilities. The second section will discuss the motivation for moving from bulk (thick) coolers to thin-film structures. Finally, the major contributions of this work will be outlined in the scope of this thesis.

## 1.1 Current Solid State Cooler Technology

There is an increasing push to improve the figure of merit for thermoelectric materials. This figure of merit is given by the dimensionless term  $ZT = (S^2 \mathbf{s} / \mathbf{k})T$ , where  $S$  is the Seebeck coefficient,  $\mathbf{s}$  and  $\mathbf{k}$  are the electrical and thermal conductivities, respectively, and  $T$  is the ambient temperature (see Appendix A). The best thermoelectric materials have a value of  $ZT \approx 1$  over a given temperature range as illustrated in Figure 1.3. This value has been an upper limit for over 30 years, yet mysteriously no theoretical reason exists to answer why it can't be larger. With the advent of new theories, materials, and analysis capabilities, it is predicted that this limit will be breached in the near future. Already, new theoretical predictions are indicating that indeed a higher  $ZT$  is possible, and initial experimental work is beginning to surface to validate these claims [10, 11]. Larger



**Figure 1.3**  $ZT$ 's of various thermoelectric materials versus temperature.



**Figure 1.4** Fraction of Carnot efficiency versus the  $ZT$  of thermoelectrics.  $ZT$ 's greater than 3 will be required to begin competing with conventional CFC cooling systems.

$ZT$ 's will not only benefit cooling of electronics and optoelectronics, but may eventually allow solid-state cooling to compete with the more efficient CFC systems. Figure 1.4 shows how the  $ZT$  of thermoelectrics is related to the fraction of Carnot efficiency, which is the theoretical maximum efficiency possible. A  $ZT$  of at least three will be needed to compete with the efficiencies of CFC systems.

### 1.1.1 Bulk Thermoelectric Materials

The fundamental problem for a good TE material is that it must have a high electrical conductivity and at the same time a low thermal conductivity. However, in most solids these two physical properties are related, similar to the Wiedemann-Franz ratio in metals [12]. The ideal material possesses the poor thermal properties of glass and the excellent electronic properties of a crystal. Skutterudites, clathrates, and other open cage structures may possess these features [13, 14]. These compounds have cage-like crystal structures in which the spaces are filled with atoms that can effectively rattle around. This motion interferes with the conduction of heat but not electricity, making them ideal candidates for the next generation of bulk thermoelectrics. Rare-earth compounds and intermetallics are another group of potential thermoelectric materials that are being explored for their large Seebeck coefficients [15, 16]. While these new breeds of materials are a good direction for TE cooler research, their application to integrated cooling still suffers from the same problems discussed previously.

### 1.1.2 Micro-Thermoelectrics

Micro-thermoelectrics are a step closer in the direction of a practical cooler technology for integrated applications. This body of research explores the concept of making much smaller thermoelectric coolers with more advanced processing techniques. The smallest conventional bulk coolers typically have a thermoelement thickness on the order of a few millimeters, while micro-thermoelectrics can be loosely categorized into thick film ( $\sim 100$ 's  $\mu\text{m}$ ) and thin film ( $\sim 1$ - $10 \mu\text{m}$ ) structures. The materials used are commonly conventional thermoelectric materials such as BiTe or SiGe whose thermoelectric properties are well known, and where the challenge lies with processing the device. Many different techniques have been employed to miniaturize the cooler including electrochemical deposition [17], extrusion [18], micro-fabrication of thick [6, 19, 20] and thin [21, 22] films to name a few. Several of these techniques have produced working prototypes, with the thick film devices typically demonstrating superior performance. This is due to the increased non-ideal effects such as contact resistance and substrate thermal resistance. The motivation for continuing to pursue thin-film structures in the presence of these non-ideal effects will be discussed in Section 1.2.

Despite the infancy of micro-thermoelectric processing technology, several commercially available products do exist. Cooling capacities on the order of 1 Watt over areas as small as  $3\text{mm}^2$  have been achieved using high conductive thermal substrates and optimized contact resistances as low as  $10^{-6} \Omega\text{cm}^2$  [23, 24].

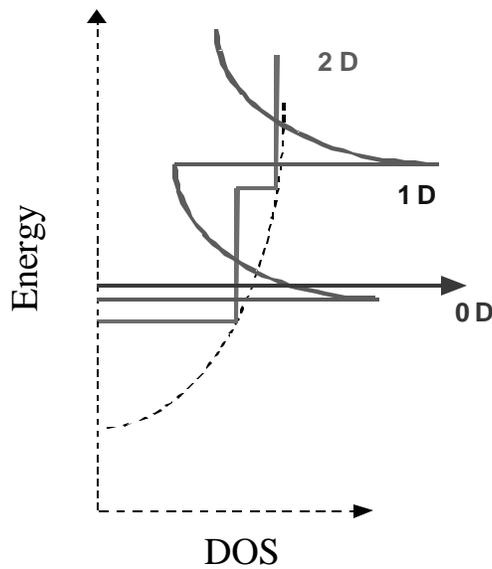
### 1.1.3 Lower Dimensional Structures

The development of thin film epitaxy, quantum wire, and quantum dot growth techniques have opened the door to a new class of thermoelectric materials. Just as the benefits of lower dimensional structures have advanced the electronic and photonic industries, so too have they allowed for novel approaches to improving solid-state cooling [25-27].

As the dimensionality is reduced, the electronic density of states accumulates near the subband transitions. With appropriate doping, step changes and even delta changes in available states for electrons result in a strong asymmetry in the differential conductivity [28, 29]. The consequence of this strong asymmetry is an enhanced thermopower which corresponds to the numerator of the  $ZT$  factor. Figure 1.5 depicts the density-of-states (DOS) versus energy in the 1-D, 2-D, and 3-D regimes. The optimum transport distribution has been shown to be a Dirac delta function centered about 2-3  $k_B T$  above or below the Fermi energy [30]. Further discussion of the differential conductivity as it relates to thermoelectrics and thermionics will follow in Chapter 2.

When designing lower dimensional structures, superlattices are typically used since they provide the additional benefit of reducing the thermal conductivity [31-33], *i.e.* the denominator of the  $ZT$  factor. With careful design of the materials, thickness, and period of the superlattices, phonon-blocking electron-transmitting structures can be realized [34].

The advantages of heterostructure thermionic cooling can be combined with that of lower dimensional structures by using multi quantum-well structures. The added constraint on the number of available electronic states should provide additional electron filtering and further improve the thermopower.



**Figure 1.5** The electronic density of states (DOS) versus energy for various dimensionalities (3D, 2D, 1D, and 0D). The first two quantified states are plotted.

## 1.2 Motivation for Thin Film Coolers

A distinct advantage of thin film coolers is the dramatic gain in cooling power density as it is inversely proportional to the length of the thermoelements. Thin films on the order of microns should provide cooling power densities greater than 1000 W/cm<sup>2</sup>. This capability for large cooling capacities is paramount for cooling of optoelectronic devices. Another convenience of thin films is that they allow for the

possibility of monolithic integration. Besides the lower cost and higher reliability, monolithic integration enables precise control over temperature anywhere on the surface of the substrate where the devices to be cooled are located. The small thermal mass of the cooler also permits a very fast cooling response.

Several disadvantages also become apparent and must be considered when moving from bulk to thin film coolers. The most evident is the reduction in the thermal resistance between the cold and hot side of the cooler. The trade-off for increased cooling power is a reduced temperature differential and efficiency. Other non-ideal effects such as contact resistance, thermal resistance of the heat sink, and heat generation in the current carrying connections are secondary effects in bulk TE coolers, but they all must be considered for thin film coolers [35].

### **1.3 Scope of Thesis**

This thesis presents the first comprehensive examination of a novel type of micro-cooler for integrated cooling applications. Using the established foundation of theory and first generation cooler design that had been completed prior to this work [9,36], the first semiconductor-based thermionic-emission cooler has been demonstrated and is described in this thesis. From this first generation of coolers, the results obtained drove continued theoretical and experimental work in cooler development and integration with optoelectronic devices. In addition, the first demonstration of integrated cooling with optoelectronics has also been achieved.

Parallel to the cooler research, advances in micro-scale temperature measurement techniques were developed. Great progress has also been made in the optimization of packaging, reduction of electrical contact resistance, and substrate transfer of thin films.

In Chapter 1, motivation for this work and an overview of relevant thermoelectric research was presented. Chapter 2 discusses more thoroughly the microscopic origins of the Peltier effect and presents a theory of thermionic cooling in heterostructures. From this theory, design guidelines are developed for the specific cooler structures which are discussed in Chapter 3. Chapter 4 examines the pertinent material properties and the techniques to measure them. The evolution of the device fabrication and packaging is presented in Chapter 5. Chapter 6 discusses measurement techniques and the experimental results and analysis. Chapter 7 presents several examples of the integration of heterostructure thermionic emission coolers with optoelectronic devices. Finally, Chapter 8 concludes with a review of the highlights from each chapter and suggestions for future work.

In summary, this thesis examines the novel approach of thermionic emission in heterostructures for enhanced cooling beyond the bulk properties of the materials, and the application of this technology to the integration of active cooling with optoelectronic devices.

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## Chapter 2

### Thermionic Emission in Heterostructures

The idea of thermionic energy conversion was first seriously explored in the mid-fifties during the development of vacuum diodes and triodes. Using a high work function cathode in contact with a heat source, electrons are emitted (thermionic emission process) and are absorbed by a cold, low work function anode. The electrons then flow back to the cathode through an external load where they perform useful work. Practical thermionic generators are limited by the work function of available materials that are used for cathodes. Another important limitation is the space charge effect, where the presence of charged electrons in the space between cathode and anode creates an extra potential barrier, reducing thermionic current. Various means of reducing this space charge effect were proposed to improve the efficiency of thermionic generators, such as close-spacing of the cathode and anode, or the use of a third positive electrode to counteract space charge. A major advance in the field occurred in 1957 when the introduction of positive ions (cesium vapor) in the inter-electrode space eliminated the need for the close spacing and resulted in substantial improvements in performance. The materials currently used for cathodes have work functions greater than  $0.7\text{ eV}$  which limits the applications to high temperatures greater than  $500\text{K}$ . Recently, these vacuum diode thermionic generators were proposed for refrigeration [1]. Efficiencies over 80% of the Carnot

value were predicted, but the operating temperatures are still limited to greater than 500K.

Even more recently, thermionic emission cooling in heterostructures was proposed by Shakouri *et al.* [2] to overcome the limitations of vacuum thermionics at lower temperatures. With current epitaxial growth techniques such as molecular beam epitaxy (MBE) or metal-organic chemical vapor deposition (MOCVD), precise control over layer thickness and composition is possible. In conjunction with bandgap engineering, these techniques allow for the design of a new class of semiconductor thermionic emission devices with improved cooling capacities. Using various material systems such as GaAs/AlGaAs, InP/InGaAsP, Si/SiGe, structures with barrier heights of 0.0 to 0.5 eV can be grown reliably. In this case, the barrier height is determined by the band edge discontinuity between heterolayers. Depending on growth constraints and lattice mismatch between materials, it is possible to grade the barrier composition to construct internal fields and to enhance electron transport properties. Close and uniform spacing of cathode and anode is no longer an issue and can be achieved with atomic resolution. The problem of space charge, if it arises, can be controlled by modulation doping in the barrier region.

In this chapter, an intuitive picture of thermoelectric and thermionic cooling in semiconductors is first presented. From this basis, the concept of thermionic emission cooling is more fully examined and the design of optimized structures explored.

## 2.1 Intuitive Picture of Thermoelectrics and Thermionics

The expressions for electrical conductivity and Seebeck coefficient can be written as [3-5]:

$$\begin{aligned} \mathbf{s} &= \frac{e^2}{4\mathbf{p}^3} \iiint \mathbf{t}(k) v_x^2(k) \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) d^3k \\ &\equiv \int \mathbf{s}(E) \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) dE \end{aligned} \quad (2.1)$$

$$\begin{aligned} S &= \frac{1}{eT} \frac{\iiint \mathbf{t}(k) v_x^2(k) (E(k) - E_F) \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) d^3k}{\iiint \mathbf{t}(k) v_x^2(k) \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) d^3k} \\ &\equiv \frac{k_B}{e} \frac{\int \mathbf{s}(E) \frac{(E - E_F)}{k_B T} \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) dE}{\int \mathbf{s}(E) \left(-\frac{\mathcal{I}f_{eq}}{\mathcal{I}E}\right) dE} \ll \langle E - E_f \rangle \end{aligned} \quad (2.2)$$

where we introduce the "differential" conductivity:

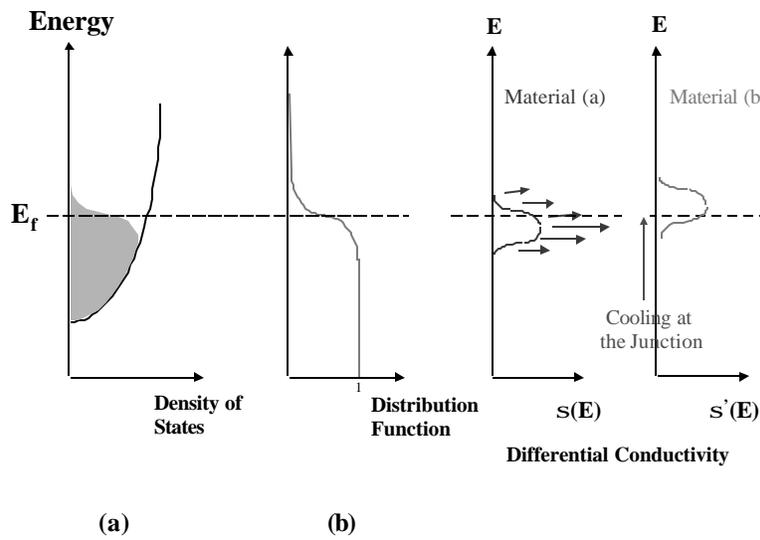
$$\mathbf{s}(E) \equiv e^2 \mathbf{t}(E) \iint v_x^2(E, k_y, k_z) dk_y dk_z \cong e^2 \mathbf{t}(E) \bar{v}_x^2(E) \bar{n}(E) \quad (2.3)$$

Here  $\mathbf{t}(E)$  is the energy dependent relaxation time,  $\bar{v}_x(E)$  the average velocity of the carriers with energy between  $E$  and  $E+dE$  in the direction of current flow, and  $\bar{n}_x(E)$  the number of electrons in this energy interval. Electrical conductivity is the sum of the contribution of electrons with various energies  $E$  (given by  $\mathbf{s}(E)$  the

differential conductivity) within the Fermi window factor  $\partial f_{eq}/\partial E$ . The Fermi window is a direct consequence of the Pauli exclusion principle, and at finite temperatures only electrons near the Fermi surface contribute to the conduction process. In this picture the Seebeck coefficient described in Equation 2.2 is the average energy transported by the charge carriers corresponding to a diffusion thermopower. This transported energy can be increased with the coupling of other energy transport mechanisms such as phonons to the electronic transit. As mentioned in Chapter 1, the overall device performance in conventional thermoelectric coolers is given by the dimensionless figure of merit  $ZT = S^2 \sigma T / \kappa$ , that describes the tradeoffs between the Peltier cooling given by the Seebeck coefficient ( $S$ ), the Joule heating given by the electrical conductivity ( $\sigma$ ), and the heat conduction from the hot to cold junction given by the thermal conductivity ( $\kappa$ ). It is this  $Z$ -factor that must be maximized to reach optimum performance and efficiency. At room temperature, conventional semiconductors have a thermal conductivity that is dominated by the lattice contribution, therefore maximizing  $Z$  necessitates maximizing the power factor  $S^2 \sigma \approx (\partial E - E_f)^2 \sigma$ . Hence the differential conductivity,  $\sigma(E)$ , should be *large* within the Fermi window and be as *asymmetric* as possible with respect to the Fermi energy.

The microscopic origin of the Peltier effect can be described as follows: When electrons move from a material in which their average transport energy is below the Fermi level, to another one in which their transport energy is increased, the electron

gas will absorb thermal energy from the lattice and the junction between the two materials will be cooled (see Fig. 2.1). Reversing the direction of current will instead generate heat and will create a hot junction signifying a reversible heat engine.



**Figure 2.1** (a) Energy versus density of states and Fermi distribution function for a degenerately doped  $n$ -type semiconductor. (b) The energy distribution of electrons moving in the semiconductor under an electric field is given by  $s(E)$  the differential conductivity that determines the average transport energy of carriers. As the average transport energy increases from material “a” to material “b”, thermal energy is absorbed from the lattice and the junction is cooled.

### 2.1.1 Lower Dimensional Structures Revisited

From the discussion above, the perceived advantage of moving to lower-dimensional semiconductor structures can be better explained than in Chapter 1. The number of electronic states in each energy interval is increased when the dimensionality is reduced, and at the same time the DOS “accumulates” near the subband edges, which

increases the asymmetry in  $S(E)$  if a proper doping is chosen. Recent literature on quantum well and wire thermoelectrics [6-9] emphasized the increased DOS, but the symmetry is not mentioned and its consequences are buried in the calculations of optimum doping in these structures. The symmetry of  $S(E)$  is the main cause of low thermopower in metals, even though they have a very large DOS.

Considering practical cooling applications, the advantages of using electron transport parallel to heterostructures is diminished by the finite thermal conductance of inactive barrier layers and other non-ideal effects [8-9,15]. Using bandstructure engineering, heterostructures can be designed that modify not only the DOS, but also the electron velocity and relaxation times. Based on these concepts, electron transport perpendicular to the quantum wells was proposed to reduce the mobility of low energy or “cold” electrons and to increase the thermopower [10-12]. A problem arises however, when only the effect of the DOS is considered in the mini-band conduction regime. Increasing the asymmetry of the DOS essentially means reducing  $\partial E/\partial k$ . However this reduction also results in a reduced electron velocity since it is also proportional to the band curvature  $\partial E/\partial k$ . Looking at Equation 2.3, these two effects are seen to be opposing each other, diminishing the benefits of asymmetry in  $S(E)$ .

All of these lower-dimensional concepts and primary calculations are based on the linearized Boltzmann transport equation which is valid in the band conduction regime and when the electronic distribution function is not changed considerably

with respect to the Fermi distribution. The application of heterostructures for thermoelectric cooling goes beyond the Boltzmann transport regime, complicating the theoretical analysis further.

### 2.1.2 Material Optimization for Traditional Thermoelectrics

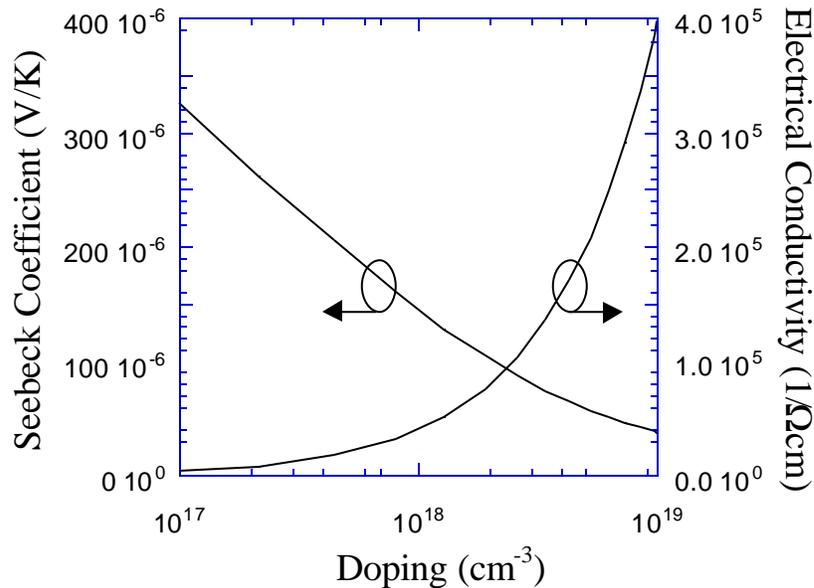
By optimizing the doping in the expressions for electrical conductivity and Seebeck coefficient, one can find that the following ratio of material parameters needs to be optimized [3-5,13,14]:

$$\left( \frac{m^*}{b} \cdot T_C \right) \quad (2.4)$$

The dependence on electron mobility in the material figure-of-merit expression reflects the importance of unimpeded electron transport in the material to reduce the Joule heating. The requirement for large effective mass is due to the symmetry of the electronic density-of-states with respect to the Fermi energy over an energy range that is on the order of thermal energy ( $k_B T$ ). The asymmetry may be increased by doping the material such that the Fermi level is close to the band edge, however this results in a small number of electrons taking part in conduction and a small amount of heat transported.

The trade off between Seebeck coefficient and conductivity versus doping is illustrated in Figure 2.2. As the doping is increased, the Seebeck coefficient decreases while the conductivity increases. The decline in Seebeck coefficient can

be explained by the reduced asymmetry in the DOS. Looking again at Figure 2.1, as the doping is increased and the Fermi level moves upward in energy, the DOS becomes more vertical and changes little above and below the Fermi energy. At these high doping densities, the situation is similar to the case of metals. Since the Fermi energy is deep inside the band, there are almost as many electrons above the Fermi energy as below, so the average energy of the moving electron gas under an electric field is very close to the Fermi level. The rise in the conductivity is simply a result of more carriers being present, even despite the reduction in electron mobility due to charged impurity scattering. The product of  $S^2 \sigma$  then gives the power factor versus doping, or the  $ZT$  after being divided by the thermal conductivity and multiplied by temperature.



**Figure 2.2** Calculation of Seebeck coefficient ( $S$ ) and electrical conductivity ( $\sigma$ ) as a function of doping for InGaAs bulk material. The substantial decrease in  $S$  at high dopings and  $\sigma$  at low dopings is the cause of low power factor and thus poor  $ZT$ .

### 2.1.3 Thermionic Emission Cooling in Heterostructures

Another more promising way to increase the asymmetry of  $\mathbf{s}(E)$  is to use thermionic emission in heterostructures. Using conduction (*n*-type) or valence (*p*-type) band offsets at heterointerfaces, the transport energy of electrons can be made to be almost entirely on one side of the Fermi level resulting in strong asymmetry [1,10-11,16-21]. In a simplified model [16-17] that neglects the finite electron energy relaxation length, the maximum cooling temperature by heterostructure thermionic emission can be expressed as:

$$\Delta T_{\max} = T_C \left( \sqrt{1 + \frac{\mathbf{I} k_B}{2e\mathbf{b}} \left( \frac{e\Phi_C(I, T_C)}{k_B T_C} + 2 \right)^2} I - 1 \right) \quad (2.5)$$

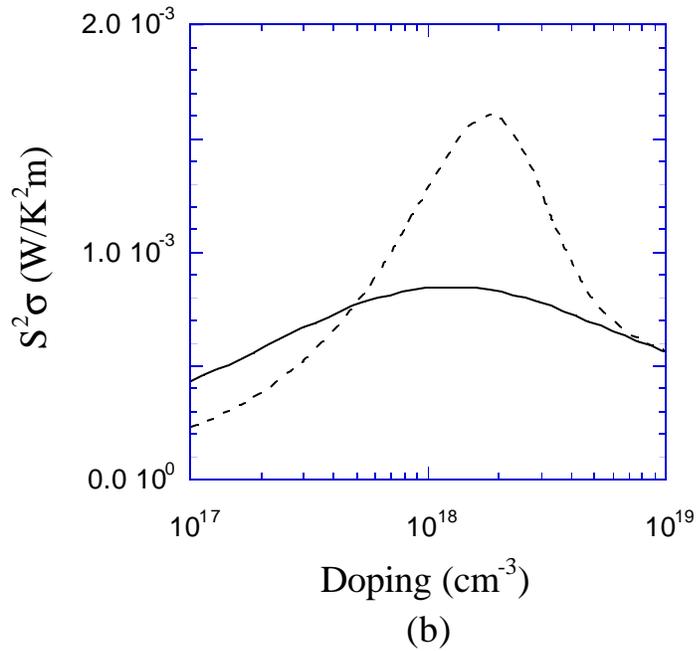
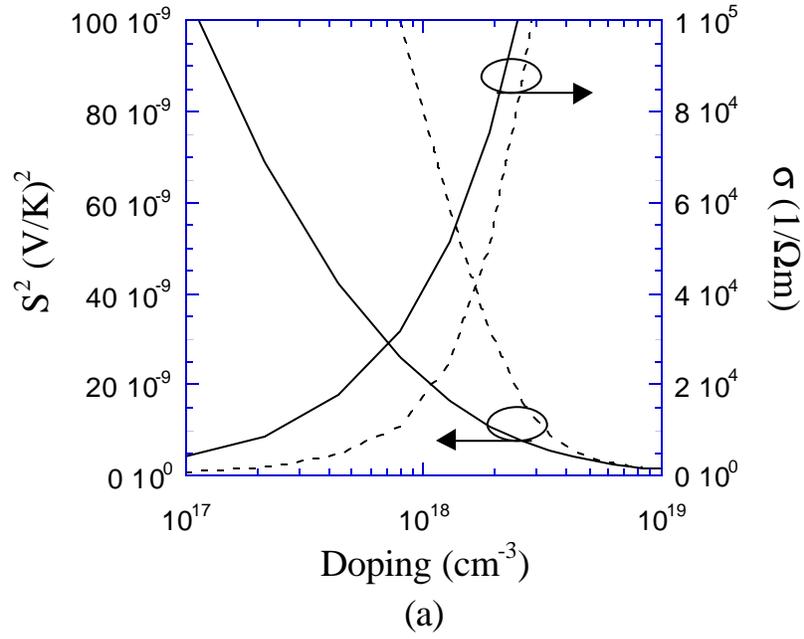
where  $T_c$  is the cold side temperature,  $F_c$  the cathode barrier height,  $I$  the current,  $\mathbf{l}$  the electron mean free path in the barrier, and  $\mathbf{b}$  the thermal conductivity of the barrier layer. By maximizing this equation with respect to current, the material dependence of  $\Delta T_{\max}$  is determined to be only through the ratio  $\mathbf{I}m^*/\mathbf{b}$  or  $\mathbf{m}m^{*1.5}/\mathbf{b}$ , where  $\mathbf{m}$  is the carrier mobility in the barrier region.

$$\Delta T_{\max} \Big|_{I_{\max}} = T_C \left( \sqrt{1 + \frac{8\sqrt{3}pk_B^{3.5}}{\sqrt{2}eh^3} \cdot \frac{\mathbf{m}m^{*1.5}}{\mathbf{b}} \cdot T_C^{2.5}} - 1 \right) \quad (2.6)$$

Interestingly, in this approximation, thermionic emission cooling and thermoelectric cooling have the same material figure of merit (Equation 2.4), and so through

selective emission of hot carriers in heterostructures we can improve the cooling capacity of conventional thermoelectric materials.

To illustrate more fully the beneficial effects of the barrier for thermionic cooling, the square of the Seebeck coefficient, electrical conductivity, and resulting power factor are compared in Figure 2.3 for an InGaAs sample with and without a barrier of 0.1 eV. The curves shown are for the evaluated expressions of Equations 2.1 through 2.3 assuming an effective mass of  $0.041m^*$ , a mobility of  $2500 \text{ cm}^2/\text{Vs}$ , and an ambient temperature of 300K. The energy dependence for effective mass and the carrier-density dependence for mobility were found to have little impact on the result and thus ignored for simplicity (they will be considered later for larger barriers). It was also assumed that all electrons with energy below the barrier are blocked, and that all electrons with energy above the barrier are emitted over the barrier. Following the argument discussed in the last section, the Seebeck coefficient of the bulk sample decreases rapidly for high doping levels due to the symmetry of the DOS above and below the Fermi level. The presence of the barrier provides the needed asymmetry in the differential conductivity at the higher doping levels by filtering the electron transport. Graphically in Figure 2.3a, the square of the Seebeck is increased with the introduction of the barrier. For very high doping, the barrier no longer has an effect on blocking cold electrons and the two curves approach one another. The barrier also negatively impacts the conductivity of the material as a reduction can also be seen in Figure 2.3a. Nevertheless, this reduction is smaller than



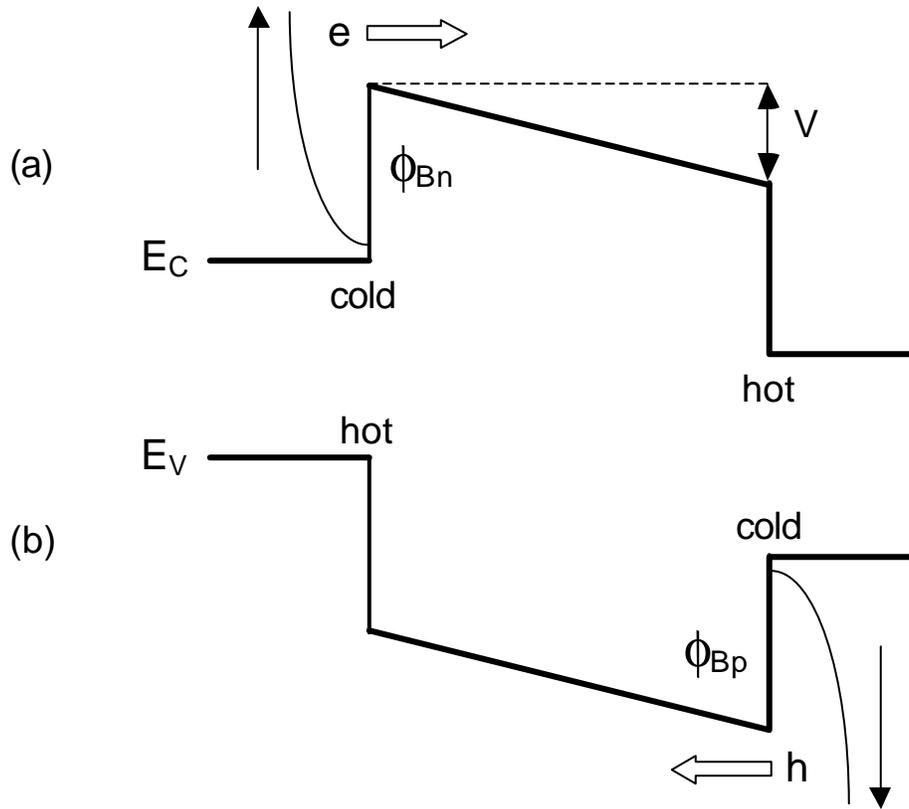
**Figure 2.3** (a) Calculation of Seebeck coefficient squared ( $S^2$ ) and electrical conductivity ( $\sigma$ ) as a function of doping for bulk InGaAs (solid lines) and for InGaAs with an undoped InGaAsP barrier (dashed lines). The impact of the barrier is to increase the Seebeck coefficient with only a slight decrease in electrical conductivity resulting in an improved power factor. (b) The power factor is seen to increase by a factor of two in this example.

the increase in Seebeck coefficient and the overall power factor is approximately doubled as shown in Figure 2.3b.

## 2.2 N-type and P-type Structures

The concept of filtering electrons with barriers in *n*-type material that has been presented so far also applies to the filtering of holes in *p*-type material as illustrated in Figure 2.4. Just as the barrier in the conduction band passes high energy (hot) electrons and blocks low energy (cold) electrons, an analogous barrier in the valence band can pass high energy holes while blocking low energy holes. It is important to note that for the same bias polarity, the *n*-type device cools on the left side and heats on the right whereas the *p*-type device heats on the left and cools on the right. This is fortunate since it lets us imitate the conventional thermoelectric configuration of multi *n*- and *p*-type elements connected electrically in series and thermally in parallel. This arrangement has several advantages over the single element case. It first allows for the removal of the external electrical connection to the cold side of the device and keeps all external connections on the hot side, close to the heat sink. The other main advantage is in reducing the necessary external current bias. A large area thermoelement (length & width  $\gg$  thickness) requires a much larger current than a small area thermoelement (length & width  $\sim$  thickness) to maintain the same temperature difference. By placing many of the small area thermoelements together, it is still possible to cool an area that is the same size as the large area

thermoelement. Correspondingly, as the individual elements are made smaller, the required current is reduced and the external voltage is increased.



**Figure 2.4** (a) Conduction band diagram of a *n*-type and (b) a valence band diagram of a *p*-type thermionic emission cooler under an applied bias  $V$ . For the same bias polarity, the *n*-type device cools on the left and heats on the right, while the *p*-type device heats on the left and cools on the right.

### 2.3 Design of Barriers for Cooling

Now that the microscopic thermoelectric and thermionic cooling mechanisms have been discussed, the question of how to optimally design these structures remains.

This section will be devoted to presenting and discussing the design issues and guidelines for thermionic emission coolers.

### 2.3.1 Band Gap Engineering

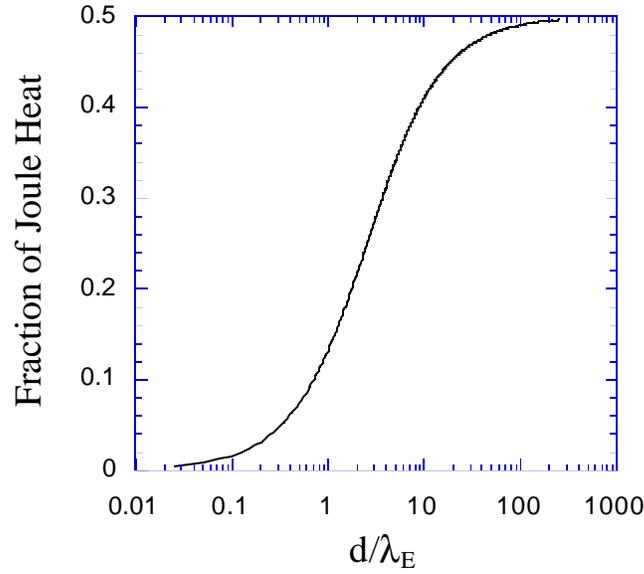
The band gap engineering of the thermionic cooler structures takes into consideration many of the same issues as thermoelectrics. In the most ideal case of designing a solid-state cooling medium, the following three effects must be considered: cooling power; Joule heating; and heat conduction. Taking into account these effects, the overall cooling capacity of a single barrier thermionic cooler with cathode-side barrier height  $\Phi_C$ , barrier thickness  $d$ , cross-sectional area  $A$ , and thermal conductivity  $b$ , can be expressed as [2]:

$$Q_{TI} = \left[ \Phi_C + 2 \frac{k_B T_C}{e} \right] \cdot I - IV \left[ \left( \frac{1}{2} - \frac{l_E}{d} \right) - \frac{l_E^2}{d^2} (e^{-d/l_E} - 1) \right] - \frac{bA}{d} \Delta T \quad (2.7)$$

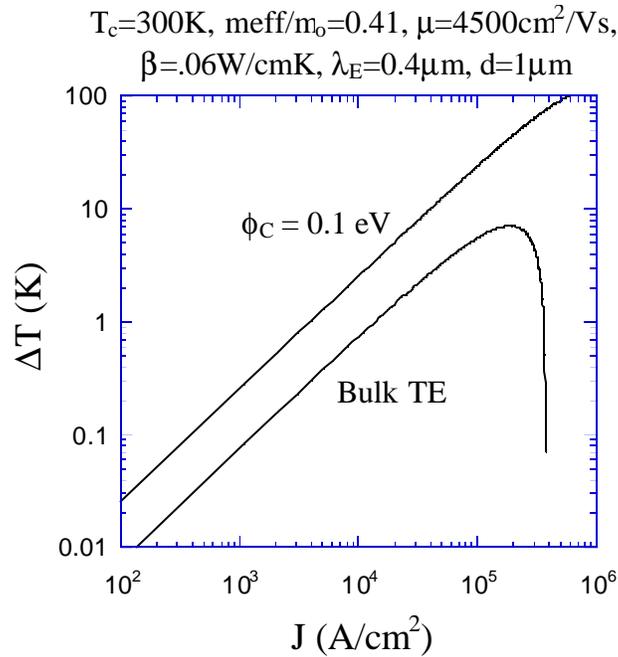
where  $k_B$  is the Boltzmann constant,  $e$  the electron charge (not to be confused with the exponential in the second term),  $l_E$  the energy relaxation length for carriers,  $T_C$  the cold side (cathode) temperature, and  $\Delta T = T_H - T_C$ . The anode barrier height is not considered in the above approximation, and it is simply assumed to be high enough to suppress the reverse current from the hot to cold side. The first term of Equation 2.7 describes the thermionic cooling power which can be explained as the total current times the average energy of the carriers that are emitted over the barrier.

Assuming a Boltzmann distribution for carriers, which is valid for barrier heights  $> 2k_B T$ , this average energy is the barrier height plus twice the thermal energy,  $(F_B + 2k_B T_C/e)$ . While this expression can give a good estimation of the cooling power in some situations, a more rigorous approach is that of Section 2.1 where  $S$  and  $\mathbf{s}$  are calculated explicitly (see Section 2.3.4). The second term of Equation 2.7 describes the Joule heating expressed as the total voltage drop over the barrier times the current, and a coefficient which takes into account the finite electronic energy relaxation length  $l_E$ . In the limit of very thick devices ( $> \text{few } \mu\text{m}$ ), this coefficient reduces to  $1/2$  which is the result for pure diffusive transport where half the heat arrives at the cathode and half at the anode. In the other limit of very short devices, the Joule heating term approaches zero. This is the ballistic transport regime, and all of the electron's energy is deposited at the anode side. Figure 2.5 illustrates this change in the Joule heating at the cathode versus the normalized barrier thickness. While very short devices appear attractive due to the elimination of Joule heating in the barrier, there is a trade off with the increased heat conduction described by the third term of Equation 2.7.

Using various material parameters for InGaAs (see Fig. 2.6), the expression for cooling capacity can be investigated more quantitatively. Assuming no heat load ( $Q=0$ ), the expression for cooling capacity can be solved for the maximum temperature difference as shown in Figure 2.6 for a cathode barrier height of 0.1eV and for no barrier (bulk thermoelectric material). Comparing the two curves at a



**Figure 2.5** Fraction of the Joule heating generated in the barrier that arrives to the cathode versus the barrier thickness ( $d$ ) normalized by the relaxation length for carriers ( $\lambda_E$ ). The anode side of the barrier is assumed to be in contact with an ideal heat sink.



**Figure 2.6** Cooling temperature as a function of current for InGaAs with (0.1 eV) and with out (bulk thermoelectric) a conduction band barrier. The electrical and thermal conductivities were measured experimentally, and the electron relaxation length was taken from previous work [18].

current density of  $10^5$  A/cm<sup>2</sup>, the maximum cooling of the bulk material is 5.5 K while the barrier device is 24 K, more than a factor of four greater. In this approximation, the maximum allowable current is limited by the thermionic emission given by the Richardson thermionic emission expression [22]:

$$J = A^* T^2 \exp\left(\frac{-q\mathbf{f}_C}{k_B T}\right) \cdot \left[ \exp\left(\frac{qV}{k_B T}\right) - 1 \right] \quad (2.8)$$

where  $A^*$  is the effective Richardson constant. For an InGaAs barrier of 0.1eV, the magnitude of the first term outside the brackets is approximately  $7 \times 10^5$  A/cm<sup>2</sup>. In practical applications of such a cooler structure, non-ideal heating effects such as contact resistance usually limits the optimum current density. Here we considered a contact resistance of  $5 \times 10^{-8}$   $\Omega\text{cm}^2$ , the lowest reported experimental value available [23]. The other non-ideal factors that ultimately limit the optimum current bias will be discussed in subsequent chapters.

### 2.3.2 Barrier Thickness

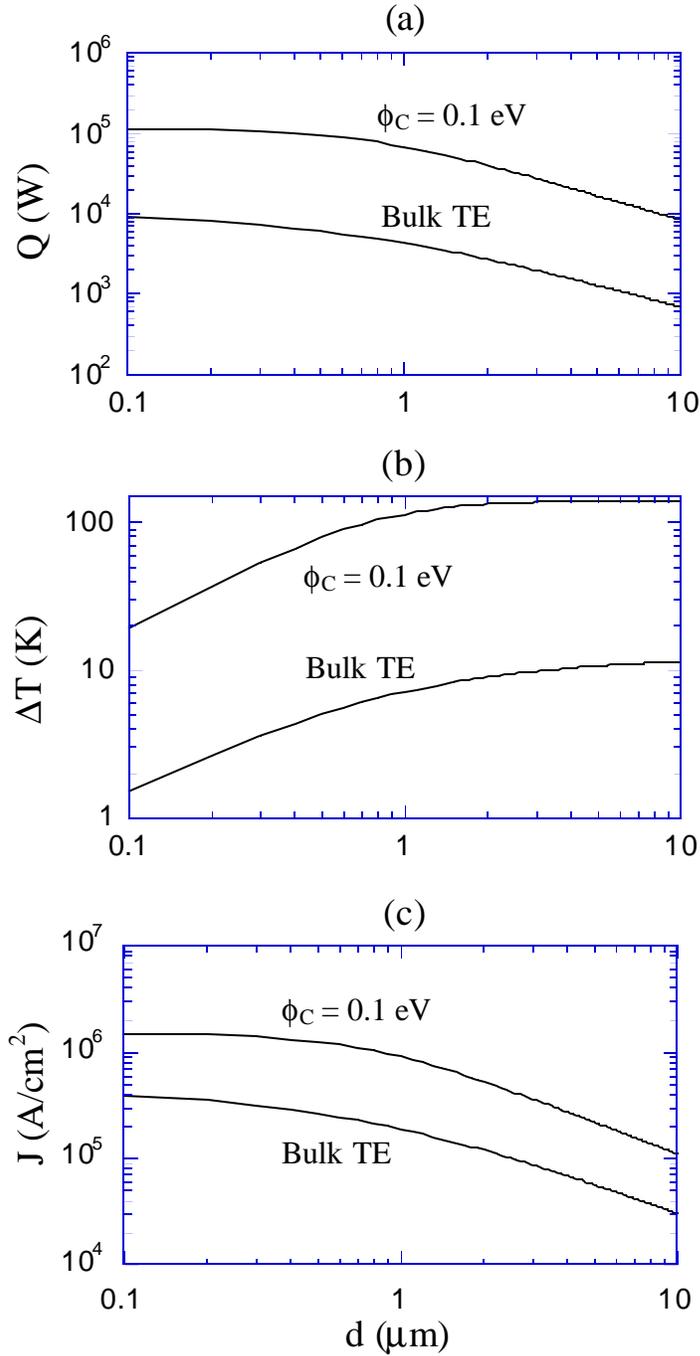
In designing thin film coolers, the thickness of the film plays an important role in the device behavior. In any type of cooler there is the same relation between temperature differential and cooling power, expressed as:

$$\Delta T = R^{th} Q \quad (2.9a)$$

$$R^{th} = \frac{d}{\mathbf{b}_{eff} A} \quad (2.9b)$$

where  $R^{th}$  is the thermal resistance and  $\mathbf{b}_{eff}$  is the effective thermal conductivity. This equation is analogous to the electrical equivalent Ohm's Law, replacing temperature for voltage, heat current for electrical current, and thermal resistance for electrical resistance. The specific application of the cooler must be considered in the design as to what temperature difference and cooling powers are required.

Continuing with the numerical analysis from the last section, the effect of barrier thickness can be examined. Figure 2.7 plots the maximum cooling power, temperature difference, and corresponding optimum current density versus barrier thickness. Below  $1\mu\text{m}$ , the cooling power and current density begin to saturate due to contact Joule-heating effects while the temperature difference decreases owing to the reduced thermal resistance. Above  $1\mu\text{m}$ , the temperature difference becomes independent of thickness, while the cooling power and current density decrease. Herein lies the trade off between cooling power and the required current supply. Basically it takes less current to maintain a certain temperature difference across a thicker device since less compensation is needed to counteract the back flow of heat to the cold side. Still, even with a  $10\mu\text{m}$  thick barrier, the cooling power exceeds  $8000 \text{ W/cm}^2$  while only requiring about  $10 \text{ kA/cm}^2$ . These orders of thickness appear attractive, however severe difficulties arise in practically growing such structures. Looking to Equation 2.9b, an alternative to increasing the thickness of the



**Figure 2.7** (a) Maximum cooling power, (b) maximum cooling, and (c) the corresponding optimum current as a function of barrier thickness for a 0.1 eV barrier and bulk thermoelectric effect. A minimum contact resistance of  $5 \times 10^{-8} \Omega \text{cm}^2$  was used to bound the current to practical values.

barrier is to decrease its thermal conductivity. Using superlattice designs to reduce the thermal conductivity is addressed in the next section.

### 2.3.3 Superlattice period

There are many issues to consider when designing the period of the superlattice. The ultimate goal is to minimize the thermal conductivity while maintaining an acceptable electrical conductivity, all while avoiding any impact on the cooling properties of the barrier. The total thermal conductivity ( $\kappa_T$ ) is the sum of both lattice ( $\kappa_L$ ) and electronic ( $\kappa_e$ ) contributions. Luckily the picture is somewhat simplified since for InP-based material systems with doping levels that we will consider, the electronic contribution can be neglected.

The origin of the contribution of specific factors on the thermal conductivity in superlattices is not completely clear. Detailed theoretical investigations using a Boltzmann transport model [24,25] and other representations [26,27] have been undertaken to explain thermal conductivity in superlattices. Several mechanisms have been considered to explain the thermal transport including scattering of the phonons at the interfaces due to roughness, defects, and dislocations, or phonon wave localization and reflection originating from the impedance mismatch. The resulting reduction in thermal conductivity from interface scattering can be attributed to the reduced phonon mean free path ( $l_{mfp}$ ). From kinetic theory [28] the two quantities can be related:

$$\mathbf{b}_L = \frac{1}{3} C v_{avg} l_{mfp} \quad (2.10)$$

where  $C$  is the heat capacity, and  $v_{avg}$  is the average phonon velocity. However, increasing the scattering at interfaces to decrease thermal conductivity may also have the effect of significantly decreasing the electrical conductivity; an undesirable result. In the InP-based material systems considered here, the superlattices are lattice matched with high quality interfaces so that the interface scattering is minimized. Hence any reduction in  $\mathbf{b}_L$  should come from phonon filtering analogous to the optical distributed-Bragg-reflection, or from other phonon wave localization effects.

With the lack of an accurate theoretical model to calculate  $\mathbf{b}_L$  versus superlattice period, an experimental approach must be taken to optimize these structures. The starting point is to design the period close to the phonon mean free path to take advantage of any wave-nature effects. Permutations about this initial superlattice period can then be investigated in an attempt to minimize  $\mathbf{b}_L$ .

#### 2.3.4 High Barrier Devices

In the previous discussion of thermionic cooling in heterostructures, we looked at the cooling properties for a moderate barrier height of 100 meV using a Boltzman approximation. Larger barrier heights will now be addressed with a more explicit calculation and their merits discussed.

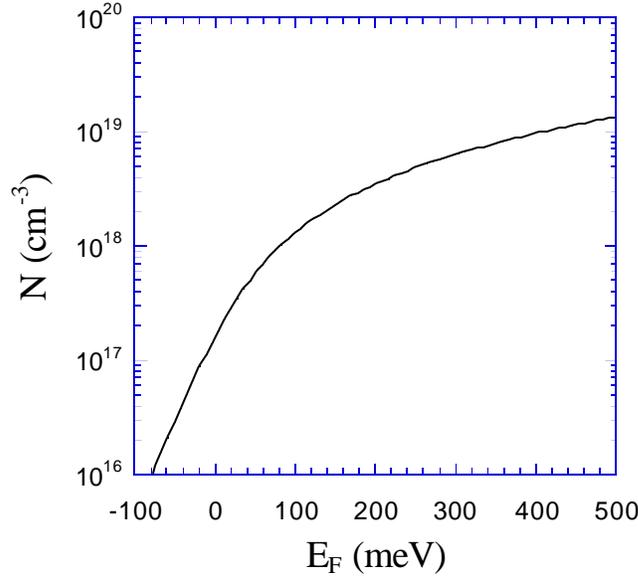
In large barrier thermionic coolers the band offset is made as large as possible and the doping is such that the Fermi level is a few  $k_B T$  below the wide bandgap material. Consequently, the electronic density of states is greatly increased allowing more charge carriers to participate in energy transfer. In this case the requirement for symmetry in density of states can be relaxed (*i.e.* requirement for large electron effective mass), however one should consider additional effects due to scattering at the heterointerfaces. Due to the large surplus of electrons participating in conduction, smaller electric fields are needed to attain considerable cooling when compared with small barrier HIT coolers. This approximately ohmic conduction regime allows the electrical conductivity, Seebeck coefficient, and the  $Z$  parameter to be defined as in bulk material. An order of magnitude improvement in  $ZT$  has been predicted in multi-barrier structures due to the dramatic increase in Seebeck coefficient [3]. This maximum  $ZT$  in multi-barrier structures occurs for high doping densities where as in bulk material it happens at much lower doping densities. These calculations assumed bulk values for thermal conductivity of the multi-layer films, however, the actual thermal conductivity is expected to be lower for superlattices as discussed in Section 2.3.3 resulting in further improvement of  $ZT$ .

To illustrate the enhancement in  $ZT$  for high barrier devices, we compare two different superlattice structures, each with steadily increasing conduction band offsets. In the structures considered below, InGaAs is used as the emitter material.

To determine  $ZT$  versus doping, the relationship between doping ( $N$ ) and Fermi energy ( $E_F$ ) must first be calculated in the emitter region (Fig. 2.8):

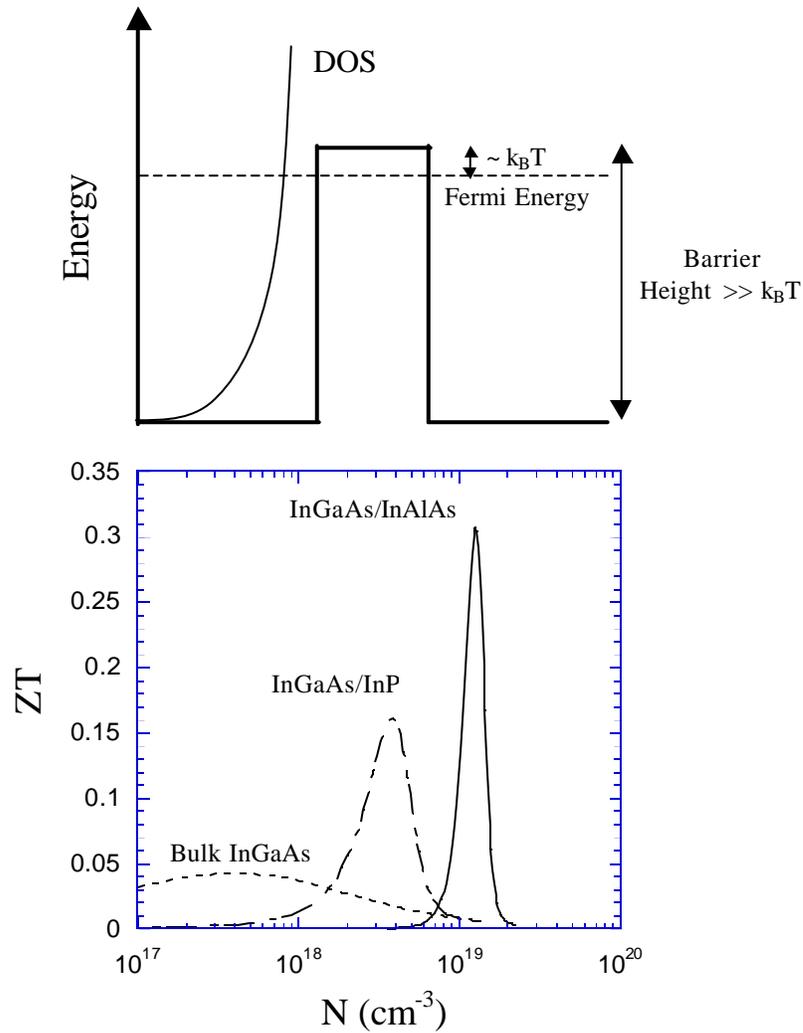
$$N = \int F(E) \cdot D(E) \cdot dE = \frac{1}{2\mathbf{p}^2} \int_{E_C}^{\infty} \frac{1}{e^{E-E_F/k_B T} + 1} \cdot \left( \frac{2m_{eff}}{\hbar^2} \right)^{3/2} \sqrt{E} \cdot dE \quad (2.11)$$

where  $F(E)$  is the Fermi distribution, and  $D(E)$  the electronic density of states ( $DOS$ ). Following the procedure outlined in Section 2.1,  $ZT$  versus doping can be calculated as in Figure 2.9 for bulk InGaAs, InGaAs/InP superlattice ( $\Delta E_C=0.24$  eV), and InGaAs/InAlAs superlattice ( $\Delta E_C=0.51$  eV). The peak in the  $ZT$  characteristics at a given doping level coincide with the Fermi level being approximately  $k_B T$  below the barrier energy. This point is the optimum trade-off between the square of the Seebeck coefficient (cooling) and the electrical conductivity (heating). Even



**Figure 2.8** Calculated doping concentration versus Fermi level for InGaAs emitter region. The zero energy references the conduction band minimum.

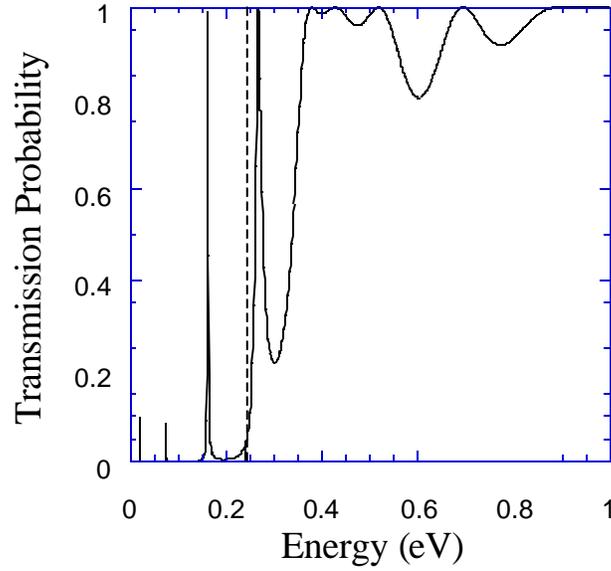
considering the reduction in mobility at the higher dopant concentrations (this was experimentally measured and included in the calculation), the InGaAs/InAlAs superlattice shows close to an order of magnitude improvement in the overall  $ZT$  compared to the bulk InGaAs value. However, the design of these high barrier



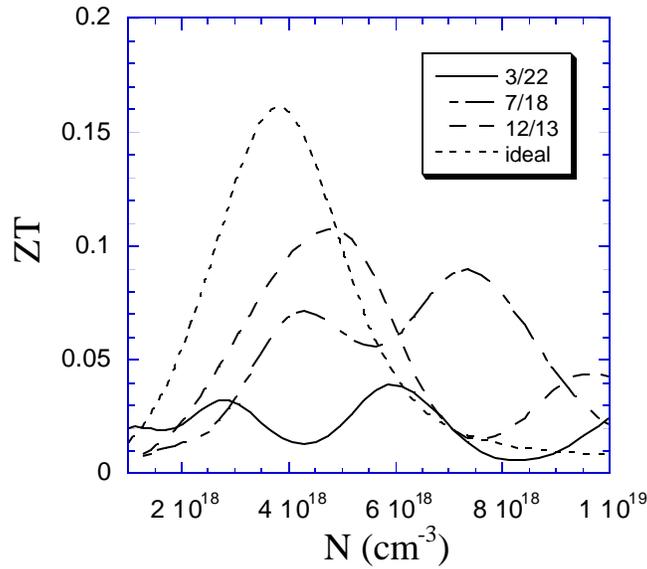
**Figure 2.9** Schematic and calculated  $ZT$  for bulk InGaAs and for high barrier heterostructure thermionic coolers based on InGaAs/InP ( $\Delta E_C=0.24\text{eV}$ ) and InGaAs/InAlAs ( $\Delta E_C=0.51\text{eV}$ ) at various doping densities. The peak in the  $ZT$  characteristic at a given doping corresponds approximately to the Fermi level being  $\sim k_B T$  below the barrier. The thermal conductivity of the composite material is taken to be  $5 \text{ W/mK}$ .

structures is not trivial since as the barrier height increases, the sharpness of the  $ZT$  characteristic increases. This amounts to growing structures with very precise doping, as small deviations can result in large swings in Fermi energy (see Fig. 2.8). Furthermore, high doping effects on material parameters such as effective mass and mobility must be modeled accurately to correctly predict the correct doping.

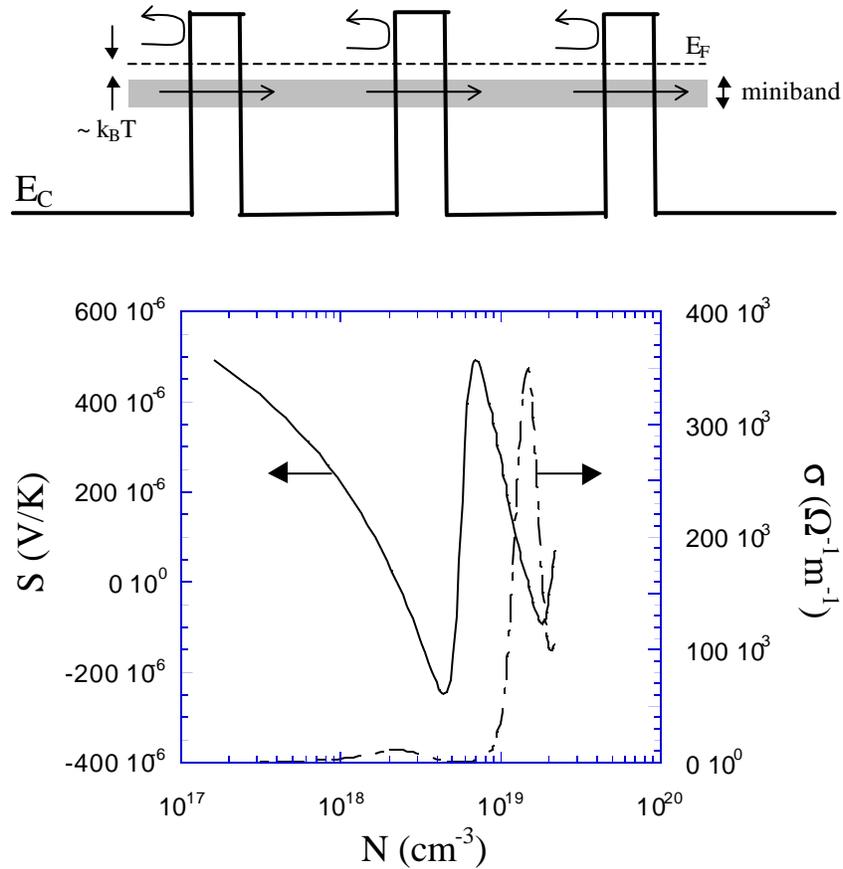
On top of the doping dependence of material parameters, the quantum mechanical transmission probability ( $T(E)$ ) should also now be considered in these high narrow-barrier calculations. For the calculations of  $ZT$  in Figure 2.9,  $T(E)$  was ideally assumed to be zero for electron energies below the barrier, and unity for energies above. Figure 2.10 shows a more realistic picture of  $T(E)$  for an InP/InGaAs (7nm/18nm) superlattice. The propagation matrix method [29] is used for the calculation and only two periods are considered where the electron coherence length is estimated to be roughly 50nm. From Figure 2.10, small minibands can be seen below the barrier energy, and the effective barrier height appears to be shifted to higher energies. By including  $T(E)$  in the equations for Seebeck coefficient and electrical conductivity, its effect can be determined. Figure 2.11 shows the revised calculation of  $ZT$  for InP/InGaAs superlattices with various ratios of the constituent materials for a 25nm period. From this plot, it is obvious that  $T(E)$  plays a major role in the determination of  $ZT$ , and can be detrimental if the superlattice is designed incorrectly. In the case of the 3nm/22nm structure, the overall  $ZT$  never even exceeds that of the bulk InGaAs, and even the 12nm/13nm structure suffers a 30% reduction.



**Figure 2.10** Quantum mechanical transmission probability versus energy for two periods of 7nm/18nm InP/InGaAs superlattice. The dashed line indicates the barrier height of 0.24 eV where the zero on the energy scale corresponds to the minimum conduction band energy in the InGaAs emitter region.



**Figure 2.11** Calculation of ZT for InP/InGaAs superlattices with various ratios of the constituent materials for a 25nm period where the quantum mechanical transmission probability is considered. In the ideal case the period is irrelevant, and the transmission probability is assumed to be zero for energies below the barrier and unity for energies above. Significant decreases can be seen in ZT due to miniband conduction.



**Figure 2.12** Calculated Seebeck coefficient and electrical conductivity for three periods of 3nm/5nm InAlAs/InGaAs. The Seebeck coefficient changes sign for certain doping levels. The simplified diagram above illustrates the concept of manipulating the miniband conduction for electron filtering.

For the 12nm/13nm ratio, a more accurate calculation would consider the 2D *DOS* in the wells.

Interestingly, with careful design of the superlattice transport, the miniband conduction can be tailored to provide cooling behavior of opposite polarity. If the miniband window is made wide enough in energy and the Fermi energy is placed

approximately  $k_B T$  above the miniband, it is possible to selectively block electrons above the Fermi level, and transmit electrons below the Fermi energy. Consequently the heating and cooling would be reversed. The barrier energy must also be far enough away from the miniband to effectively block higher energy electrons from passing over the barrier. Figure 2.12 shows a simplified schematic of the miniband cooler structure and a plot of Seebeck coefficient and electrical conductivity for a sample InGaAs/InAlAs structure. A negative Seebeck coefficient of  $-250 \mu\text{V/K}$  is predicted, however this does not directly translate into a large  $ZT$  since the electrical conductivity is reduced. Further investigation is needed to evaluate whether reasonable amounts of cooling could be accomplished using the miniband concept. Prospective applications of this reverse behavior will be mentioned in later chapters.

In all of the above analysis, quasi diffusive transport of electrons above the barriers is assumed. Further improvements in  $ZT$  may be possible when considering ballistic transport effects.

### 2.3.5 Cooling Efficiency

The efficiency of refrigerators is typically described by the coefficient-of-performance ( $COP$ ) which is a ratio of cooling power to input electrical power (see appendix A). The maximum  $COP$  of a Peltier cooler may be expressed as:

$$COP_{\max} = \frac{T_1}{T_2 - T_1} \cdot \frac{[\sqrt{1 + ZT_M} - T_2/T_1]}{[\sqrt{1 + ZT_M} + 1]} \quad (2.12)$$

where  $T_1$  is the source temperature,  $T_2$  is the sink temperature, and  $T_M$  is the mean temperature [4]. Taking the best  $ZT$  of 0.31 from Figure 2.9, the efficiency of the InGaAs/InAlAs heterostructure thermionic cooler is only about 7% of the ideal thermodynamic  $COP$ . Fortunately in optoelectronic cooling applications, efficiency is not of critical importance, and the devices need only provide the required amount of cooling power. It is possible however to further increase the efficiency of the coolers. The main problem is that the high cooling power at the cathode needs to fight the large heat flux that is coming from the hot junction only a few microns away. The concepts of using thicker films or minimizing thermal conductivity in superlattices from the previous sections would contribute significantly to improving the efficiency. More generally speaking, any increase in  $ZT$  will improve the efficiency.

#### **2.4 Cascading Coolers for Larger $\Delta T$**

Considering that a single thin barrier can provide such a significant amount of cooling, an obvious question to ask is whether cascading coolers is possible to achieve even greater temperature differentials. Theoretically it should be possible to achieve any temperature down to absolute zero, however practical limitations prevent this in reality. One of the problems that arise is in the lower stages having to pump the ever increasing amount of heat that is passed on by the upper stages. This argument explains why conventional multistage thermoelectric coolers are limited in

the number of stages they use. This is also why there are always more thermoelements in the lower stages than the upper stages. A similar concept would need to be applied to a multistage heterostructure thermionic cooler.

Other, more physical challenges lie in the realization of such stacked structures. A continuous growth of several stages of thermionic coolers becomes exceedingly difficult as the number of stages increases. The only alternative is to take separate stages and join them mechanically by fusion or some other bonding technique, but this is also limited in the tolerance of the device to continuing processing steps. It is not known at this time as to the practical limits on the number of stages for cascading thermionic coolers, but conventional TE coolers are rarely ever more than eight stages.

## **2.5 Summary**

In the beginning of this chapter, a clear explanation of the microscopic origin of Peltier cooling was presented. Using this basis, thermionic emission cooling in heterostructures was proposed as a way to improve upon the bulk-material cooling properties. While the concepts that were discussed are applicable to many material systems, the InP-based system was used to illustrate more quantitatively the theory involved. A general set of guidelines for the design of such coolers was presented, and the main considerations discussed. It was shown that large enhancements in the figure of merit,  $ZT$ , can be achieved using thermionic emission in heterostructures,

especially for high barrier devices which showed an order of magnitude improvement with InAlAs heterobarriers. Furthermore, it was shown for the first time that the use of miniband conduction in superlattices makes possible the design of  $n$ -type structures that exhibit  $p$ -type cooling behavior.

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*Chapter 2: Thermionic Emission in Heterostructures*

## Chapter 3

### Heterostructure Design and Growth

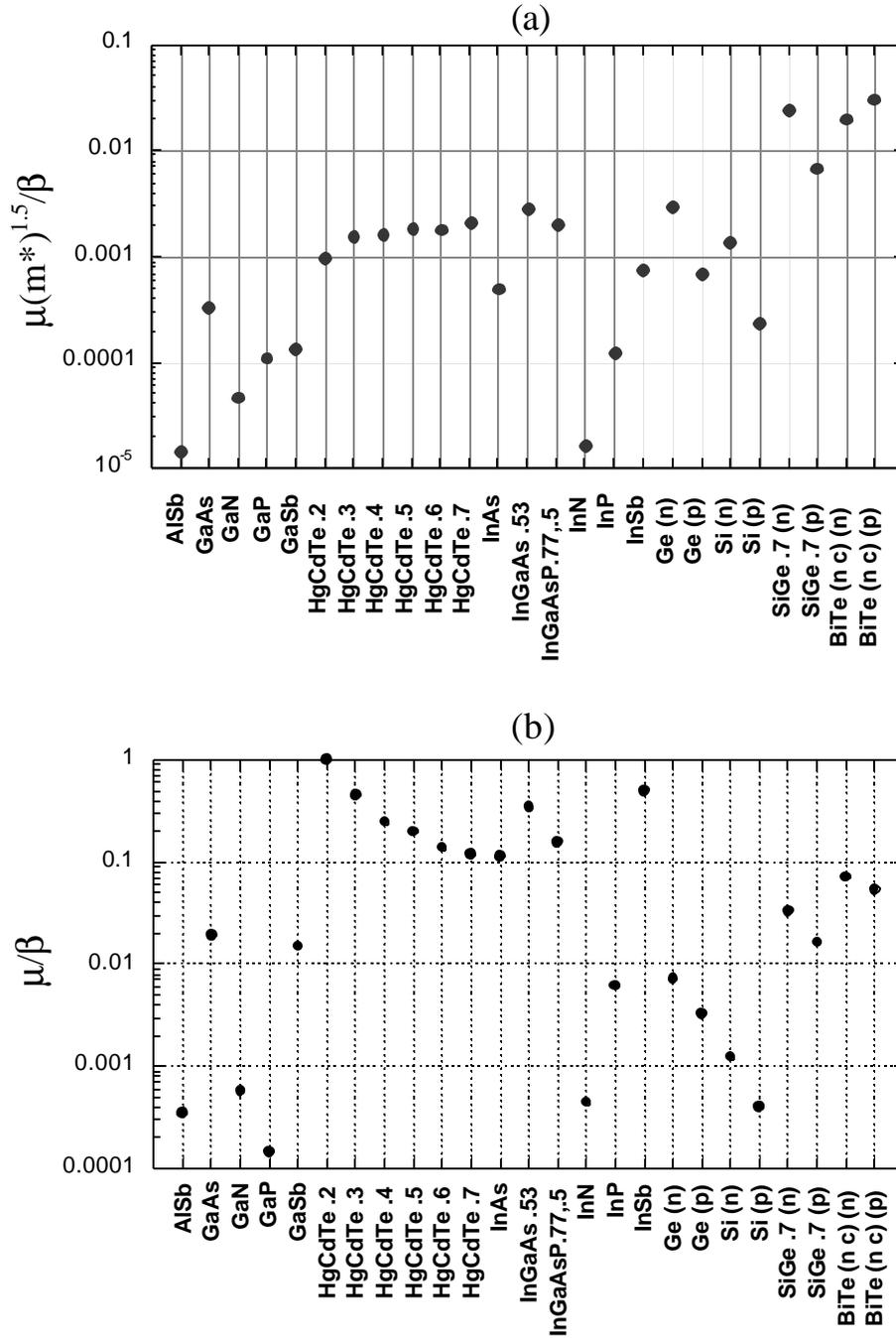
In Chapter 2, it was shown that for certain approximations, thermionics and thermoelectrics have the same material figure-of-merit. As discussed below, the use of high barrier thermionic emission coolers relaxes the need for high effective mass. Considering this, many III-V compounds used in optoelectronic devices actually have very attractive cooling properties. Several proposed structures will be described and investigated in this chapter, all of which were grown lattice matched to InP substrates. The experimentally measured material properties of the grown structures will be discussed more fully in Chapter 4.

#### 3.1 Thermoelectric and Thermionic Material Figure-of-Merit

To review, the material figure-of-merit of thermoelectrics and low-barrier thermionics can be expressed as  $\mu(m^*)^{1.5}/\kappa$ , where  $\mu$  is the mobility,  $m^*$  the effective mass, and  $\kappa$  the thermal conductivity. Figure 3.1a shows this material figure-of-merit for several different semiconductor systems. SiGe is already an important thermoelectric material for high temperatures (>900°C), and is an attractive material for thermionic cooling at room temperature [1,2].  $\text{Bi}_2\text{Te}_3$ , the dominant thermoelectric material at room temperature, is also a good candidate for thermionic cooling, but the crystal growth and processing technology is not as mature as SiGe

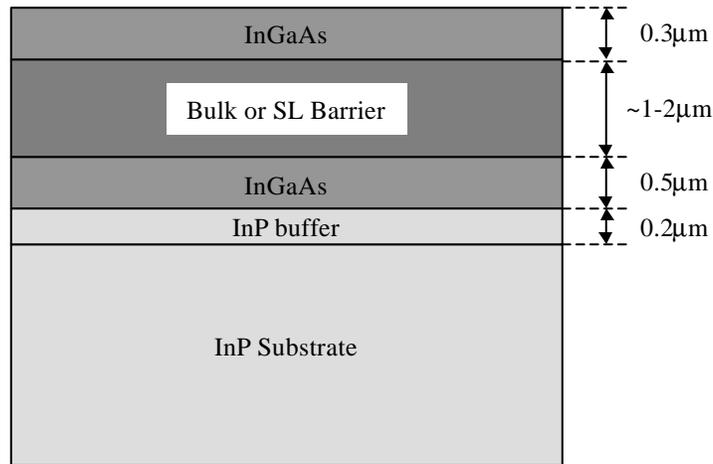
[3]. Other materials such as InGaAs and HgCdTe are well suited for integration with optoelectronic devices and infrared detectors respectively. While these latter two material systems have a material figure-of-merit that is roughly an order of magnitude smaller, a fundamental feature of thermionic cooling in heterostructures is the reduced constraints on material choice. Specifically, thermionic cooling relaxes the requirement for high thermopower since the band edge discontinuities perform the work of creating large asymmetries in the transport energy. This equates to negating the requirement for large effective mass in the material figure-of-merit expression. The need for large effective mass stems from the curvature of the energy versus momentum relation relating the need for large asymmetry in the density-of-states. Therefore, the barrier material should simply have an adequate electrical conductivity and a low thermal conductivity making ternaries and quaternaries good candidates for barrier elements. Figure 3.1b shows the ratio of  $m/b$  with the effective mass term eliminated. Many of the III-V semiconductor compounds now appear to have a larger figure-of-merit than even  $\text{Bi}_2\text{Te}_3$ .

To go step further, the restraint on thermal conductivity could also be alleviated if the hot electrons arriving at the anode could lose their energy by photon emission instead of passing their energy to the lattice as heat. This concept of integrating light emitting structures was previously proposed by Shakouri *et al.* [4]. In this configuration, a high thermally conducting barrier material, such as InP, would be beneficial.



**Figure 3.1 (a)** The material parameter  $m^*m^*)^{1.5}/b$  for different compounds indicates the prospects of various semiconductors for low-barrier thermionic or thermoelectric cooling.  $m$  is the mobility in the barrier layer,  $b$  is the thermal conductivity, and  $m^*$  is the carrier effective mass. **(b)** The modified material parameter neglecting the effective mass.

In the following sections, four different material systems are examined, InGaAs/InGaAsP, InGaAs/InP, InGaAs/InAlAs, and InGaAs/AlGaAsSb. Each of these systems is commonly used in optoelectronic devices and so their use in cooler structures presents a natural process for monolithic integration. InGaAs is used as the cathode (emitter) and anode (collector) regions in each case due to its high mobility, low contact resistance, and the capability of high doping incorporation. The generic structure is described in Figure 3.2, where the barrier region is modified for each new barrier design described below.



**Figure 3.2** A generic cooler structure consists of the bulk or superlattice barrier sandwiched between two InGaAs emitter and collector regions all grown lattice matched to an InP substrate. Typical layer thickness is indicated.

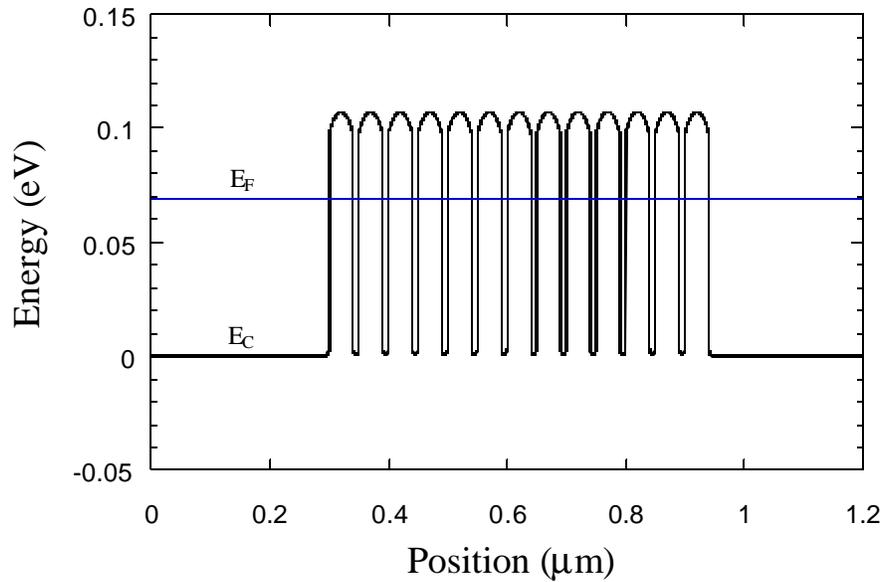
### 3.2 InGaAs/InGaAsP (low-barrier)

The InGaAs/InGaAsP material system was chosen to investigate the cooling properties of low-barrier thermionic coolers. The conduction and valence band

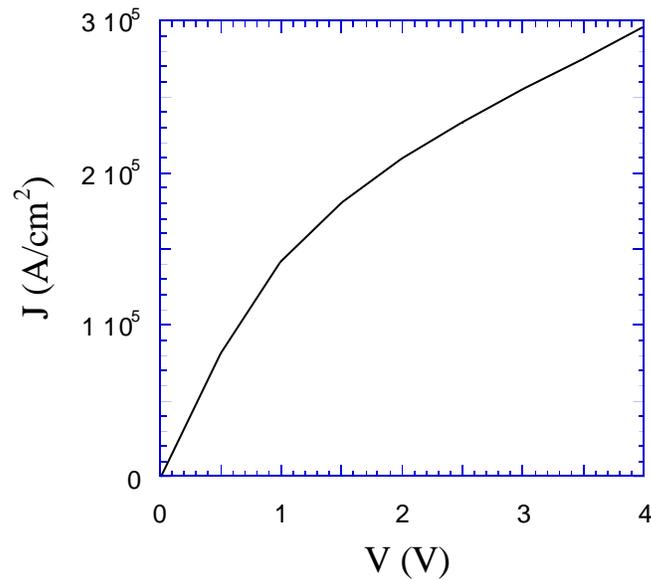
offsets are 110 meV and 102 meV respectively, when lattice matched to InP (InGaAsP  $\lambda_{\text{gap}}=1.3\mu\text{m}$ ) [5,6]. The nearly equal offsets in both the conduction and valence bands allow for suitable barriers in both  $n$ - and  $p$ -type structures. Metal organic chemical vapor deposition (MOCVD) was used to grow bulk and superlattice samples, and all compositions were grown lattice matched to the InP growth substrate. The substrates used for cooling were highly doped to reduce any additional Joule heating in the substrates, while additional growths were done on semi-insulating substrates for material characterization.

While many variations in growth were investigated, the typical  $n$ -type device consisted of a 25 period superlattice of 10nm InGaAs and 30nm InGaAsP, giving a total thickness of  $1\mu\text{m}$ . The doping was chosen so that the Fermi level was optimally located approximately  $k_B T$  below the barrier as discussed in Chapter 2. A one-dimensional semiconductor device simulator [7] was used to calculate the band diagram and Fermi level as shown in Figure 3.3 under equilibrium. A doping of  $3 \times 10^{18} \text{ cm}^{-3}$  was used in the InGaAs regions while the InGaAsP regions were undoped. Figure 3.4 shows the simulated current versus voltage for this structure. The current remains in a linear regime below  $10^5 \text{ A/cm}^2$ .

The  $p$ -type material was grown with a 67 period superlattice of 10nm InGaAs and 5nm InGaAsP, also giving a total thickness of  $1 \mu\text{m}$ . The quaternary is kept shorter in the  $p$ -type structure due to the lower mobility compared to  $n$ -type material. The optimum doping was found to be much higher for the  $p$ -type barrier due to the



**Figure 3.3** Simulated conduction band diagram and Fermi level at equilibrium for a 10nm/40nm InGaAs/InGaAsP ( $\lambda_{\text{gap}}=1.3\mu\text{m}$ ) superlattice barrier with InGaAs emitter and collector regions. The InGaAs regions are doped to  $3\times 10^{18}\text{ cm}^{-3}$  and the InGaAsP regions are undoped. All compositions are lattice matched to InP.



**Figure 3.4** Simulated current-voltage relationship for the structure shown in Figure 3.3. The current is linearly dependent on voltage below  $10^5\text{ A/cm}^2$ .

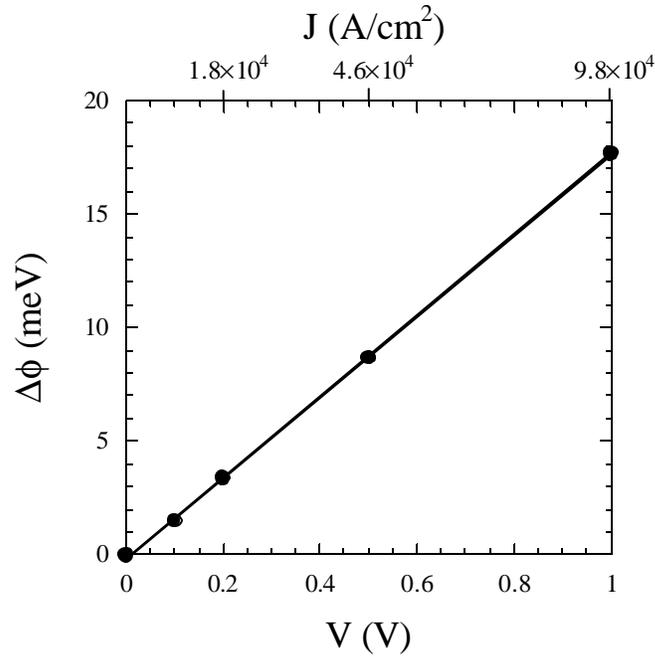
increased density-of-states. A value of  $1 \times 10^{19} \text{ cm}^{-3}$  was used in the InGaAs regions, and a slightly lower value in the InGaAsP barriers.

### 3.3 InGaAs/InP (high-barrier)

The advantages of high-barrier InGaAs/InP structures were previously mentioned in the  $ZT$  calculations of Chapter 2. Due to the larger band offsets in this material system ( $DE_g=0.75\text{eV}$ ), only  $n$ -type materials are considered since the doping levels required for  $p$ -type material ( $>2 \times 10^{19} \text{ cm}^{-3}$ ) are not readily available. The conduction band offset used here and in the previous calculations is 0.242 eV [5]. A variety of structures were grown to study cooling for different superlattices in an attempt to optimize the design parameters. The InP barriers were undoped while doping in the InGaAs regions was varied in an attempt to optimize the Fermi level, and ranged from  $5 \times 10^{17}$  to  $9 \times 10^{18} \text{ cm}^{-3}$ . The InGaAs/InP superlattice period was also modified between 22nm/3nm and 18nm/7nm. Barrier thickness was typically 2  $\mu\text{m}$ , but several superlattices were grown as thick as 6  $\mu\text{m}$ .

As the current bias is increased, the effective difference in energy between the quasi-Fermi level and barrier ( $Df$ ) is diminished [8]. While this effect could be neglected in the low-barrier design, it is more pronounced in the high-barrier superlattice and should be considered when attempting to optimize the Fermi level with respect to the barrier edge. Ideally, the Fermi level is positioned approximately

$k_B T$  below the barrier at the optimum operating bias. Figure 3.5 shows  $Df$  versus bias for an InGaAs/InP superlattice with the InGaAs region doped to  $7 \times 10^{18} \text{ cm}^{-3}$ . The difference in energy between the Fermi level and barrier was 34.5 meV at equilibrium. While the relation for barrier lowering versus voltage in Schottky barriers is proportional to the square root of voltage [8], the condition of a linear conduction regime results in a linear relationship in the semiconductor heterobarriers.



**Figure 3.5** Calculated barrier lowering as a function of voltage bias for an InGaAs/InP superlattice. The linear relationship is due to the linear conduction regime in the heterobarriers.

### 3.4 InGaAs/InAlAs (very high-barrier)

InGaAs/InAlAs superlattice barriers were also examined theoretically in the previous  $ZT$  calculations. While the very high barriers ( $DE_C=0.51\text{eV}$ ) appear promising, the

difficulty in designing and growing the structures presents a significant challenge. From simply a design perspective, the predicted  $ZT$  is highly dependent on a number of different assumed material constants and properties which are used in the calculation of many factors such as transmission probability, density-of-states, and Fermi level. Moreover, the growth of such highly modulation-doped structures requires special techniques, and careful characterization is needed. Deviations about the correct doping profile or layer thickness can have a large impact on the final performance.

Several structures were attempted in this material system. Three micron thick superlattices were composed of 120 periods of 20nm/5nm or 18nm/7nm InGaAs/InAlAs. The wells were doped from  $1.5 \times 10^{19} \text{ cm}^{-3}$  to  $3.0 \times 10^{19} \text{ cm}^{-3}$  while the barriers were non-intentionally-doped (nid).

### **3.5 InGaAs/AlGaAsSb**

The InGaAs/AlGaAsSb material system has been investigated recently for the development of distributed Bragg reflectors (DBR's) for use in long-wavelength vertical-cavity surface-emitting lasers (VCSEL's) [9]. The foremost challenge for the design of such devices is the low thermal conductivity of the Sb-based quaternary material. This low thermal conductivity along with the relatively high Seebeck coefficient make this material system very attractive for the development of thermionic emission coolers and for integration with VCSEL's. Furthermore, the

conduction band offsets can be tailored over a wide range by changing the Al and Sb mole fractions [10].

A 2 $\mu\text{m}$  thick superlattice was grown, composed of 100 periods of 10nm/10nm  $\text{Al}_{0.1}\text{GaAsSb}/\text{Al}_{0.2}\text{GaAsSb}$  sandwiched between InGaAs emitter and collector regions. The superlattice was doped uniformly to  $10^{18} \text{ cm}^{-3}$  while the InGaAs regions were doped to  $5 \times 10^{18} \text{ cm}^{-3}$ .

### 3.6 Summary

After reviewing the material figure-of-merit for thermoelectrics, it was explained that thermionic emission in heterostructures relaxes the need for high thermopower (large  $m^*$ ) in the material structure. With this in mind, it was shown that InP-based material systems are favorable for the design of thermionic coolers due to the high mobilities and low thermal conductivities. Four material systems were proposed for experimental investigation of cooling: InGaAs/InGaAsP; InGaAs/InP; InGaAs/InAlAs; and InGaAs/AlGaAsSb. The material properties of these structures are discussed in Chapter 4.

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*Chapter 3: Heterostructure Design and Growth*

## Chapter 4

### Material Characterization

The material properties of interest should be clear from our previous discussion of  $ZT$  and the material figure-of-merit. Specifically, the electrical conductivity  $\mathbf{s}$ , Seebeck coefficient  $S$ , and thermal conductivity  $\mathbf{b}$  are of utmost concern. In many cases conventional measurement techniques, as in Hall measurements for carrier mobility, can be used to extract properties of interest. In other instances, new methods must be developed to measure parameters such as the Seebeck coefficient perpendicular to superlattice structures. For each of the material properties of interest discussed below, the measurement methods are explained and the results reviewed.

#### 4.1 Electrical Conductivity

The importance of large electrical conductivity follows from minimizing Joule heat. However, the trade-off between  $\mathbf{s}$  and  $S$  was shown explicitly in Chapter 2 when trying to maximize the power factor  $S^2\mathbf{s}$ . On that account, when qualifying a new thermionic cooler structure, the electrical conductivity must be resolved. The measurements described below are for in-plane transport. Cross-plane measurements of conductivity and mobility are difficult to extract due to the small

dimensions and variable effects of current spreading, though methods have been proposed based on a transmission line model [1].

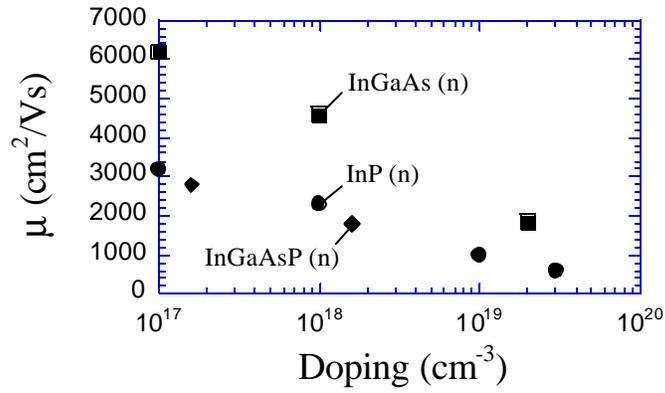
The electrical conductivity can simply be measured through a resistivity measurement ( $\mathbf{s}=1/\mathbf{r}$ ), however more insight is preferred into its contributions. The electrical conductivity can be expressed as:

$$\mathbf{S} = qn\mathbf{m} \quad (4.1)$$

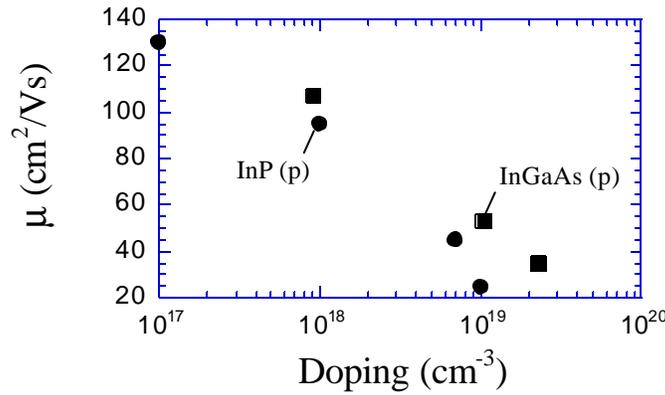
where  $q$  is the electron charge,  $n$  the carrier concentration, and  $\mathbf{m}$  the carrier mobility. The carrier concentration and charge type ( $n$ -type or  $p$ -type) can be determined from a Hall measurement [2]. Knowing the conductivity and carrier concentration, the mobility can then be deduced. The mobility for a given doping concentration gives a measure of material quality and the quality of superlattice interfaces where carrier scattering may occur.

#### 4.1.1 Experimental Results

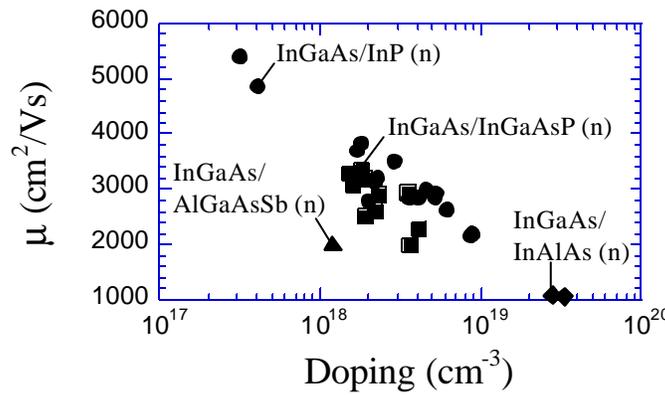
Figure 4.1 shows experimentally measured values for bulk  $n$ - and  $p$ -type materials, as well as various  $n$ -type superlattice systems. The most obvious distinction is between the  $n$ - and  $p$ -type mobility. This is largely due to the order of magnitude difference in effective mass for holes and electrons since mobility is inversely proportional to effective mass. For example, the electron effective mass in InGaAs is  $0.041m_o$  while the hole effective mass is  $0.46m_o$ . Fortunately, the low mobility, and consequently low conductivity, can be offset with higher doping and



(a)



(b)



(c)

**Figure 4.1** Mobility versus doping for various (a) *n*-type materials, (b) *p*-type materials, and (c) *n*-type superlattice systems. The InP values are referenced experimental values from INSPEC [3]. All other values were experimentally measured by the Hall effect.

the inherently larger Seebeck coefficient. For the superlattice systems, most of the structures are modulation doped and the barrier regions are kept thin so the in-plane transport is dominated by conduction in the InGaAs well regions. This explains the close spacing of data points for all the superlattice structures. The overall electrical conductivity is on the order of  $1500 \Omega^{-1}\text{cm}^{-1}$  for *n*-type structures and  $100 \Omega^{-1}\text{cm}^{-1}$  for *p*-type structures. These values are typically less than the corresponding contact resistance in fabricated devices, and so are not limiting cooling performance.

## 4.2 Thermal Conductivity

Thermal conductivity is perhaps even more important than the electrical conductivity as no other variation has a more direct impact on cooling. While other sources of electrical resistance dominate over the material conductivity, the thermal conductivity is considered a limiting factor in current device results. To this end, the superlattice design continually seeks to minimize **b**. Several encouraging reports have been made regarding reduced thermal conductivity with superlattices compared to bulk values in III-V systems [4-7]. Generally, they indicate that short periods produce the lowest thermal conductivity (< 50nm).

### 4.2.1 Experimental Results

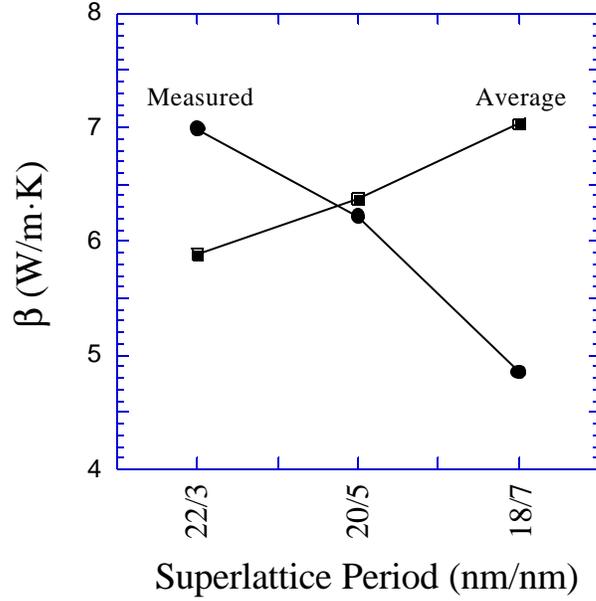
Thermal conductivity perpendicular to the superlattice is of special interest for heterostructure thermionic cooling since the majority of electrical and thermal

transport occur in this direction. Currently, the most common way to measure the cross-plane thermal conductivity is by the  $3\omega$  method [8]. In this technique, an AC current with frequency  $\omega$  is applied to a narrow metal line on the surface of the sample. From Ohm's Law ( $P = I^2 R$ ), heat of frequency  $2\omega$  is generated on the sample. For small temperature changes, the resistance of the metal is linearly proportional to the temperature, and the electrical resistance also oscillates at  $2\omega$ . Multiplying this by the applied current at  $\omega$  produces a voltage signal at  $3\omega$ . This resulting voltage then gives the thermal response of the sample.

**Table 4.1**  $3\omega$ -measured thermal conductivity compared to calculated and experimental values for several InP-based materials. All compositions are lattice matched to InP. Units are in W/mK.

<i>Material</i>	<i>Calculated <math>b</math></i>	<i>Referenced <math>b</math></i>	<i>Measured <math>b</math></i>
InP	68	64 – 84	57 – 71
InGaAs	4.8	4.8	5.2 – 5.4
InAlAs	–	4.5	–
InGaAsP ( $\lambda=1.3\mu\text{m}$ )	4.4	3.8 – 4.9	–

Table 4.1 compares thermal conductivity measured by the  $3\omega$  technique to reported calculated and experimental values [3,9] for InP, and InP lattice-matched InGaAs, InAlAs, and InGaAsP. The good agreement between columns confirms the validity of the measurement for use on more complex superlattice structures. Figure 4.2 plots measurement results for InGaAs/InP superlattices with various ratios and



**Figure 4.2** Thermal conductivity versus the ratio of InGaAs/InP for a constant superlattice period. The circles are experimentally measured values while the squares were calculated geometrical averages from experimental bulk values of the constituent materials. Opposite trends are observed even though the same number of interfaces are present. Experimental values from S. Huxtable.

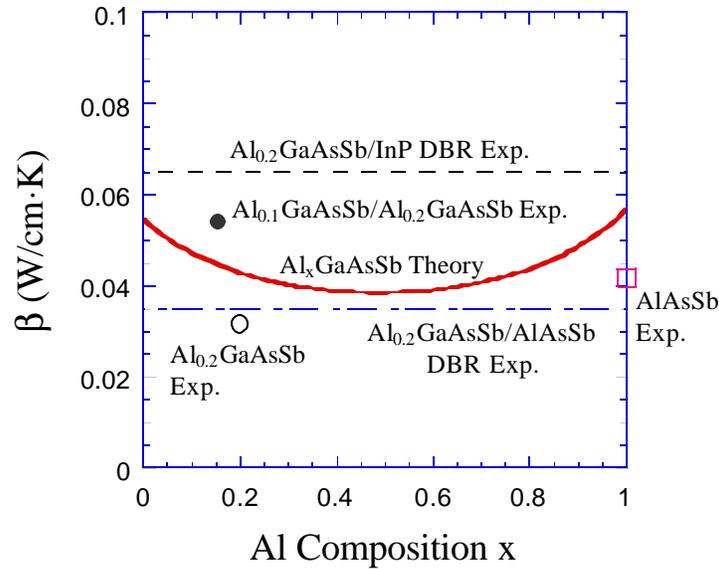
constant period [10]. Looking simply at the bulk values of  $\mathbf{b}$ , as the amount of InP is increased, the effective thermal conductivity ( $\mathbf{b}_{eff}$ ) is expected to increase as:

$$\frac{d_{InGaAs} + d_{InP}}{\mathbf{b}_{eff}} = \frac{d_{InGaAs}}{\mathbf{b}_{InGaAs}} + \frac{d_{InP}}{\mathbf{b}_{InP}} \quad (4.2)$$

where  $d$  is the thickness of the corresponding material for a single period. This average  $\mathbf{b}$  is based on Fourier's law of heat conduction, and does not take into account effects such as interface scattering or phonon filtering. These other effects are shown to be important however, as the measured values show  $\mathbf{b}_{eff}$  decreasing for increasing InP, even though InP has an order of magnitude greater  $\mathbf{b}$  than InGaAs.

Since the same number of interfaces are present in all cases, the result cannot be explained by discrete-interface phonon-scattering effects, and must be due to some other phonon transport physics.

Figure 4.3 summarizes the theoretical and experimental results for the  $\text{Al}_x\text{GaAsSb}$  system where all compositions are lattice matched to InP. The thermal conductivity for the distributed Bragg reflectors (DBR's) is quite low, suggesting that the DBR's themselves are potentially attractive materials for thermionic cooling. The superlattice structure investigated for thermionic cooling is shown as a solid dot in Figure 4.3, and was composed of 10nm/10nm  $\text{Al}_{0.1}\text{GaAsSb}/\text{Al}_{0.2}\text{GaAsSb}$ .



**Figure 4.3** Measured and theoretical thermal conductivity for various  $\text{AlGaAsSb}$  compounds and Al compositions. The superlattice structure investigated for thermionic cooling was 10nm/10nm  $\text{Al}_{0.1}\text{GaAsSb}/\text{Al}_{0.2}\text{GaAsSb}$ . DBR values from G. Almuneau.

Overall, more than an order of magnitude difference in  $\mathbf{b}$  between the InP-substrate and other epitaxial films is evident. This bodes well for thermionic coolers on InP substrates since the substrate needs to provide as ideal a heat sink as possible for the thin film cooler.

### 4.3 Seebeck Coefficient

When considering superlattices, a distinction must be made between the in-plane and cross-plane Seebeck coefficient. While enhancements can be seen in the in-plane direction for lower-dimensional structures, the cross-plane properties are of more interest for heterostructure thermionic cooling. Still, the in-plane measurement is important for characterizing the bulk thermoelectric effect between the metal and contact layers which is in addition to any thermionic emission cooling.

#### 4.3.1 In-Plane

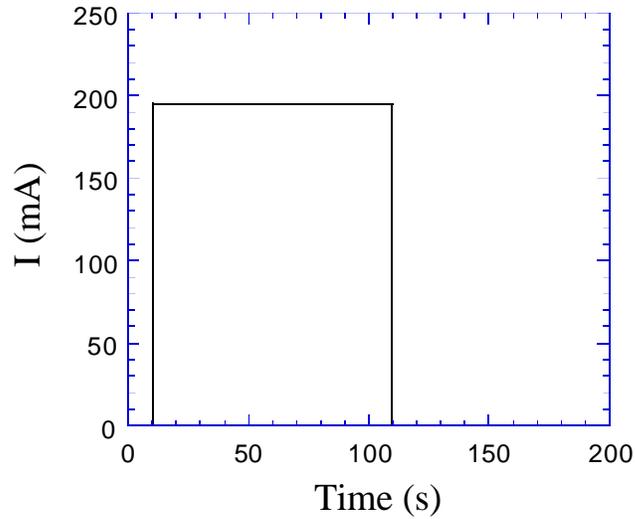
The in-plane and bulk Seebeck coefficient can both be measured in a similar manner. By applying a temperature gradient across a sample and measuring the generated voltage, the ratio of *voltage/temperature* determines the Seebeck coefficient. *N*- and *p*-type substrates were measured, and Seebeck coefficients of 70 and 520  $\mu\text{V/K}$  were measured, respectively. The substrates were both doped to  $5 \times 10^{18} \text{ cm}^{-3}$ , the same as all growth substrates for cooler samples.

### 4.3.2 Cross-Plane

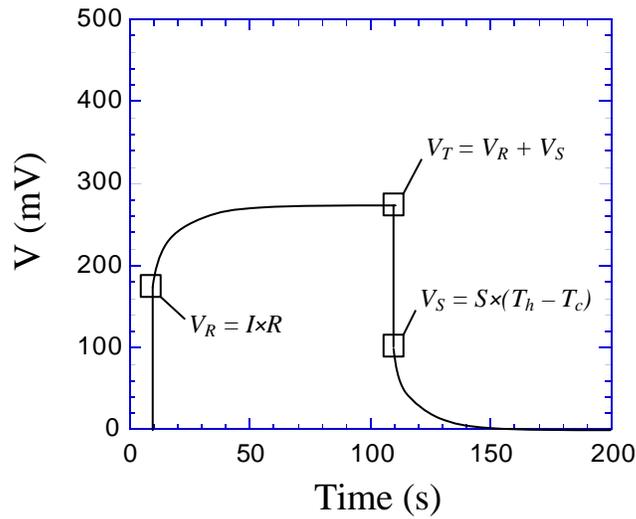
A direct measurement of the cross-plane Seebeck coefficient is difficult at best. Simply applying the same procedure as the in-plane case is not practical because of the dimensions and geometry of the problem. Whereas before temperature and voltage were measured across hundreds of microns, the same parameters need to be measured across thin films on the order of a few microns. In addition, the bottom of the film is not directly accessible, so temperature and voltage need to be inferred from points on the surface. Clearly an alternate measurement method is needed.

The Harman method [11] and further refined transient method [12] have been previously used to not only characterize the Seebeck coefficient, but also the overall  $ZT$  in bulk thermoelectrics. These approaches are based on the inherent differences in time response between the expected voltage from Ohm's law ( $V_R$ ), and the additional Seebeck voltage ( $V_S$ ). Figure 4.4 shows how these two components can be resolved from the total device voltage  $V_T$ , when a square current waveform is applied to a commercial Peltier module with 62 thermoelements. Between the 60 second and 110 second time mark, the voltage has reached a steady state value. Looking closely at the voltage at the 110 second mark, there is a nearly instantaneous ohmic voltage drop due to the current turn-off. The remaining voltage is due to the Seebeck effect which dies out exponentially due to the gradual temperature transient. In this example, the measured Seebeck voltage was 100 mV and the temperature differential was 7.88 K, giving a total Seebeck coefficient of 12.69 mV/K. This value can then

be divided by the total number of thermoelements in the module, resulting in a material Seebeck coefficient of  $205 \mu\text{V/K}$ , which is in good agreement with the manufacturer specifications.



(a)



(b)

**Figure 4.4** (a) Applied current pulse and (b) resulting voltage waveform in the transient Seebeck measurement of a Peltier module. The total voltage  $V_T$  is comprised of an instantaneous component  $V_R$  according to Ohm's law, and an exponential component  $V_S$  from the Seebeck voltage.

The application of this technique to single thermoelements is more difficult however. The reason lies with the noise of the measured voltage signal. In the analysis of the Peltier module, the Seebeck voltage of each element adds to produce the measured voltage. For single elements, voltages on the order of micro-volts must be resolved compared to milli-volts in the case of multi-element modules. Attempts made with noise filters and low-noise amplifiers to extract the signal from single element coolers have met little success.

Since measuring the cross-plane Seebeck coefficient has proven so difficult, an alternative method was necessary to characterize the cooling potential. The cooling potential for thermionic emission coolers is most associated with the barrier used to filter charge carriers. The characterization of the barriers is discussed in the next section.

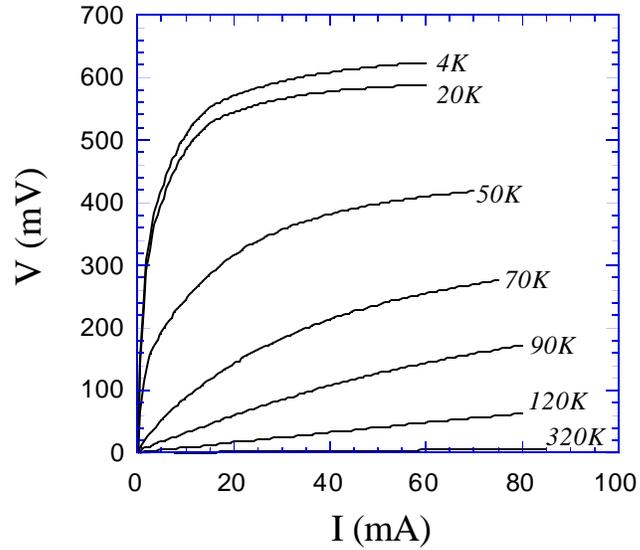
#### **4.4 Barrier Characterization**

The entity responsible for modifying the cross-plane Seebeck coefficient is the barrier used to create the necessary asymmetry in the charge carrier transport. Characterizing the barrier can provide a way to compare various sample structures when changing design variables such as doping, period, and materials. A combination of low temperature current-voltage measurements and secondary ion mass spectroscopy are used to determine the presence of barriers and estimate their magnitudes.

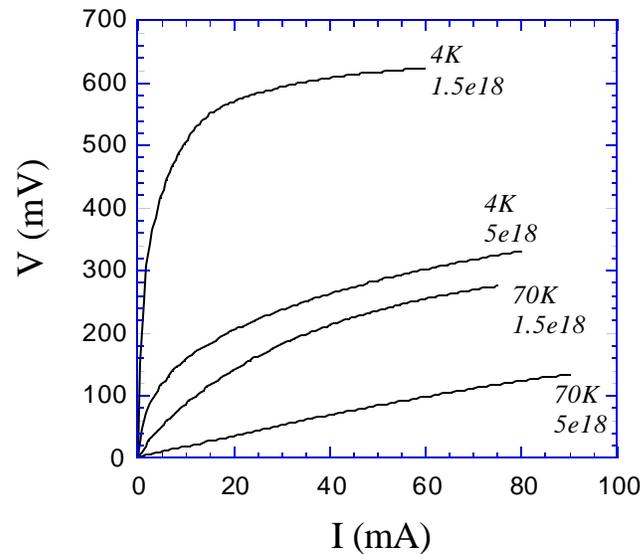
#### 4.4.1 Low Temperature I-V Characteristics

Using a liquid-helium cooled cryostat, current-voltage curves were measured for a variety of superlattice designs. Figure 4.5 shows typical characteristics for a 10nm/30nm InGaAs/InGaAsP ( $1.5 \times 10^{18} \text{ cm}^{-3} / \text{nid}$ ) superlattice with a device area of  $100 \times 100 \mu\text{m}^2$ . From room temperature to around 100 K, the I-V curves appear linear. As the temperature is further reduced, the Fermi distribution narrows and less carriers occupy the available states with energy greater than the barrier. Therefore, at lower temperatures, the I-V curves become Schottky-like indicating that a barrier is indeed present. Sample structures of metal contacts to InGaAs showed linear I-V characteristics over the entire temperature range confirming that the Schottky effects are not due to the metal-semiconductor junction. Figure 4.5b demonstrates how the non-linearities change with increased doping in the InGaAs well regions. More quantitative analysis of the I-V data is needed before an accurate correlation to barrier height and Fermi level is possible.

Not all samples showed the observed behavior described above. In fact, the majority of the InGaAs/InP and all the InGaAs/InAlAs samples showed completely linear characteristics over the entire temperature range. The only explanation is that the barrier is not present. This would suggest that the desired doping profile through the structure is not as it should be.



(a)



(b)

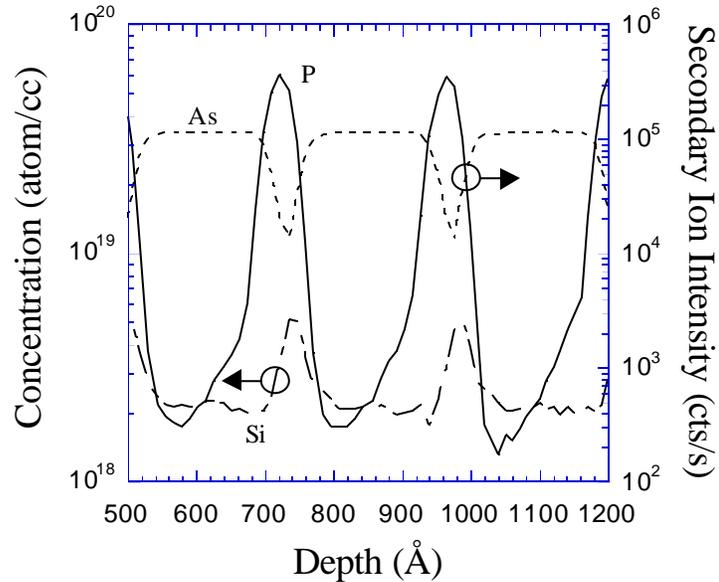
**Figure 4.5** (a) Current-voltage characteristics versus temperature for a 10nm/30nm InGaAs/InGaAsP ( $1.5 \times 10^{18} \text{ cm}^{-3}/\text{nid}$ ) superlattice. (b) Comparing the same structure for different doping levels. The device area was  $100 \times 100 \mu\text{m}^2$ . Measurement by D. Vashaee.

#### 4.4.2 SIMS Analysis

To further investigate the samples that did not indicate the presence of a barrier in the low temperature I-V measurement, secondary ion mass spectrometry (SIMS) was employed to analyze the atomic concentrations of the individual elements in the MOCVD grown material. A sample SIMS result is shown in Figure 4.6 for a silicon-doped 20nm/5nm InGaAs/InP superlattice. The superlattice structure can easily be identified from the arsenic and phosphorus profiles. The feature of interest is the silicon dopant profile that shows significant amounts and even peaks of silicon in the barrier regions. Doping in the InP tends to drastically reduce the barrier, which explains why the I-V curves were linear over all temperatures.

Incorporation of silicon doping in the barrier regions was believed to have happened in one of two ways. Either a substantial amount of residual silicon was present in the chamber after the shutter closed, during the InP growth, or the silicon simply diffused during the growth. To solve the problem, a series of three test structures were grown and analyzed again by SIMS. In the first two structures, a stop-growth was performed between the InGaAs and InP layers for one second and ten seconds. The purpose of the stop-growth was to allow sufficient time for any remaining silicon to evacuate the chamber. In the third test structure, the first and last 30 Å of each InGaAs layer was left undoped. While the same problem remained for the one second stop-growth test structure, proper silicon doping profiles were found in the other two. For reasons of material quality at the heterointerfaces, such

as impurity accumulation, the 30 Å undoped InGaAs regions were favored over the stop-growth solution.



**Figure 4.6** SIMS material analysis of a silicon-doped 20nm/5nm InGaAs/InP superlattice, monitoring As, P, and Si. The InP layers (P peaks) should be undoped, however a significant amount of Si is found to be present.

#### 4.5 Summary

In this chapter the important material properties for heterostructure thermionic cooling were reviewed, and the measurements of those properties discussed. Analysis of carrier mobility, electrical and thermal conductivity, in-plane and cross-plane Seebeck coefficient, and barrier characterization was presented. While many of the properties have established measurement techniques, the latter two are not

well developed for highly-doped thin-film structures. Characterizing the cross-plane Seebeck coefficient remains one of the most challenging problems.

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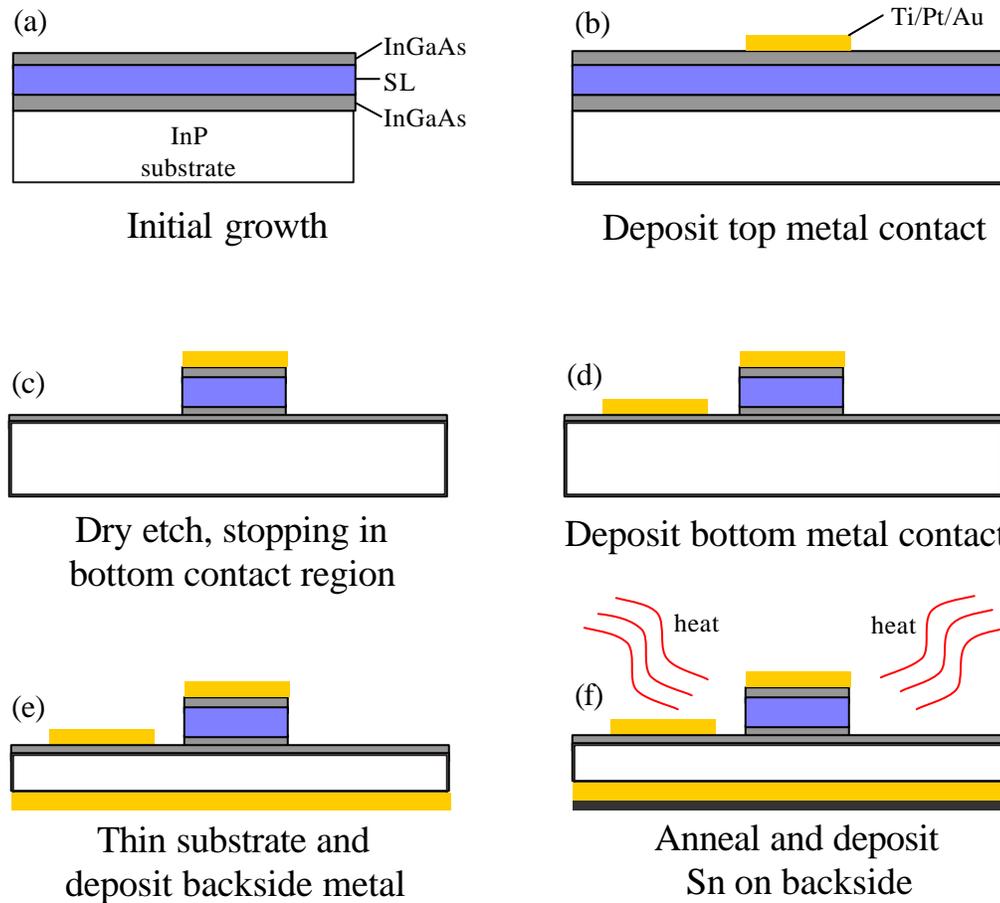
## **Chapter 5**

### **Device Fabrication and Packaging**

Basic processing of thin film coolers is kept as simple as possible to facilitate integration with optoelectronic devices, however formidable challenges remain in the optimization of these devices. The foremost concern is with the thermal design, and ensuring proper heat flow through the structure. This is especially true of the packaging where Joule heating and heat conduction in the electrical connections must be minimized, as well as all thermal resistances between the hot side of the cooler and heat sink. Furthermore, contact resistance must be minimized to values below  $10^{-7} \Omega\text{cm}^2$ , a difficult task indeed. To begin this chapter, the generic processing procedure for the coolers is outlined. Three generations of packaging are then discussed, and the improvements in each described. Contact resistance measurements are presented and optimum metals and annealing conditions are given. Finally, substrate transfer is proposed as a means to improve upon the InP heat sink.

#### **5.1 General Processing Flow**

The general processing steps for fabrication of heterostructure thermionic coolers are shown in Figure 5.1. After the initial growth and sample cleaning, square areas of various size are patterned by photolithography. Oxygen plasma is used to clean the surface by removing any residual photoresist, and the surface is prepped for the top



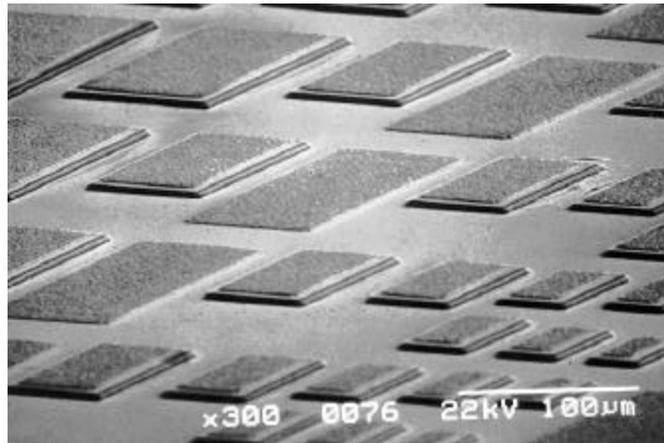
**Figure 5.1** (a) - (f) General processing procedure for heterostructure thermionic coolers. The basic steps involve forming mesas of various size and providing low resistance contacts.

metal contact. This entails a 5 second dip in buffered HF, 5 second rinse in  $\text{H}_2\text{O}$ , 5 second dip in  $1\text{H}_2\text{O}:1\text{HCl}$ , and a final rinse in  $\text{H}_2\text{O}$  followed by a blow dry with  $\text{N}_2$ . The purpose of the HF is to remove the native oxide on the InGaAs surface, while the  $\text{H}_2\text{O}:\text{HCl}$  etches a small amount of InGaAs so that the metal can contact a fresh surface. After the surface prep, the sample is quickly loaded into the e-beam evaporator to minimize new formation of a surface oxide. Metal contacts are then

deposited after the pressure has reached at least  $10^{-6}$  Torr (metals used for contacts will be specified later in Section 5.3). Acetone liftoff is used to remove the photoresist and unwanted metal. This first metallization is perhaps the most critical step as any oversights can seriously impact the contact resistance and degrade the cooler performance. The same mask is then used again to pattern photoresist to protect the metal during the next etch step. After hardening the resist at  $120\text{ }^{\circ}\text{C}$  for 5 minutes, the samples are loaded into the RIE and pumped down to a base pressure of  $2\times 10^{-6}$  Torr.  $\text{Cl}_2$  is used to etch approximately  $0.1\text{ }\mu\text{m}/\text{min}$ , until the lower InGaAs collector region is reached. For the RIE conditions used, the baked photoresist is etched at approximately the same rate as the material. For most coolers with a 1-2  $\mu\text{m}$  superlattice, a single photoresist mask is sufficient. A metal contact is again deposited following the same procedure described above.

The next series of processing steps, with the exception of annealing, are to prepare the sample for packaging and wire bonding. The substrate is mechanically lapped to a thickness of approximately  $100\text{ }\mu\text{m}$ . While the goal of this step is to thin the substrate as much as possible to reduce the thermal impedance seen by the cooler, lapping below  $100\text{ }\mu\text{m}$  creates difficulties in handling the sample during the remaining processing steps. A backside metal layer is deposited and the samples are annealed. Finally, a solder layer is thermally evaporated on the backside for later packaging. Additional processing steps to this basic procedure for specific applications are described as appropriate in the following chapters.

The top surface of a processed sample is shown in Figure 5.2. For a device area of  $100 \times 100 \mu\text{m}^2$ , leaving  $25 \mu\text{m}$  between devices, a two inch wafer can produce nearly 130,000 coolers.



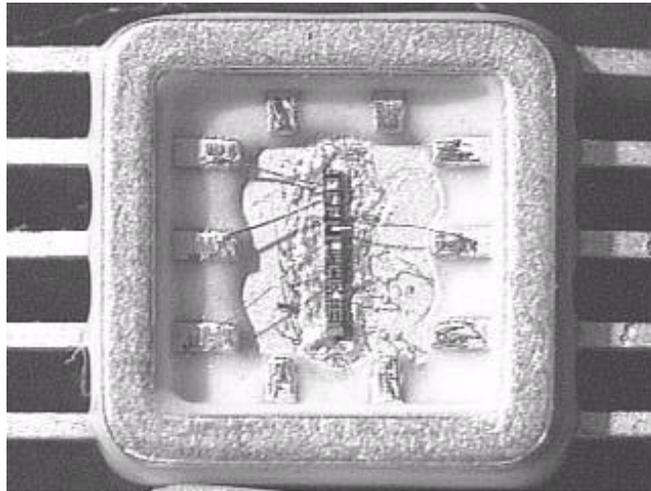
**Figure 5.2** SEM image of the surface of a processed thermionic cooler sample. The mesa heights are  $1.5 \mu\text{m}$  and the areas range from  $20 \times 40 \mu\text{m}^2$  to  $100 \times 200 \mu\text{m}^2$ .

## 5.2 Packaging

To experimentally measure cooling in the devices, packaging was necessary to provide low resistance electrical connections. Simply probing the devices directly created too much heat in the probe tips which drastically impacted the temperature measurement. These low resistance connections needed to be implemented without compromising the thermal paths to the heat sink. In the following three sections, the improvements made in cooler packaging are described.

### 5.2.1 First Generation

The first generation of packaging is shown in Figure 5.3. The first step was to use a dicing saw or the scribe and cleave method to separate the die into individual sets of devices. A die-attach bonder was then used to place a set onto a flattened piece of InSn solder sitting in the package. The package was heated to above the melting point of the solder at which point the die was scrubbed into place to ensure good contact and to eliminate any voids in the solder layer. A wedge bonder was used to wire bond the individual coolers to the package pads. Gold wire with diameters of 1-2 mils was used.



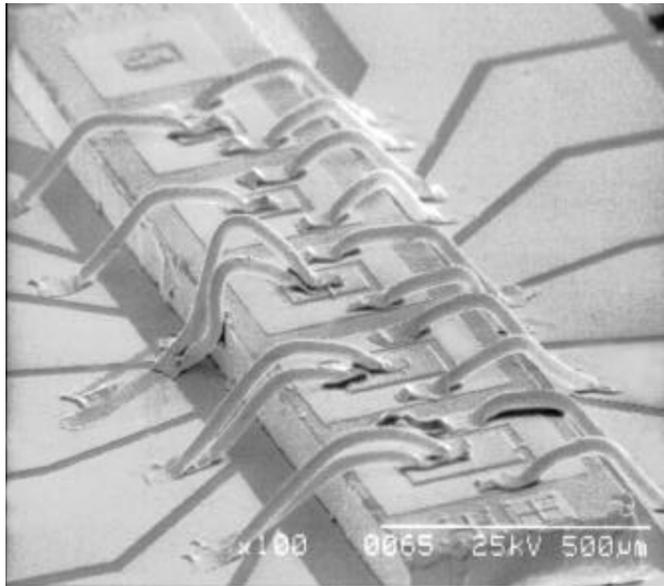
**Figure 5.3** First-generation packaged set of devices. The devices (middle) were cleaved and mounted in the base with InSn solder alloy. A wedge bonder was used for wire bonding with 1 mil diameter wire. The package itself is ceramic with a gold alloy casing and bond pads.

While this first generation package was widely employed to successfully measure cooling, it suffered from several shortcomings. First, the package was not ideally suited for good heat sinking due to the low thermal conductivity of the ceramic material. Secondly, the InSn solder alloy also had a relatively low thermal conductivity and could be tens of microns thick even after manual pressing to flatten it out. Also, lower than normal wire bonding temperatures were needed to avoid having excess solder re-melting. Lastly, long wire bonds were necessary due to the proximity of the device to the bond pads. Placing the device to one side of the package to shorten this distance was not possible due to the clearance needed with the mounting tool.

### *5.2.2 Second Generation*

The second generation provided many solutions to the deficiencies of the previous package. This second package was made from undoped Si wafers where Au contact pads were patterned on the surface. The Si material provided a much better thermal conductivity than the ceramic package, resulting in a superior heat sink. Pure Sn was thermally evaporated on the package mounting pad replacing the pressed InSn solder alloy and avoiding excess amount of solder. This resulted in very thin solder interfaces, on the order of a few microns. The thinner interfaces along with the higher thermal conductivity of pure Sn resulted in an overall decrease in thermal resistance. In fact, the thermal conductivity was further increased due to the

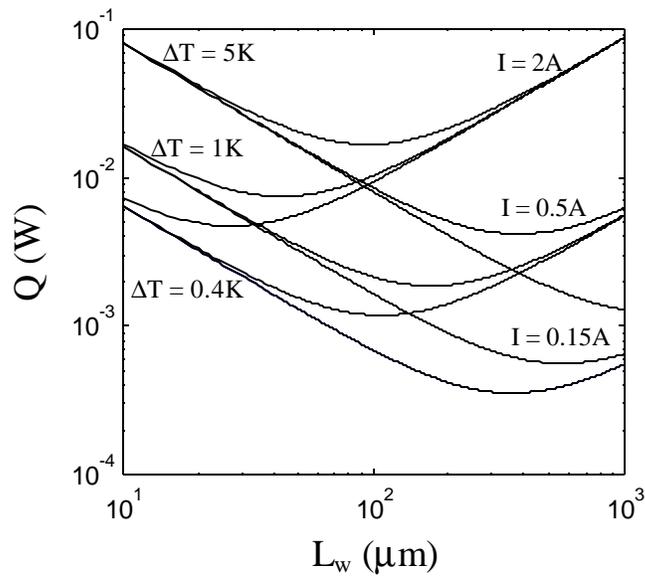
formation of a Au-Sn eutectic when the Sn was melted. Wire bonding could also now be performed at the normal temperature ( $\sim 130$  °C) since the Au-Sn eutectic has a higher melting temperature than pure Sn. A SEM image of a packaged sample is shown in Figure 5.4.



**Figure 5.4** SEM image of a second-generation packaged set of devices. The package was made from an undoped Si substrate where Au contact pads were patterned on the surface.

With the new geometry of the package, the long high-resistance wire bonds could be eliminated. The wire bond length should not be too short however, or else the heat conduction through the wire from the cold side to the heat sink will begin to become an issue. An optimum wire length can be resolved from the wire diameter, its electrical and thermal conductivity, and the temperature difference across the wire bond. Figure 5.5 shows this analysis for a gold wire (1 mil  $\approx 25$   $\mu\text{m}$  diameter) with

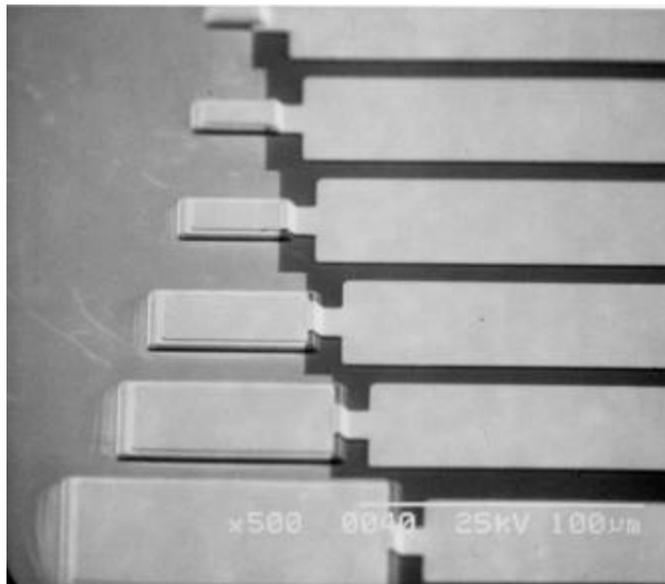
various values of current and cooling temperature assuming that the package side of the wire bond is well heat sunk. For long wire bonds, the Joule heating dominates the cooling power loss, and curves with a similar current approach the same value. For short wire bonds, the heat conduction dominates, and curves with a similar temperature difference approach the same value. In-between these two extremes there is an optimum wire bond length for a given current and temperature differential. This length was usually on the order of a few hundred microns for the bias conditions used.



**Figure 5.5** Cooling power lost versus gold wire length for various bias currents and temperature differences. The electrical and thermal conductivities of gold were taken as  $45.5 \times 10^4 \Omega^{-1} \text{cm}^{-1}$  and  $3.17 \text{ W/cm}\cdot\text{K}$  respectively.

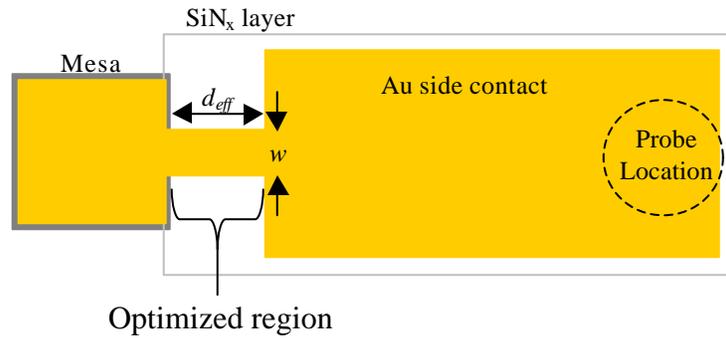
### 5.2.3 Third Generation

The last permutation of packaging involved eliminating the package completely. This was accomplished by replacing the external wire bond with an integrated side contact as shown in Figure 5.6. A thin layer (3000Å) of SiN<sub>x</sub> was used to electrically isolate the side contact from the substrate. The metal lines run for 250 μm, and can be safely probed at the opposite end without incurring any additional heat from the probes. Packaging is no longer necessary as the electrical connections are now integrated, and on-chip testing is possible. While a large improvement in performance is not expected compared to the previous package generation, the process is simpler. The steps of scribing, cleaving, dicing, mounting, and wire



**Figure 5.6** SEM image of the surface of a third-generation processed sample. The dark staircase region on the right side of the mesas is the SiN<sub>x</sub> used to electrically isolate the side contacts from the substrate. The metal lines run for 250 μm.

bonding can be discarded, and variances from run to run are reduced considerably. This makes comparison of results for different devices or processing runs more straightforward. Removal of the gold wire results in further simplification in the temperature measurement since the top of the device is now uniformly flat. Finally, smaller area devices can be tested, and are not limited by the capabilities of the wedge bonder and wire diameter.



**Figure 5.7** Top view of the side contact geometry. The optimized region is the area close to the device mesa where Joule heating and heat conduction are most important.

Just as the wire length was optimized in the second generation of packages, the side contact geometry must also be optimized. The critical part of the design is in the section nearest the mesa as shown in Figure 5.7. The same basic equation for cooling power loss can be used:

$$Q = \frac{d_{eff}}{2sA} I^2 + \frac{bA}{d_{eff}} \Delta T \quad (A = t \cdot w) \quad (5.1)$$

where  $d_{eff}$  is the effective length,  $t$  the thickness,  $w$  the width,  $A$  the cross-sectional area,  $I$  the electrical current,  $\mathbf{s}$  and  $\mathbf{b}$  the electrical and thermal conductivities, and  $\Delta T$  the temperature differential. The first term on the right hand side of Equation 5.1 describes the Joule heating, and the second represents heat conduction. In the case of the wire bond, the diameter was fixed and the optimum wire length was minimized. Now the length is fixed and the width must be minimized. The optimum width and corresponding cooling power loss can be derived from Equation 5.1:

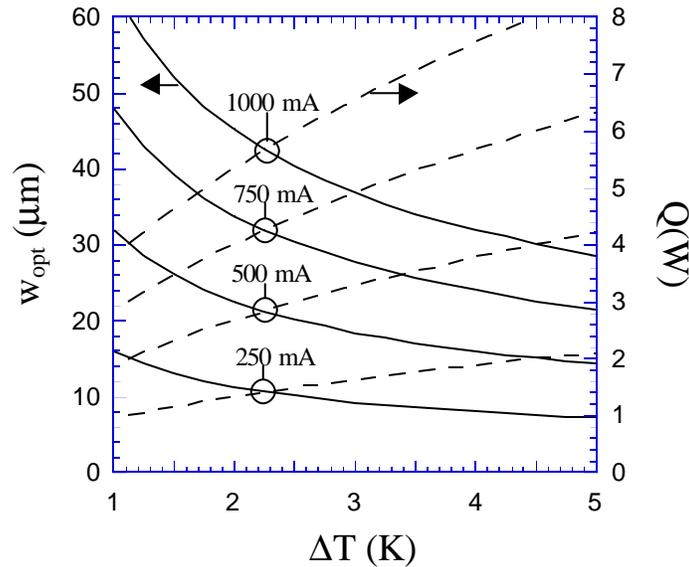
$$w_{opt} = \frac{I d_{eff}}{t} \sqrt{\frac{1}{2 \mathbf{b} \mathbf{s} \cdot \Delta T}} \quad (5.2)$$

$$Q(w_{opt}) = I \sqrt{\frac{2 \mathbf{b} \cdot \Delta T}{\mathbf{s}}} \quad (5.3)$$

To make these equations useful, the effective length  $d_{eff}$  must be determined. Since the side contact wire dissipates heat in a three-dimensional fashion through the  $\text{SiN}_x$  isolation layer and substrate, the question to ask is over what distance does the majority of the temperature-drop fall? To estimate this length, a three-dimensional heat-equation finite-element simulation was used to extract the temperature profile along the side contact. Assuming a uniform temperature across the top of the mesa and an ideal heat sink at the bottom of the substrate,  $d_{eff}$  was estimated to be 10-15  $\mu\text{m}$  where this value was taken to be the distance at which the temperature dropped to  $1/e$  of its maximum value. The calculated optimum contact width and cooling

power loss are shown in Figure 5.8 assuming a substrate thickness of 150  $\mu\text{m}$ ,  $\text{SiN}_x$  thickness of 0.3  $\mu\text{m}$ , Au metal thickness of 1  $\mu\text{m}$ , and a  $d_{\text{eff}}$  of 12  $\mu\text{m}$ .

The use of an air-bridge structure was also considered to perhaps further reduce the heat conduction in the side metal next to the mesa. Further analysis using ANSYS showed only marginal improvements, and the added complexity was not justified.



**Figure 5.8** Optimum contact width (solid lines) and corresponding cooling power loss (dashed lines) versus bias currents and temperature differences for integrated side contact geometry.

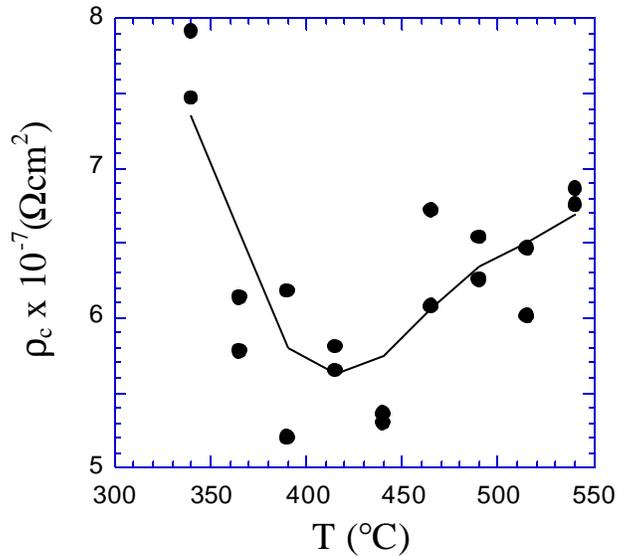
### 5.3 Contact Resistance

Throughout the development of thermionic coolers, reduction in contact resistivity ( $r_c$ ) has been an incessant pursuit. Because the various InP-based materials have a low electrical resistivity,  $r_c$  usually dominates. This provides additional Joule

heating very close to the cooling region of the device and must be minimized to attain any appreciable cooling. Since all of the contact regions in the device structure are InGaAs, only contacts to this material will be considered.

The transmission line model (TLM) method [1] was used to measure contact resistivity. This analysis included the measurement of “end resistance” ( $R_E$ ), often overlooked in other reports on  $r_c$ . This additional measurement accounts for the changing sheet resistance underneath the contact area during the alloying process. The simple TLM analysis assumes that the sheet resistivity is the same everywhere and does not change during alloying. The changing sheet resistance alters the transfer length or effective area of the contact over which the majority of current passes.  $R_E$  infers the transfer length from a measurement of voltage drop across the contact pad. Accurate measurements require very narrow pad widths due to the very low sheet resistivity of the metal layer. The pad widths used here were 3 to 20  $\mu\text{m}$ .

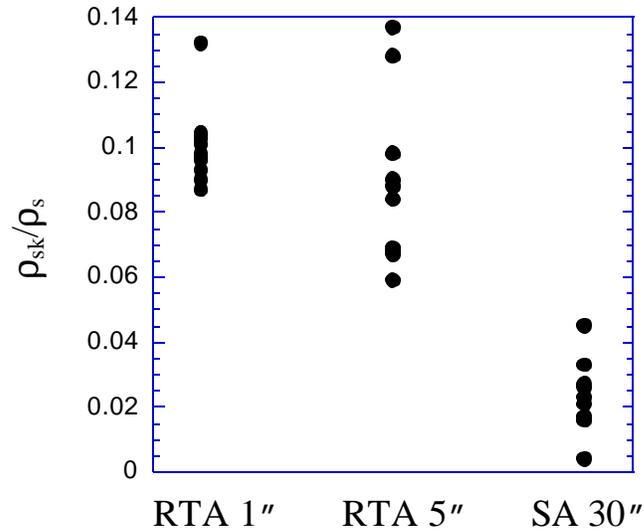
The first contact scheme investigated was for *n*-type InGaAs, and used Ni/AuGe/Ni/Au (50/1000/100/5000Å). The details of the microstructure after the alloying process have been studied extensively in the literature [2-4]. The basic idea is that the Ge diffuses into the semiconductor and acts as a dopant element while the Ni enhances diffusion and is a wetting layer. Figure 5.9 shows the results for contact resistivity versus alloying temperature for an InGaAs contact layer doped to  $3 \times 10^{18} \text{cm}^{-3}$ . The best values are between 5 and  $6 \times 10^{-7} \Omega\text{cm}^2$  for alloying temperatures near 425 °C. For the values measured in Figure 5.9, the alloying used a



**Figure 5.9** Contact resistivity versus RTA alloying temperature for Ni/AuGe/Ni/Au contacts to InGaAs ( $3 \times 10^{18} \text{ cm}^{-3}$ ). Samples were alloyed for 1 second and measured by the TLM method.

rapid thermal anneal (RTA) process where the temperature is ramped up and down very quickly. In this metallization scheme, rapid heating and cooling was shown to produce the lowest contact resistance in agreement with previous reports [2,4]. From the TLM analysis, it was possible to estimate the change in sheet resistivity under the contact pads resulting from the alloying process. Figure 5.10 shows these results for three different alloying methods and hold times. In the RTA method the heating and cooling ramp rates are on the order of 50-100 °C/sec while the strip annealer is roughly 5-10 °C/sec above 300 °C. For the 1 second hold time in the RTA, the normal Si-wafer stage is replaced with sapphire to further speed up the heating and cooling rates. From Figure 5.10, the longer the sample is kept at elevated temperatures, the greater the change in sheet resistivity under the contacts.

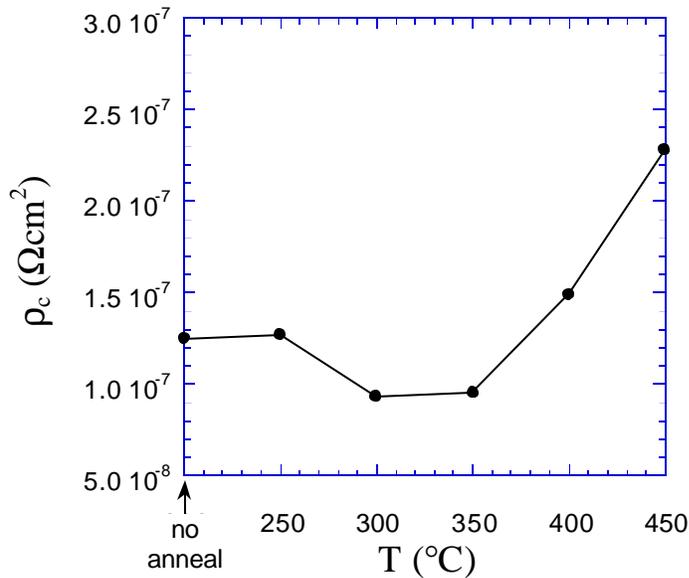
Generally, however, this is at the expense of an increased contact resistance and little advantage is gained from the enhanced sheet resistivity.



**Figure 5.10** Ratio of alloyed to unalloyed sheet resistivity versus alloying method and hold time for Ni/AuGe/Ni/Au contacts to  $n$ -type InGaAs ( $3 \times 10^{18} \text{ cm}^{-3}$ ). RTA stands for a rapid thermal anneal process while SA represents a slower strip anneal process.

If higher doping is used in the InGaAs contact layer, the extra Ge-doping and alloying process is unnecessary. In this case, unalloyed contacts are attractive since careful control over the alloying process is no longer needed. Also, there is no alteration of the semiconductor underneath the contacts which is desirable for reliability issues. Ti/Pt/Au (150/1000/5000Å) was investigated for contacts to  $n$ -type InGaAs doped around  $1.5\text{-}2.0 \times 10^{19} \text{ cm}^{-3}$ . In this metallization recipe, the Ti acts as both an adhesion layer and barrier component. The high dopant concentration allows

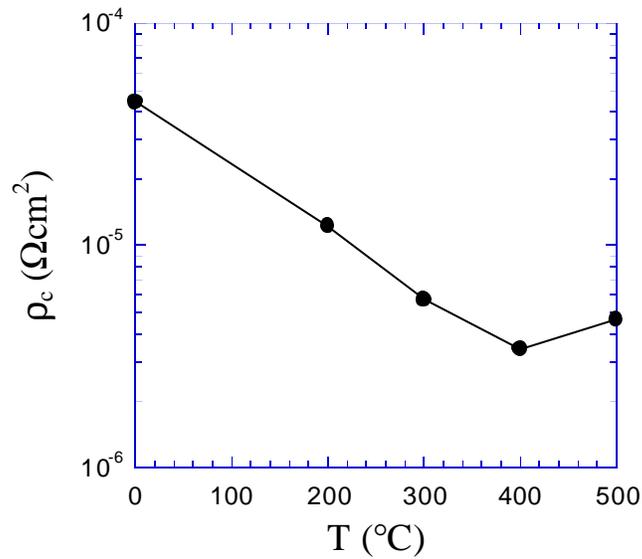
for a large field emission providing that the native oxide is not too thick [5]. The Pt layer prevents Au penetration into the underlying layers. A thickness of at least 1000Å is required for annealing up to 450 °C, and 2000 Å if the device is to undergo extended high temperature operation [6]. Figure 5.11 shows  $r_c$  versus annealing temperature, which was performed in the strip annealer and held for 20 seconds. The contact resistance was found to be relatively independent of the heating and cooling procedure, and a good value is even obtained with no annealing at all.



**Figure 5.11** Contact resistivity versus alloying temperature for Ti/Pt/Au contacts to *n*-type InGaAs ( $2 \times 10^{19} \text{cm}^{-3}$ ). Samples were alloyed for 20 seconds and measured by the TLM method.

*P*-type contacts were also investigated, however only highly doped InGaAs ( $2 \times 10^{19} \text{cm}^{-3}$ ) was examined. The same Ti/Pt/Au metallization was used as in the *n*-type case. The use of a common contact for both *p*- and *n*-type coolers is expected to

simplify the integration process of the two thermoelements. Figure 5.12 shows  $r_c$  versus annealing temperature. The minimum value obtained was  $3.5 \times 10^{-6} \Omega\text{cm}^2$ . Despite attempts with alternate metallization schemes such as Au/Zn/Au, this remains best value for  $r_c$  at this time.



**Figure 5.12** Contact resistivity versus alloying temperature for Ti/Pt/Au contacts to p-type InGaAs ( $2 \times 10^{19} \text{cm}^{-3}$ ). Samples were alloyed for 20 seconds and measured by the TLM method.

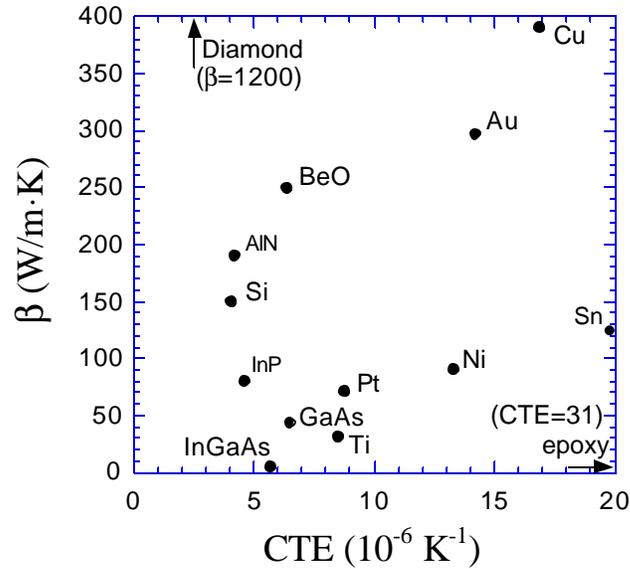
**Table 5.1** Summary of minimum contact resistivity results and comparative values reported in the literature for *n*- and *p*-type InGaAs. All values are in units of  $\Omega\text{cm}^2$ .

<i>Metallization</i>	<i>Type</i>	<i>Doping</i> ( $\text{cm}^{-3}$ )	<i>Measured</i> $r_c$	<i>Reported</i> $r_c$	<i>Ref</i>
Ni/AuGe/Ni/Au	N	$3 \times 10^{18}$	$5.3 \times 10^{-7}$	$8 \times 10^{-8}$	[3]
Ti/Pt/Au	N	$1.5 \times 10^{19}$	$9.4 \times 10^{-8}$	$2.1-5.5 \times 10^{-7}$	[7]
Ti/Pt/Au	P	$2 \times 10^{19}$	$3.5 \times 10^{-6}$	$3.4 \times 10^{-8}$	[8]
Au/Zn/Au	P	$10^{18}-10^{19}$	–	$1.3-16 \times 10^{-6}$	[9]

A summary of the presented results and comparative values reported in the literature are shown in Table 5.1. The measured values for *n*-type InGaAs compare fairly well with the best reported numbers. The very best reported value of  $4.3 \times 10^{-8} \Omega \text{cm}^2$  was for higher doped material ( $5 \times 10^{19} \text{cm}^{-3}$ ) [10]. Generally speaking, if the doping is greater than  $1 \times 10^{19} \text{cm}^{-3}$ , then the Ti/Pt/Au metallization should be used. Otherwise for lower dopings, the Ni/AuGe/Ni/Au contacts should be considered for *n*-type material, and Au/Zn/Au contacts for *p*-type material. Further work is needed to reduce the contact resistance for our *p*-type InGaAs, as our best value is two orders of magnitude higher than the best reported value.

#### 5.4 Substrate Transfer

A more in depth and quantitative analysis of substrate thermal resistance will be presented in Chapter 6, yet the incentive for attempting substrate transfer should be evident from a simple estimation. While the thermal conductivity of the thermionic cooler layers is at least an order of magnitude smaller than InP, the thermal resistance of the substrate can be as large or even larger than the cooler layers due to the greater thickness. This results in a significant amount of heat flowing back to the cold side of the cooler, reducing the efficiency. The efforts for replacing the InP substrate with a higher thermally conducting one such as silicon, copper, or even diamond, are described in this section.

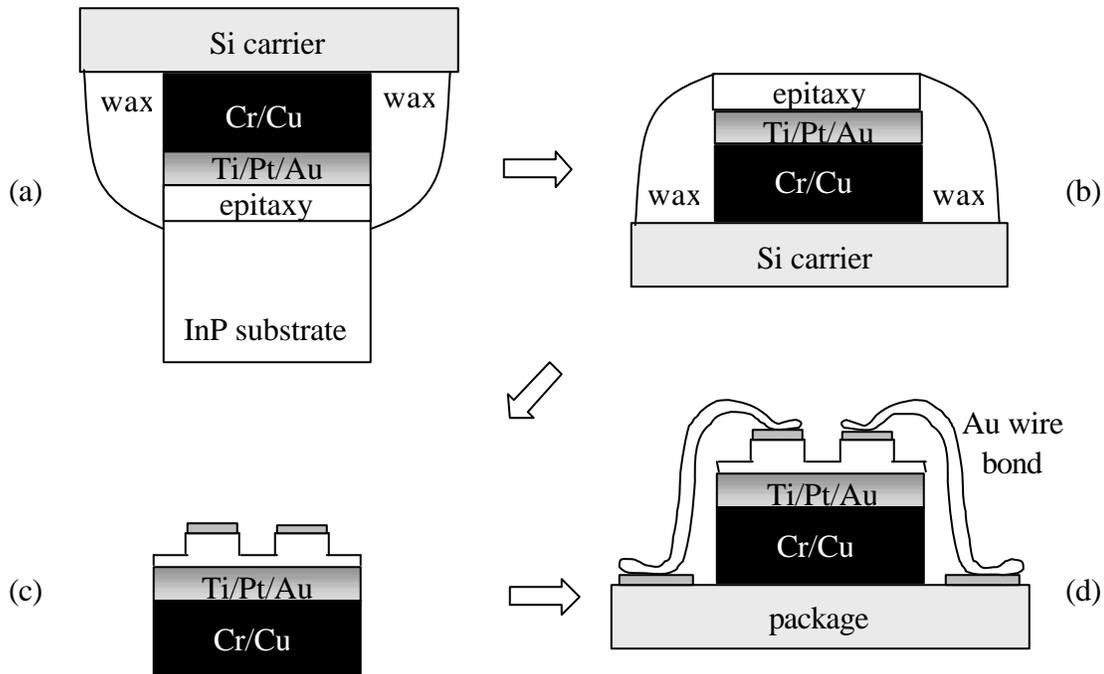


**Figure 5.13** Thermal conductivity and coefficient of thermal expansion for materials relevant to substrate transfer processes.

The processes for substrate transfer considered here can be categorized as either bonded or deposited. Bonded refers to the joining of the epitaxial grown layers to a surrogate substrate where the original substrate is removed before or after the union. In most cases an intermediate material, such as a metal, solder, or epoxy, is used to facilitate a complete and uniform junction. A deposited process means that the new substrate is actually formed directly on the epitaxial layers such as in vacuum evaporation or electroplating. In any of these above cases, careful attention must be paid to the material properties and a trade-off between the coefficient of thermal expansion (CTE) and thermal conductivity ( $\mathbf{b}$ ) is often the issue. Figure 5.13 shows the CTE and  $\mathbf{b}$  for the semiconductors, metals, and bonding materials considered

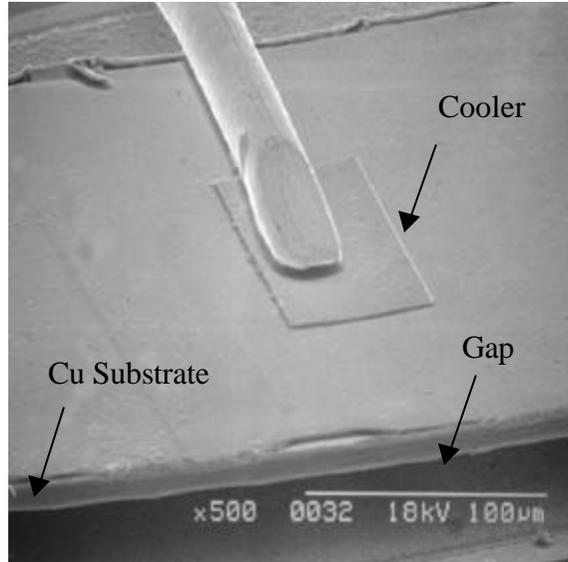
here [11,12]. Comparing the CTE for the InP-based films to that of most pure metals, a large mismatch can be seen. There are a few refractory metals like tungsten and molybdenum (not shown in figure) that have much closer CTE's, but their  $\mathbf{b}$  is not as great as Au or Cu. The CVD Diamond with a CTE of  $2.5 \times 10^{-6} \text{ K}^{-1}$  and a  $\mathbf{b}$  of 1200 W/mK seems to be a good compromise between the two, however it is a much more expensive material and it is difficult to get highly polished surfaces. Besides  $\mathbf{b}$  and CTE, issues of surface roughness, adhesion quality, and bonding mechanisms must be evaluated.

The first method investigated involves the transfer of a 2- $\mu\text{m}$ -thick epitaxial-grown thermionic-cooler structure to a thermally evaporated 10- $\mu\text{m}$ -thick copper substrate. A blanket evaporation of Ti/Pt/Au (100/500/5000Å) was performed to make an ohmic contact to the topmost InGaAs layer. Three successive runs in a thermal evaporator were then executed to deposit a total of 10  $\mu\text{m}$  of Cu. Before the first deposition of Cu and each time the system was vented to replenish the Cu source, a 500 Å layer of Cr was deposited as a sticking layer and to prevent the oxidation of the Cu surface. After the desired Cu thickness was reached, 1  $\mu\text{m}$  of Sn was thermally evaporated for later use as a soldering layer in the device packaging. The processing procedure from this point is outlined in Figure 5.14. The sample is mounted Cu-side down onto a larger piece of silicon using wax. The InP substrate is then chemically etched in a solution of 3HCl:1H<sub>2</sub>O, exposing the epitaxial layers.



**Figure 5.14** Thin Cu-substrate transfer process. The steps are (a) E-beam evaporate ohmic metal, copper substrate, and solder layers, and mount epi side down to a silicon carrier with wax. (b) Remove InP substrate with a wet etch and (c) deposit top metal to etch mesas. Dice samples and remove the wax. (d) Package and wire bond devices. (Sn soldering layer not shown)

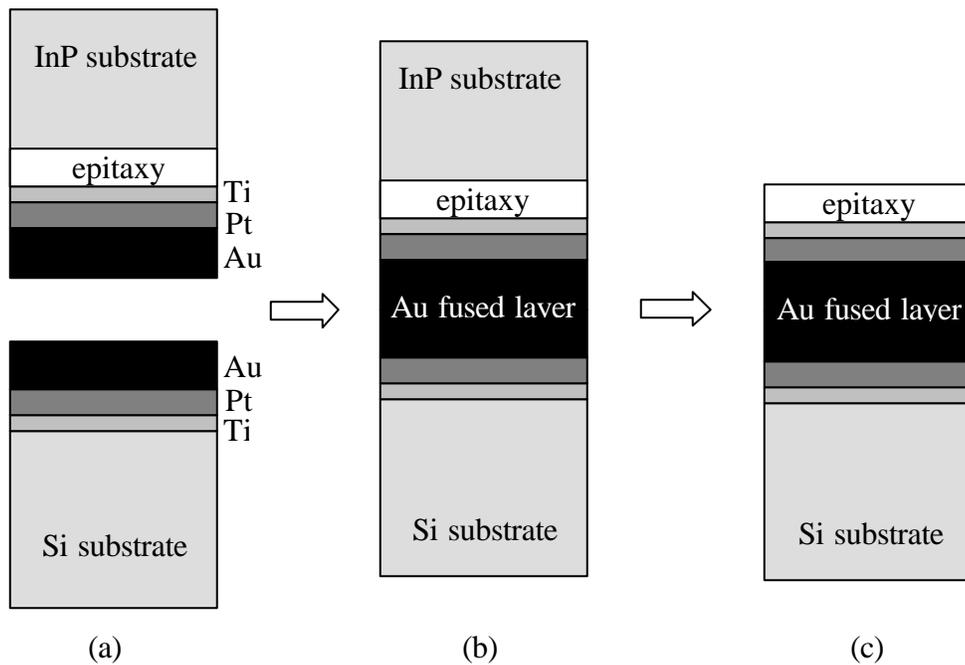
Ti/Pt/Au ohmic contacts were patterned on the surface and mesas were defined by dry etching. The devices were then diced into rows with a diamond saw and the wax was removed with acetone. The individual rows of devices were attached to packages using the pre-deposited Sn solder. Figure 5.15 shows a SEM image of a packaged device. While about 75% of the sample survived all of the processing steps up to the dicing, most of the sample was lost due to the large mechanical stress associated with dicing. Future processing runs with this technique should use a wet chemical etch of the copper to separate the devices into sizes that are manageable



**Figure 5.15** SEM of a packaged thin-film thermionic cooler on a 10- $\mu\text{m}$ -thick copper substrate. It is clear from the photo that there are large gaps that the solder did not spread to during packaging.

with vacuum tweezers. The maximum cooling achieved with this device was only 0.1 °C, which compares poorly to the same structure processed on the growth substrate that cooled by 0.7 °C. This is likely due to the large thermal resistance at the interface between the copper and the package. Specifically, the solder layer was not performing as desired and large voids were present. The SEM photo in Figure 5.15 indicates that there is indeed an air gap in this region. While the packaging continues to be a challenge for the Cu-substrate samples, the process itself appears to work adequately. No cracking or bowing of the epitaxial layer was observed, even though film stress values have been reported in the range of 50 MPa for sputtered Au [13]. Electroplating is known to result in thin metal films with much less stress on

the order of 1 MPa in plated Cu [14]. Electroplating was not considered in this work due to the small size of the samples and the foreseen difficulties with obtaining uniform robust metal layers, however there has been reports of success on 2" diameter wafers with this process for HBT integrated circuits [15].



**Figure 5.16** Au-Au fusion process for transferring epitaxial layers from the InP growth substrate to a Si substrate. The steps are (a) E-beam evaporation of Ti/Pt/Au metallization, (b) Au-Au fusion under pressure and at high temperatures, and (c) InP substrate removal. The process can be generalized to any surrogate substrate.

The second method attempted was to transfer the InP epi layer onto a Si substrate by Au-Au fusion. This process was attractive since bonding parameters had already been optimized in previous work [16]. Characterization samples were used to determine the feasibility of the process for later thermionic cooler processing.

Figure 5.16 shows the steps used in the Au-Au bonding. After sample cleaning, metal layers of Ti/Pt/Au 500/1000/15000Å were deposited by e-beam evaporation. The samples were then brought into contact and held under pressure (~ 70 kPa) using a rubber-boot vacuum fixture on a hot plate. The temperature was ramped up at 1°C/min to a temperature of 350 °C, held for five minutes, and then ramped down at the same rate. The slow ramping was to reduce stress caused by the CTE mismatch between the wafer and metal. After the fusion, the InP substrate was etched off, and the remaining epi layers were examined under an optical microscope. Of the two samples bonded, only one appeared to have most of its surface fused and void bubbles were present in several places on the sample. Evaporating a thin layer of Sn after the Au evaporation is expected to help with the reliability of this process since the solder can actually reach its melting temperature and reflow to fill in any voids. Any addition of Sn would increase the thermal resistance, and must be considered when deciding how thick a layer to use.

In a variation of the previous procedure, Au-Au fusion using a diamond substrate (1 cm<sup>2</sup> area, 300 μm thick) was briefly attempted. It became evident early on that the CVD-grown substrates used were not planar enough and showed a bowing across the surface of 3 μm and a maximum surface roughness of 1.2 μm. Highly planar samples and crystallographic surfaces are necessary for high quality Au-Au fusion. The use of Sn was employed in order to planarize the surface, but even with 5 μm of evaporated Sn, difficulties achieving a good bond were

encountered. Smoother and more planar diamond samples are needed to improve the bonding without sacrificing the benefits of thermal conductivity by using thick solder layers.

## 5.5 Summary

In this chapter we discussed the basic processing procedures used for heterostructure integrated thermionic coolers. The steps are kept as simple as possible to facilitate their integration with optoelectronic devices. To characterize the single-stage coolers, packaging is required. The goal of packaging is to allow for the measurement of the intrinsic device without effecting the measurement itself. Three generations of packaging were presented, and the improvements in each discussed. It is believed that we are nearly at the limit of optimizing the packaging, and further improvements in single-stage performance must come from the device design.

The minimum contact resistivity values for *n*-type InGaAs are also close to being fully optimized and compare well with the best values reported in literature. *P*-type contact resistance still needs further reduction which should be possible. Ti/Pt/Au contacts are generally preferred for both *n*- and *p*-type contacts as long as the InGaAs material is doped to at least  $10^{19} \text{ cm}^{-3}$ .

Several prospects exist for transferring the InP-based epitaxial layers from the InP growth substrate to a surrogate substrate with a higher thermal conductivity. Moderate success was obtained with the thin Cu-film process, but handling and

packaging problems were encountered. Au-Au bonding to Si or Cu substrates seems feasible. Diamond substrates are preferred, however highly polished surfaces are needed.

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*Chapter 5: Device Fabrication and Packaging*

## **Chapter 6**

### **Cooling Results and Analysis**

Before moving forward with the integration of thermionic coolers with optoelectronic devices, it is first necessary to fully characterize and optimize the individual cooler. In the last chapter, the evolution of packaging for effective heat sinking and electrical connections for testing was described. Our first challenge here is with the measurement of temperature itself. The device areas considered range from  $200 \times 200 \mu\text{m}^2$  to as small as  $10 \times 10 \mu\text{m}^2$ . In many cases, not only the average temperature over such areas is desired, but the actual temperature distribution. Several commercial vendors claim to have characterization equipment that can measure temperature with sub-degree or sub-micron precision, but none are capable of high spatial and temperature resolution simultaneously. Consequently, novel small-scale temperature characterization systems needed to be developed. The first section of this chapter is devoted to these characterization solutions and techniques. The section following presents the experimental results and analysis for various device sizes, ambient temperatures, superlattice designs, and material types. A new type of cooler structure is also presented that integrates together a thermionic and thermoelectric (TITE) cooler structure into a two-stage three-terminal device. The non-ideal effects that impede our arrival to the intrinsic device limitations are then discussed in detail. Finally, simulations to model and explain the device operation,

including the non-ideal effects, are given. These simulations are then used to predict improvements in performance as the non-ideal effects are reduced.

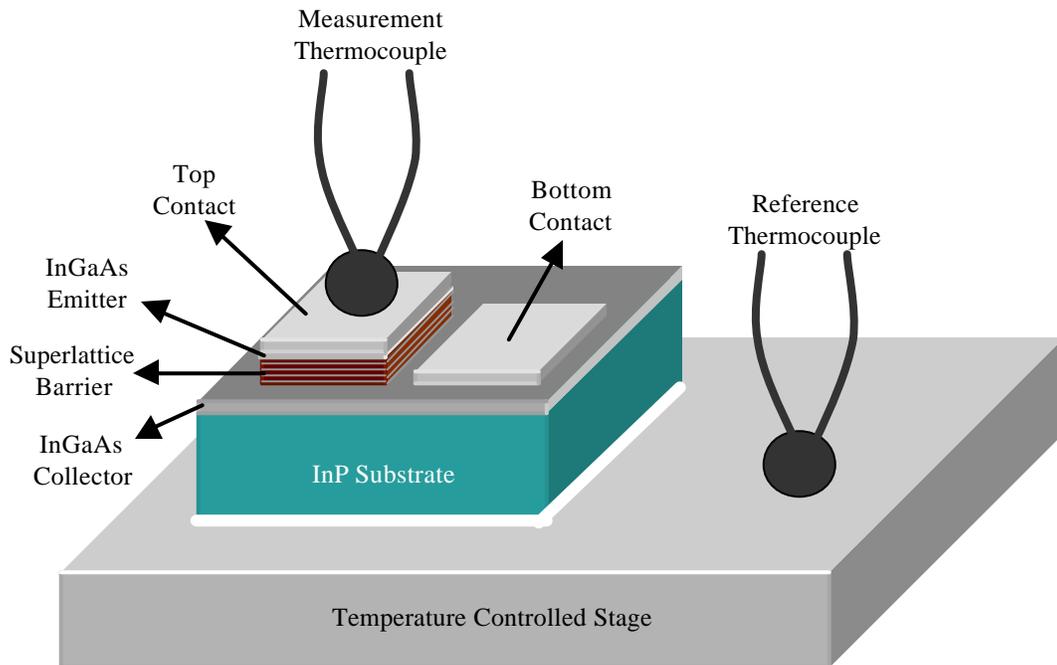
## 6.1 Measurement Techniques

The measurement methods described below can be categorized into either contact or non-contact implementations. The contact techniques involve either the manual placement or the integration of a temperature sensor with the cooler, while the non-contact techniques measure the temperature indirectly by monitoring such things as reflectivity or emissivity. The advantages and disadvantages are described in each specific case.

### 6.1.1 Micro-Thermocouples

The micro-thermocouple measurement has been used for the majority of temperature characterization due to its robustness and ease of testing many devices quickly. The set-up is shown in Figure 6.1. As in many of the temperature measurement systems, the sample is placed on a temperature-controlled copper stage using thermal compound to ensure good contact with the heat sink. Two thermocouple wires (1-2 mil diameter, type E) are mounted on micro-positioners where a positive and negative lead are attached and the remaining two leads connect to a voltmeter. The reference thermocouple is kept on the stage while the measurement thermocouple is placed on the cooler. Normally, for atmospheric conditions, a thin layer of moisture

is present on all surfaces that allows for an adequate thermal connection between the thermocouple and cooler. However, it was determined that the temperature results were more reproducible when a small amount of thermal compound was used as a thermal interface. With the stage kept at constant temperature, the two micro-thermocouples are used in a differential measurement of temperature as the current bias is varied. A computer along with LabVIEW [1] software was used to control all instrumentation and automate the measurement process with the only exception being the thermocouple placement.



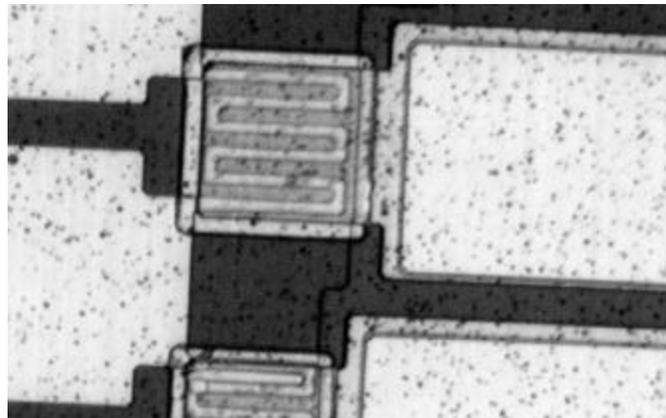
**Figure 6.1** Micro-thermocouple characterization set-up. The stage is kept at constant temperature while two micro-thermocouples are used in a differential measurement of temperature for various current biases. The external or integrated wire bond is not shown.

Using this system, point measurements anywhere on the surface were possible within the limits of the thermocouple size. While thermocouple wire diameters as small as 1 mil were used, the actual junction was typically twice that size. Only devices down to around  $40 \times 40 \mu\text{m}^2$  could reliably be tested, and even then the thermocouple would present a significant thermal conduction path and affect the measurement. Nonetheless, superb temperature resolutions of below  $0.01 \text{ }^\circ\text{C}$  were possible, with response times less than  $100 \mu\text{s}$ . Many of the results shown in Section 6.2 used this system.

### 6.1.2 Integrated Platinum Heaters

Platinum material is used extensively in resistive temperature devices (RTD's). As their name implies, these types of devices use the fact that the electrical resistance of metals change with temperature. For Pt, in the range of 0 to  $100 \text{ }^\circ\text{C}$ , the resistance changes nearly linearly with a temperature coefficient of  $3.929 \times 10^{-3} \text{ K}^{-1}$ . In our case, Pt metal lines were lithographically defined on top of the cooler as in Figure 6.2. These lines not only worked as temperature sensors, but also as variable heaters to measure the cooling versus heat load. While valuable heat load characterization could be made on the larger devices, the Pt resistors did not scale well for small devices since metal lines could not be made long enough. Even the longer wires on the larger devices did not match the resolution of the micro-thermocouple system, and little advantage in temperature measurement was seen. Furthermore, the

additional thermal conduction paths of the connections for the resistors and  $\text{SiN}_x$  isolation layer resulted in reduced cooling by as much as 50% when compared with normal devices. In spite of this, specific applications such as transient testing or measurement in vacuum still exist for the Pt resistors.

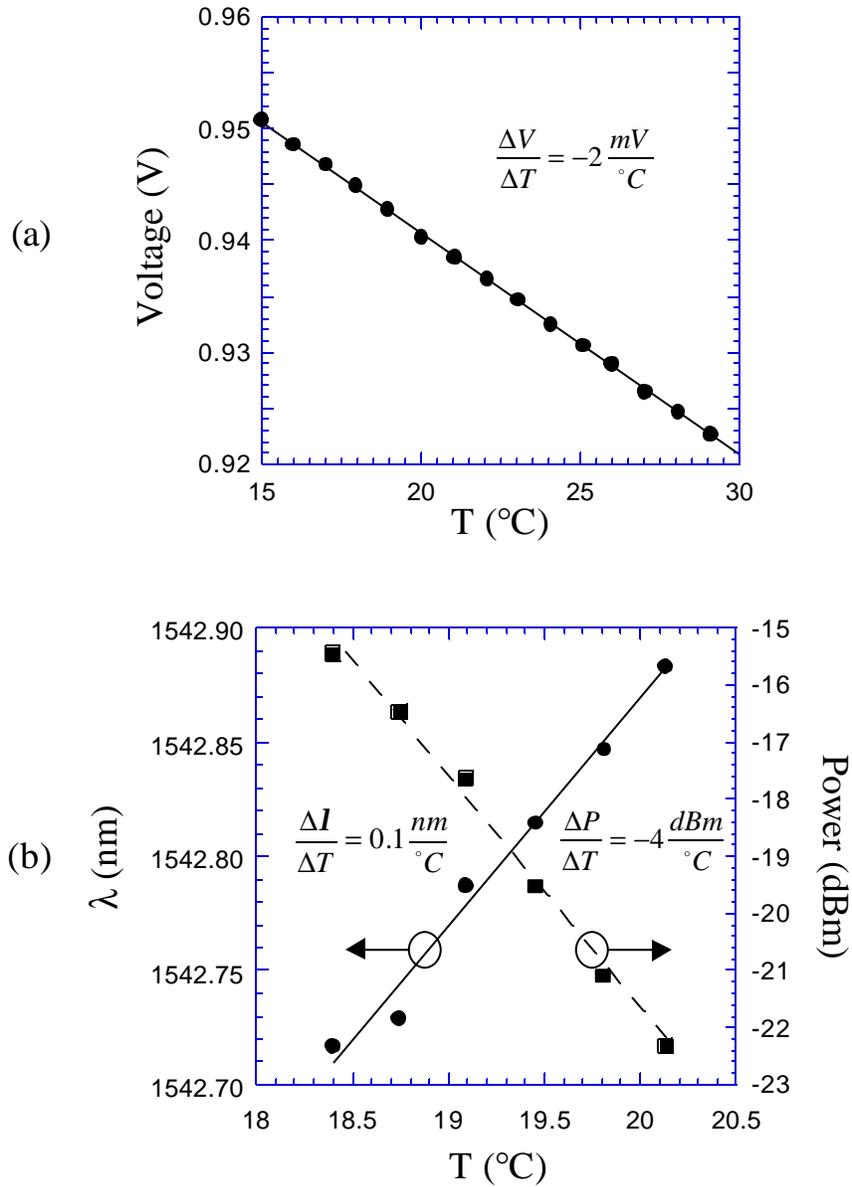


**Figure 6.2** SEM image of a cooler with a patterned Pt-heater on top. The Pt metal was electrically isolated from the top of the cooler with a thin layer of  $\text{SiN}_x$ .

### 6.1.3 Integrated Optoelectronic Devices

The operational characteristics of most optoelectronic devices are by nature temperature dependant. These characteristics can therefore be correlated to temperature as a measurement method. For instance, in the case of *p-i-n* detectors the temperature-dependent current-voltage relationship can be used to measure temperature [2]. A more familiar example is the use of wavelength shift or output power in lasers. Figure 6.3 illustrates some of these characteristics versus

temperature. Further discussion of integrated structures will be postponed until Chapter 7.



**Figure 6.3** Temperature dependent properties of some optoelectronic devices (a) A p-i-n InP diode under constant current has a temperature dependent voltage. (b) The wavelength and optical power of a DFB laser diode are also temperature dependent.

#### 6.1.4 IR Camera

Infrared cameras have found numerous uses in macroscopic temperature measurement, especially when the temperatures are extremely high and exceed the range of contact-type sensors. Recently they have also found applications in microscopic thermal imaging [3,4] as new advances in the technology have emerged. In conjunction with precision optics, the IR camera systems can produce thermal images of surfaces with temperature resolutions of a few degrees and spatial resolutions of 10's of microns.

The basic experimental set-up was controlled by a PC which coordinated the timing of the camera snapshots and the pulse generator that applied the signal to the device [3,5]. The camera captured 3-5  $\mu\text{m}$  IR radiation on a  $256 \times 256$  InSb focal plane array detector. Each of the 65,536 detectors formed a single pixel in the final image.

While qualitative data of heating and cooling could be collected using this technique, the temperature resolution was not adequate and reproducibility was difficult. This is most likely attributed to the poor emissivity of smooth metals (<20%) which cover the top of the cooler surface allowing for a large portion of the signal to come from reflected radiation off other sources. The emissivity of an opaque material is in general inversely proportional to its reflectivity. When measuring the surface of a low emissivity material, much of the energy reaching the sensor can be reflection from other nearby emitters. This effectively increases the

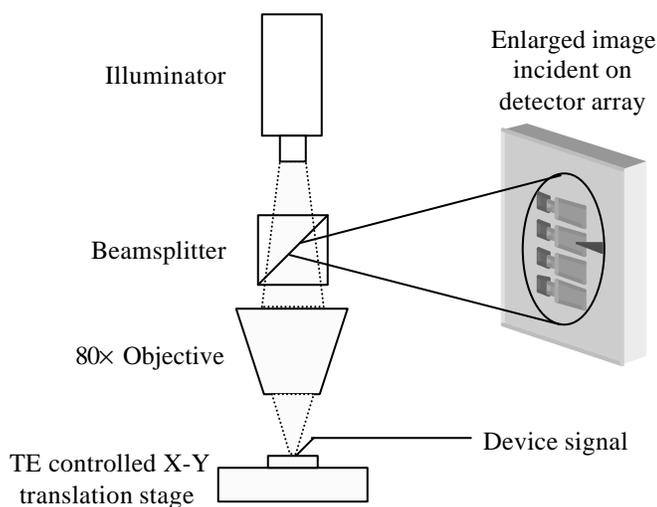
noise in the signal. In the next section, an alternative method for temperature imaging is described which solves many of the problems encountered with the infrared system.

### 6.1.5 Thermoreflectance

The thermoreflectance technique is based on the temperature-induced reflectivity change in materials. All materials exhibit this change, albeit small in most cases. By monitoring the change in intensity of reflected light, the surface temperature can be determined [6-8]. Due to the small change in reflectivity ( $\Delta R/\Delta T \sim 2 \times 10^{-5} / ^\circ\text{C}$ ), a lock-in technique is needed to detect the signal.

The measurement system is shown in Figure 6.4 (developed by James Christofferson). The device is illuminated with a white light source and biased with current pulses at 200 Hz to allow for heterodyne filtering. A magnifying objective and beamsplitter are used to image the reflected signal on to the detector. The detector used was a Hamamatsu 16×16 photodiode array. Calibration is accomplished by normalizing to previously measured temperature measurements using the micro-thermocouple system. Only the large devices are used for calibration so that the thermocouple size does not affect the cooling.

This method has proved to be indispensable in the mapping of temperature profiles across the surface of coolers. High quality images of the coolers have been successfully measured with 100 mK temperature and sub-micron spatial resolution.

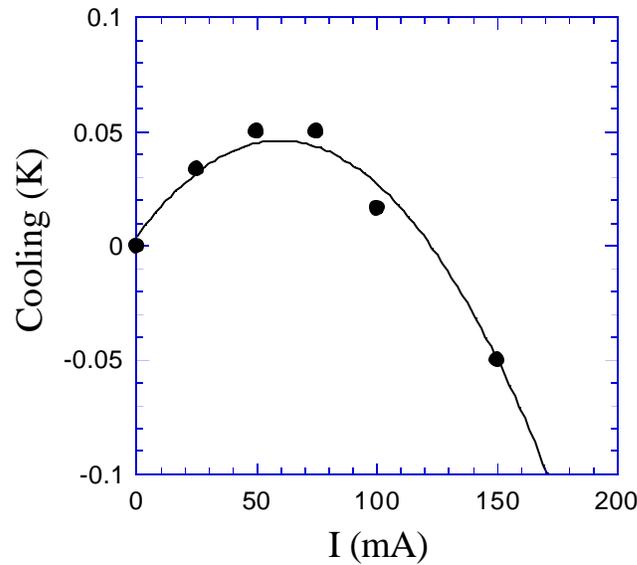


**Figure 6.4** Experimental setup for thermoreflectance measurement system. The diffraction limit of visible white light from the illuminator bounds the spatial resolution to a sub-micron scale.

## 6.2 Experimental Results

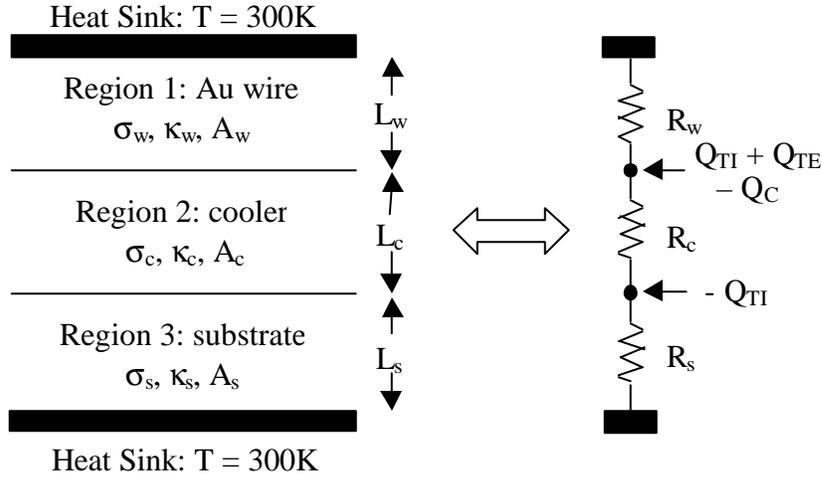
The first experimental demonstrations of cooling were modest to say the least. An example of an early cooling result is shown in Figure 6.5. A humble 0.05 K of cooling was measured around 60mA of current for a  $3200 \mu\text{m}^2$  device size. Still, the successful measurement of such a small temperature change was encouraging as it allowed for analysis as to the limitations on performance. By fitting the data points with a second order polynomial, the linear and quadratic components could be quantified. As in conventional TE coolers, the linear coefficient represents the Peltier cooling or heating effects in the device ( $\mu I$ ) and the quadratic coefficient describes the Joule heating contributions ( $\mu I^2$ ). By observing how these coefficients change versus device size, geometry, ambient temperature, superlattice

design, and other conditions, conclusions can be made about optimum design parameters or limitations from non-ideal effects. The results discussed in this section are for single-stage coolers. More complex, integrated structures are analyzed in Chapter 7.



**Figure 6.5** One of the first experimental results demonstrating cooling. The thermionic cooler structure consisted of a simple  $1\ \mu\text{m}$  thick  $n$ -type InGaAsP-barrier ( $1 \times 10^{17}\text{cm}^{-3}$ ) between InGaAs emitter and collector regions ( $2.8 \times 10^{18}\text{cm}^{-3}$ ). The device area was  $3200\ \mu\text{m}^2$ . Small cooling in this early device was limited by the packaging and contact resistance.

Before discussing the results, a more in-depth look at the qualitative device operation would be useful. The device can be broken into three regions as shown in Figure 6.6, where the electrical conductivity ( $\mathbf{s}_n$ ), thermal conductivity ( $\mathbf{b}_n$ ), and area ( $A_n$ ) are defined for the  $n^{\text{th}}$  region. The equivalent circuit model is shown on the right with the arrows indicating sources or sinks of heat flux.  $Q_{TI}$  refers to



**Figure 6.6** One-dimensional model and boundary conditions. Electrical conductivity ( $\sigma$ ), thermal conductivity ( $\kappa$ ), and area ( $A$ ), are defined in each region. The equivalent circuit model is shown on the right with the arrows indicating sources or sinks of heat flux.  $Q_{TI}$  refers to thermionic heating/cooling,  $Q_{TE}$  to thermoelectric cooling, and  $Q_C$  to heat generation by contact resistance.

thermionic heating/cooling,  $Q_{TE}$  to thermoelectric cooling (metal-semiconductor interface), and  $Q_C$  to heat generation by contact resistance. From circuit analysis, an expression can be found for the temperature at the cold side of the device (between regions 1 & 2). If the thermal resistance of the wire ( $R_w^{th}$ ) is much less than the sum of the cooler and substrate thermal resistance, it can be neglected to simplify the analysis. Likewise, the electrical resistance of the substrate can be ignored compared to the other regions. The resulting expression is:

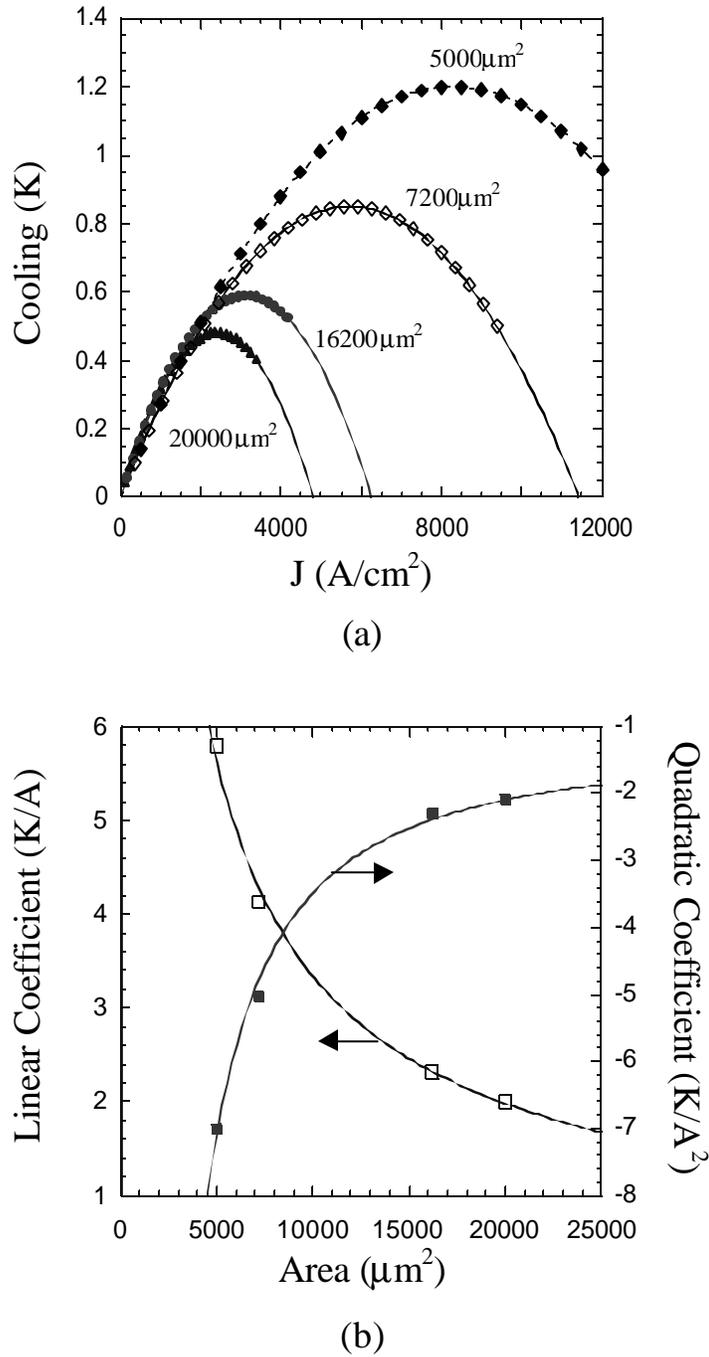
$$\Delta T = \{(Q_{TI} + Q_{TE})(R_d^{th} + R_{sub}^{th}) - Q_{TI} R_{sub}^{th}\} - \left\{ \left( \frac{1}{2} R_{Au} + R_C \right) (R_d^{th} + R_{sub}^{th}) \right\} I^2 \quad (6.1)$$

where  $R_d^{th}$  and  $R_{sub}^{th}$  are the cooler and substrate thermal resistances, and  $R_{Au}$  and  $R_C$  are the gold wire and contact electrical resistances respectively.  $Q_{TE}$  and  $Q_{TI}$

comprise the linear term ( $I$  is located inside the expressions) as mentioned above. Likewise, the second term containing the electrical resistances is proportional to the square of current. Each term is also scaled by a factor that describes the thermal resistances between the heat sources and sinks. This equation is similar in form to the expression for conventional thermoelectrics (Equation A.1, Appendix A), but includes all of the important non-ideal parameters for thin film coolers such as contact resistance, wire bond heat load, and substrate thermal resistance.

### 6.2.1 Cooling Vs. Size

Most of the terms in Equation 6.1 are area dependent, and so studying the cooling dependence on device size provides much information about the behavior of the device. The measured cooling versus current density for several device areas is shown in Figure 6.7a for the low-barrier InGaAs/InGaAsP structure described in Chapter 3 (Section 3.2). At low current densities, all the devices operate nearly identically as expected. As the current is increased, the area dependent non-ideal heating contributions become apparent. The smallest size device ( $5000\mu\text{m}^2$ ) cools best because it requires less current to reach a given current density, and the rollover occurs later. Referencing Equation 6.1, the curves in Figure 6.7a can be fitted with a second order polynomial and the corresponding linear and quadratic coefficients extracted. Figure 6.7b plots these coefficients versus area. Using Equation 6.1 and the known material properties, the area dependence can be modeled and the device



**Figure 6.7** (a) Cooling versus current density for several device sizes and (b) the corresponding linear (cooling) and quadratic (heating) coefficients from a second order polynomial fit as in Equation 6.1. The points are the experimental values, and the curves are simulated from Equation 6.1. Measurements were performed with a heat sink temperature of 300K.

operation understood. The term  $R_{Au}$  is area independent, the terms  $R_d^{th}$  and  $R_C$  are proportional to  $1/\text{area}$ , and the term  $R_{sub}^{th}$  is proportional to  $1/\sqrt{\text{area}}$ . Thus the following proportionalities result:

$$linear \propto \frac{1}{A^{1/2}} + \frac{1}{A} \quad (6.2)$$

$$quadratic \propto \frac{1}{A^{1/2}} + \frac{1}{A} + \frac{1}{A^{3/2}} + \frac{1}{A^2} \quad (6.3)$$

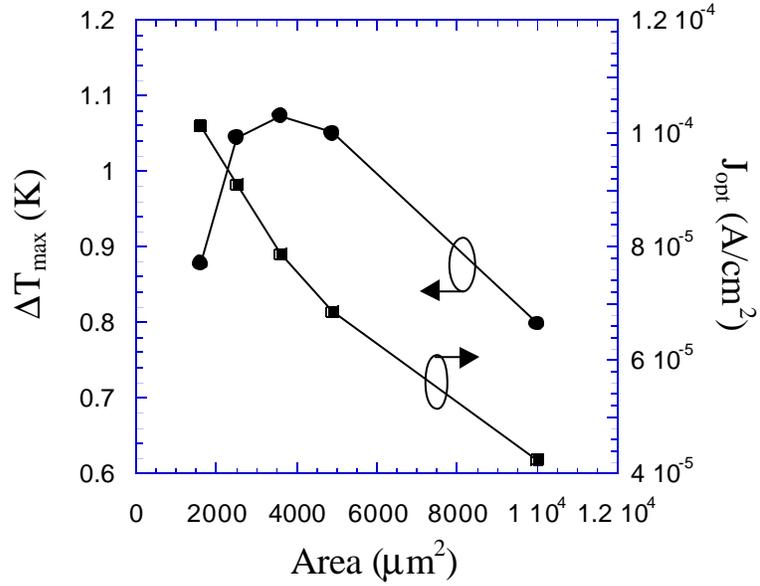
The values assumed in the curve fits of Figure 6.7b are listed below in Table 6.1. Fitting the linear coefficient is fairly straightforward if accurate values of  $Q_{TI}$  and  $Q_{TE}$  can be determined. In this analysis,  $Q_{TE}$  was first estimated from theoretical values as well as Seebeck measurements on InGaAs test structures.  $Q_{TI}$  was then adjusted to account for the additional cooling necessary to fit the experimental results. The need for an additional cooling term is evidence that thermionic cooling is indeed taking place, and in this case it accounts for 78% of the total cooling. The thermal and electrical resistance values used considered full 3D self-consistent electrical and thermal simulations where appropriate (the 3D simulations will be discussed in Section 6.4). Using a power fit, the area dependence was  $1/A^{0.75}$ , indicating that both terms of Equation 6.2 are important. The more challenging task is the curve fit for the many terms of the quadratic coefficient. For this, estimated values of resistance were used for all terms except  $R_{sub}^{th}$ , which was used as a fitting coefficient. The value chosen must be carefully considered to satisfy both the linear and quadratic expressions. An adequate curve fit for the quadratic term necessitated

all of the terms of Equation 6.3, and neglecting any one term would compromise a good fit. Area dependence with a power fit was  $1/A^{0.9}$ . The encouraging conclusion from this, is that an improvement in any one of the non-ideal effects should improve the cooling result. While the approximations made here helped to gain an intuitive feeling for the device operation, a complete analysis should include all relevant parameters. A more exhaustive model and device simulation are presented later.

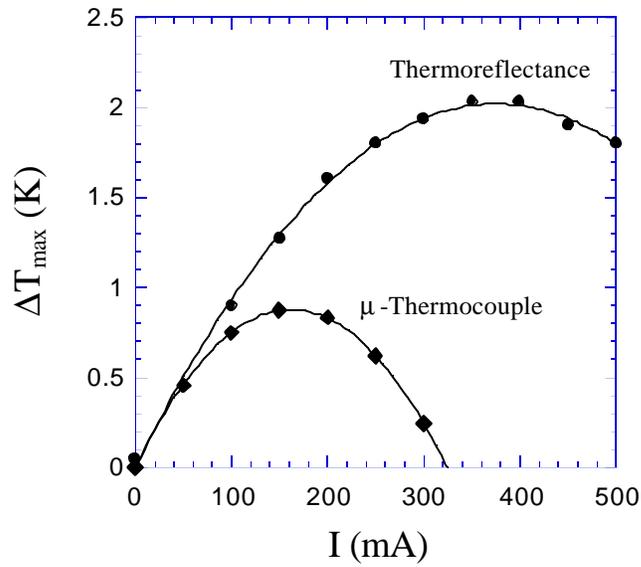
**Table 6.1** Important material parameters and calculated resistance values for the curve fits in Figure 6.7b. The resistances are calculated from equations of the form  $L / \beta \cdot A$ , except for the substrate thermal resistance which was used as a fitting parameter.

<i>Parameter</i>	<i>Description</i>	<i>Value [units]</i>
$L_w$	Au wire length	600 [ $\mu\text{m}$ ]
$A_w$	Au wire cross-sectional area	507 [ $\mu\text{m}^2$ ]
$\rho_w$	Au wire resistivity	0.0227 [ $\Omega \mu\text{m}$ ]
$\rho_c$	Contact resistivity	50 [ $\Omega \mu\text{m}^2$ ]
$L_c$	Cooler thickness	1 [ $\mu\text{m}$ ]
$\beta_c$	Cooler thermal conductivity	$4 \times 10^{-6}$ [ $\text{W}/\mu\text{m}\cdot\text{K}$ ]
$\beta_s$	Substrate thermal conductivity	$68 \times 10^{-6}$ [ $\text{W}/\mu\text{m}\cdot\text{K}$ ]
$Q_{\text{TI}} / I$	Thermionic voltage	0.053 [V]
$Q_{\text{TE}} / I$	Thermoelectric voltage	0.015 [V]
$R_{\text{Au}}$	Au wire electrical resistance	0.027 [ $\Omega$ ]
$R_c$	Contact resistance	50/A [ $\Omega \mu\text{m}^2$ ]
$R_d^{\text{th}}$	Cooler thermal resistance	$2 \times 10^5 / A$ [ $\text{K}\mu\text{m}^2/\text{W}$ ]
$R_{\text{sub}}^{\text{th}}$	Substrate thermal resistance	$9632 / \sqrt{A}$ [ $\text{K}\mu\text{m}/\text{W}$ ]

For some devices, an optimum device size is observed as in Figure 6.8a. Since Equation 6.1 only predicts improved cooling for smaller devices (at least over the range of device sizes considered here), some other explanation must be found. The



(a)



(b)

**Figure 6.8** (a) Maximum cooling and corresponding current versus device area showing an optimum device size in  $\Delta T$  due to the heat load from the thermocouple. (b) Increased cooling with the thermocouple heat load removed and the thermoreflectance measurement used ( $1600 \mu\text{m}^2$  size).

first possibility is that for the smallest devices, the wire bond is no longer optimized and heat conduction through the electrical connection becomes important. This can be corrected however by optimizing the wire bond for each size device. The other likely influence is in the measurement itself. For small devices, the thermocouple becomes much larger than the cooler and presents a considerable heat load. The effect of the thermocouple for small devices has been verified with the thermoreflectance measurement, which shows that the smaller devices do still produce larger cooling as shown in Figure 6.8b.

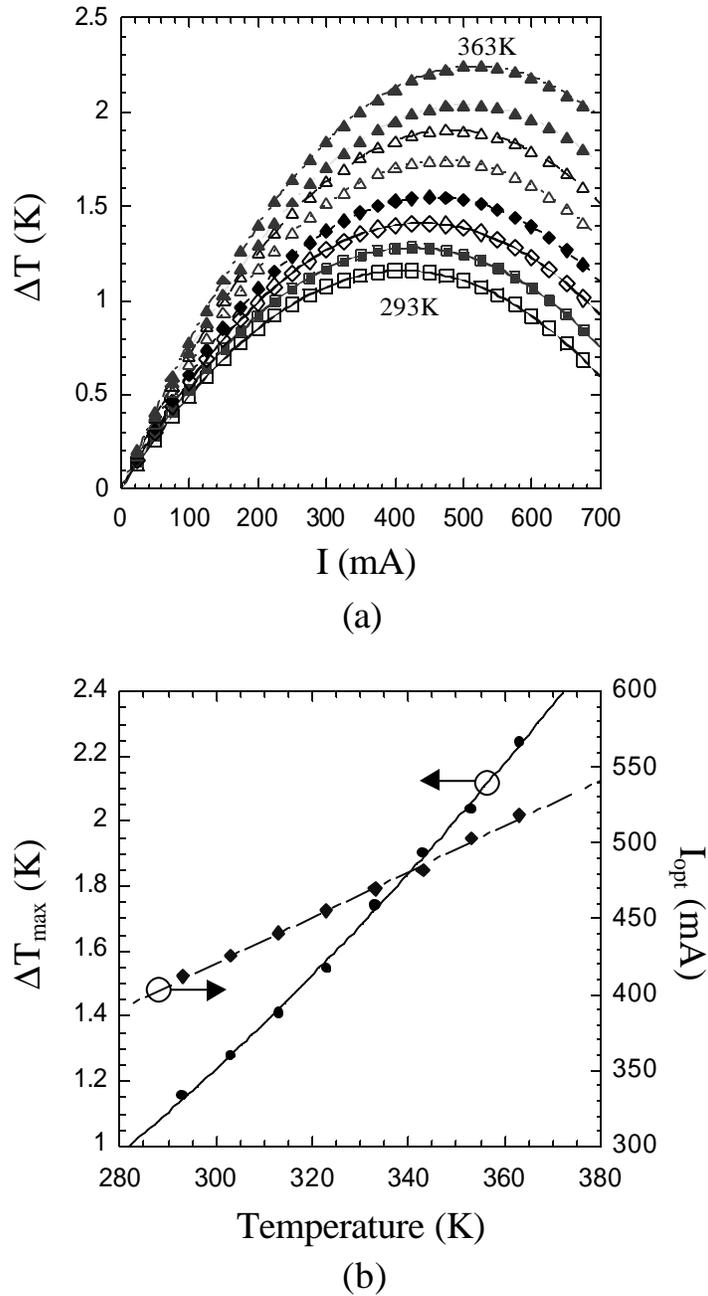
### 6.2.2 Cooling Vs. Ambient Temperature

Ideally the height of the heterobarrier and the Fermi level are engineered to be optimum for a given operating temperature. All of the structures examined were designed for room temperature operation. The cooling behavior was examined for various heat sink temperatures to determine the effects. Figure 6.9 shows the cooling versus current bias at different temperatures for a size  $5000 \mu\text{m}^2$  cooler. The observed trend is increased cooling at elevated operating temperatures. The origin of the temperature dependence stems from the change in material properties (thermal and electrical conductivity) and in the thermionic and thermoelectric cooling mechanisms. Borrowing from the analogous case of conventional thermoelectrics, the maximum cooling and optimum current can be expressed as [9],

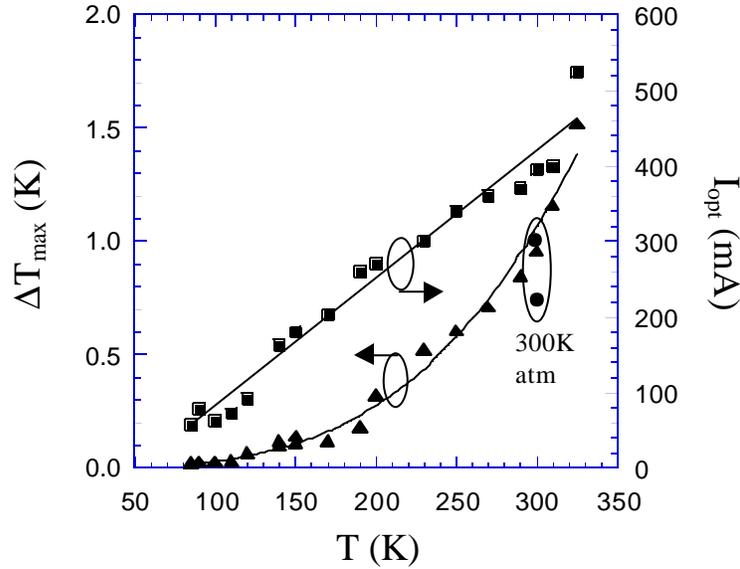
$$\Delta T_{\max} = \frac{1}{2} \frac{(\Phi_B + 2k_B T/e)^2 \mathbf{s}}{\mathbf{b}} \quad (6.4)$$

$$I_{opt} = \frac{\Phi_B + 2k_B T/e}{R} \quad (6.5)$$

where  $(\Phi_B + 2k_B T/e)$  was used in Chapter 2 as an approximation for the thermionic effect in the limit of Boltzmann statistics,  $\mathbf{s}$  and  $\mathbf{b}$  are the electrical and thermal conductivity respectively, and  $R$  is the electrical resistance. Over the temperature range of interest, the effective cooling is approximately  $\propto T$  and thermal conductivity  $\propto T^{-1.4}$  [10]. The temperature dependence of electrical conductivity is determined by the mobility which is approximately constant over these temperature values since it is mostly dominated by impurity scattering. From Equations 6.4 & 6.5, the maximum cooling and optimum current are roughly proportional to  $(T^{1.4} + T^{2.4} + T^{3.4})$  and  $T$  respectively. The data points in Figure 6.9b fit very well to these corresponding powers. Numerically, the temperature dependence of  $I_{opt}$  is easier to analyze since it is a simple linear equation. Comparing the fit,  $I_{opt} = 380 + 1.51T$ , with Equation 6.5, a resistance of  $0.114 \Omega$  and a barrier height of  $43 \text{ meV}$  result. Both values are within a factor of two of the expected values. For an analysis over a wider temperature range, the dependence of the electrical conductivity may have to be estimated, as well as a more accurate model of the effective cooling using Fermi-Dirac statistics.



**Figure 6.9** (a) Cooling versus current bias for heat sink temperatures of 293-363K in 10K increments. (b) Corresponding maximum cooling (solid) and optimum current (dashed) versus heat sink temperature. The points are the experimental values and the curves are the theoretical curve fits,  $\Delta T_{\max} \propto T^{1.4} + T^{2.4} + T^{3.4}$ ,  $I_{\text{opt}} \propto T$ .  $\Delta T$  is measured with respect to the heat sink temperature.



**Figure 6.10** Maximum cooling and optimum current versus heat sink temperature for a 18/7nm InGaAs/InP superlattice design. The measurements were performed in a liquid-N<sub>2</sub> cooled low temperature micro probe system. The chamber pressure was approximately  $10^{-4}$  to  $10^{-5}$  torr. Two measurements of  $\Delta T_{max}$  at room temperature and pressure are shown for reference.

In some cases, such as certain IR lasers or photodetectors, cooling at very low temperatures with solid-state refrigeration is desired. Conventional thermoelectrics are forced to work with the temperature-dependent bulk cooling-properties of separate materials, but thermionic cooling in heterostructures can be designed for a broader range of temperatures by tailoring the barrier height and superlattice to account for the change in the carrier distribution over temperature. While none of the structures investigated in this work were designed for low temperature operation, it is still interesting to observe the behavior for these conditions. Figure 6.10 shows  $\Delta T_{max}$  and  $I_{opt}$  versus heat sink temperature for an 18/7nm InGaAs/InP superlattice. The measurements were performed in a liquid-N<sub>2</sub> cooled low temperature micro-

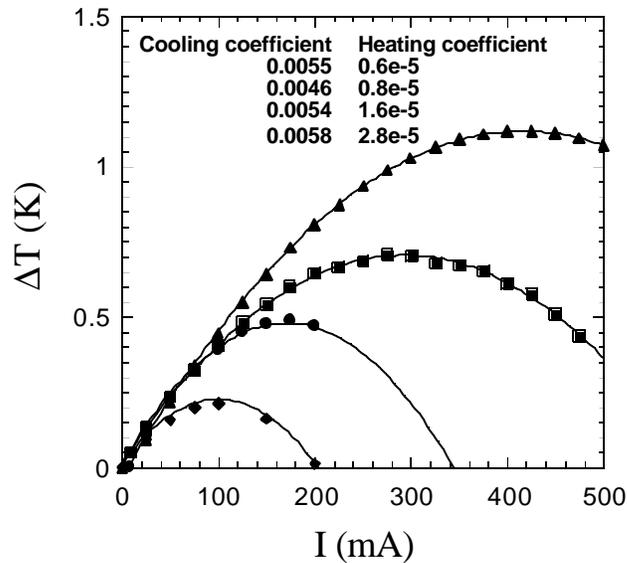
probe system with a chamber pressure of approximately  $10^{-4}$  to  $10^{-5}$  torr. Even over this extended temperature range, the data still fits very well to the expressions derived above. Two measurements of  $DT_{max}$  at room temperature and pressure are also shown for reference. There was an average increase of 15-20% in  $DT_{max}$  when testing under vacuum, that is attributed to heat convection through the air.

### 6.2.3 Cooling Vs. Packaging

The packaging has proven to be an important factor to optimize as mentioned in Chapter 5. The addition of a package between the substrate and heat sink adds another thermal barrier for heat to pass through. Improvements in reducing this added thermal resistance by using silicon or copper packages and by optimizing the length of the wire bond have resulted in a maximum cooling increase of around 300% in some devices. Ultimately, when the thin film coolers are integrated with real devices or are packaged in a conventional TE configuration (*n*- and *p*-type legs electrically in series, thermally in parallel — for example, see Ref. 9), the issue of wire bonding will be less of a concern.

Figure 6.11 shows the increase in InGaAs/InGaAsP thermionic cooler performance for four variations in packages. In each successive package, the cooling (linear) coefficient remains nearly constant while the heating (quadratic) coefficient is reduced. The reduction in the heating coefficient can be explained from a combination of lower contact resistance, wire bond length, and package thermal

resistance. According to Equation 6.1, the former two only effect the heating coefficient, but the latter quantity should also reduce the linear coefficient. Since this remains relatively constant, it suggests that either  $R_d^{th} \gg R_{sub}^{th}$  which is not the case, or that  $Q_{TI} > Q_{TE}$ . The best cooling shown in Figure 6.11 is for a package made from a 350- $\mu\text{m}$ -thick Si-wafer and using a wire bond length of 250  $\mu\text{m}$ , corresponding to the second package generation described in Chapter 5. While the package is near to being fully-optimized for single-stage coolers, estimated reduction in cooling due to the wire bond is estimated to be as high as 50%. Combined  $p$ - and  $n$ -type structures should be used to eliminate this loss.

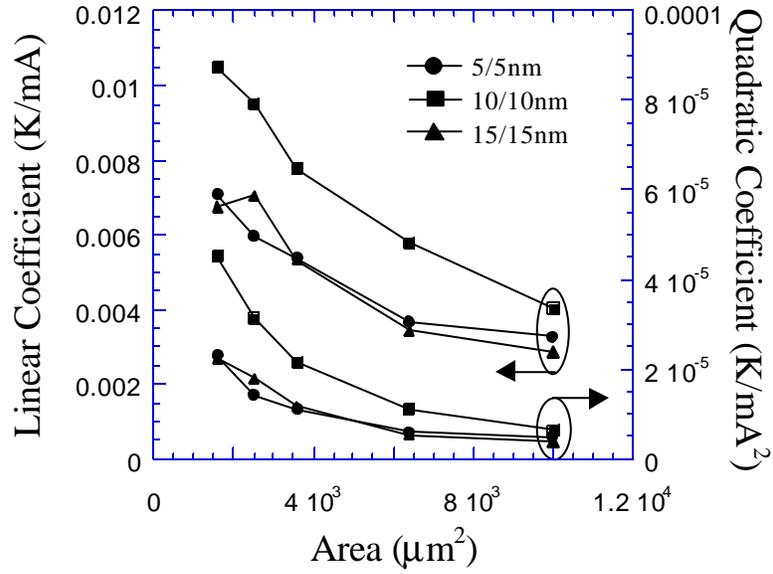


**Figure 6.11** Measured cooling for a 1  $\mu\text{m}$  InGaAs/InGaAsP thermionic cooler with various packages. The cooling (linear) and heating (quadratic) coefficients correspond to a second order polynomial fit. The cooling coefficients remain nearly constant while the heating coefficients are reduced. All temperatures are relative to the value at zero current with a heat sink temperature of 20  $^{\circ}\text{C}$ .

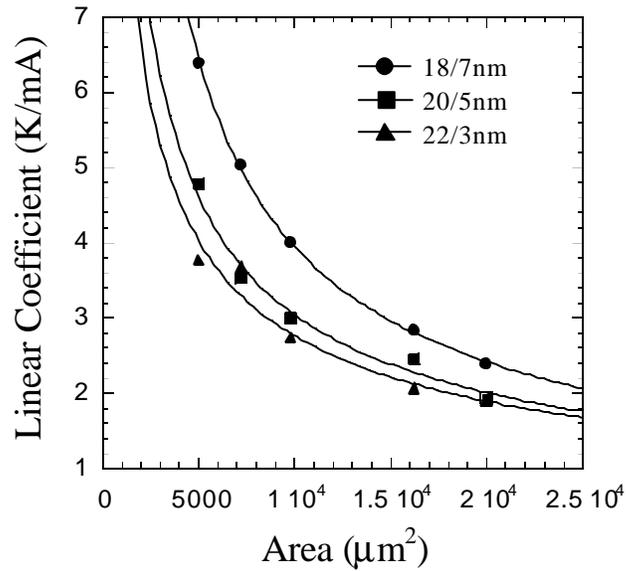
#### 6.2.4 Cooling Vs. Superlattice Design

With the extrinsic parameters of geometry, temperature, and packaging having been discussed, the intrinsic parameters of heterostructure design are now examined. The ultimate goal is of course to maximize the  $ZT$  of the effective material. Unfortunately, the inherent cooling properties of the thin film structure are masked by the external effects of the substrate and contacts.

One fundamental effect that is difficult to distinguish is the bulk thermoelectric effect between dissimilar materials, especially at the metal-InGaAs interface. This is because the thermoelectric effects have the same linear dependence on current as thermionic emission cooling, and occur very near each other in the device. When reviewing measurements, the question is raised of how much cooling is due to each effect? One straightforward approach that attempts to answer this question is a simple  $A-B$  comparison. Structures with and without barriers for thermionic emission are tested, and the results compared. For example, in the analysis that included Table 6.1 and Figure 6.7, the thermoelectric Seebeck voltage was estimated to contribute roughly 30% to the overall cooling term. The ratio of thermionic to thermoelectric cooling can vary dramatically from structure to structure, and in some cases the latter is believed to be the dominant effect. The  $A-B$  comparison is not an accurate method for quantifying the cooling effects since the very act of removing the heterobarriers will also alter the transport properties that define the electrical and



**Figure 6.12** Linear and Quadratic coefficients versus area for different periods of a 1- $\mu\text{m}$ -thick InGaAs/InGaAsP superlattice. Both coefficients are higher for the 10/10nm period indicating a lower superlattice effective thermal-conductivity.



**Figure 6.13** Linear coefficients versus area for different periods of a 2- $\mu\text{m}$ -thick InGaAs/InP superlattice. The coefficients are larger for the periods containing more InP.

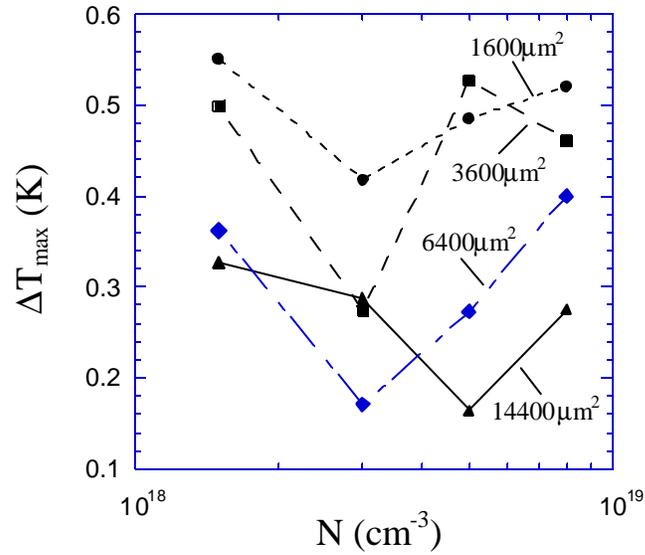
thermal conductivities. Other analyses that indicate the magnitude of the two cooling effects are discussed later.

Arguably the two most controllable parameters to change in the heterobarriers are the superlattice period and the doping or Fermi level. A series of structures were tested for both the low barrier (InGaAsP-barriers) and high barrier (InP-barriers) thermionic coolers, where either the period or doping was varied while the other was kept constant. Figure 6.12 plots the measured linear and quadratic coefficients versus device area for three different superlattice periods of InGaAs/InGaAsP ( $1.5 \times 10^{18} \text{ cm}^{-3}/\text{nid}$ ). In each set of coefficients, the 5/5nm and 15/15nm period devices have nearly the same magnitudes while the 10/10nm period device has both larger linear and quadratic values. An increase in both coefficients suggests that the effective thermal conductivity of the 10/10nm superlattice is lower. This can be seen from Equation 6.1 where  $R_{sub}^{th}$  is constant. Figure 6.13 shows a similar analysis for various superlattices of InGaAs/InP ( $5 \times 10^{18} \text{ cm}^{-3}/\text{nid}$ ). The quadratic term was not compared because of the different contact region doping in each structure. An increase in the linear coefficient is observed for periods containing more InP. This is also most likely explained by the lower thermal conductivity of the 18/7nm period superlattice (see Chapter 4, Figure 4.2). Another possibility is that the effective Seebeck coefficient is larger for the wider InP-barriers. The degrading effect of carrier-tunneling on cooling for narrow high-barrier structures was discussed in Chapter 2.

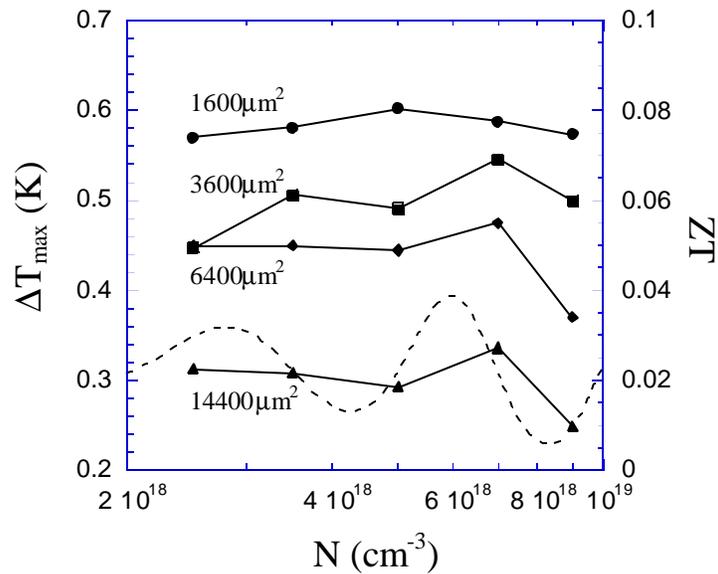
In Chapter 2, theoretical calculations of  $ZT$  versus doping for various heterobarrier designs were presented. The results showed that the added asymmetry supplied by the barriers caused a simultaneous increase in  $ZT$  and shift of optimum doping to higher levels. Since the maximum cooling can be related to  $ZT$  through:

$$\Delta T_{\max} = \frac{1}{2} ZT_{\text{cold}}^2 \quad (6.6)$$

measuring  $\mathbf{DT}_{\max}$  versus doping should ideally produce a similar experimental result. This is not entirely accurate in our case due to the extra non-ideal effects, but the same qualitative trends should be present. Figure 6.14 shows  $\mathbf{DT}_{\max}$  versus doping for several different device sizes of a 10/30nm InGaAs/InGaAsP structure. The result is inconclusive as it does not show any consistent trend. However, it also does not show the monotonic decrease in  $\mathbf{DT}_{\max}$  that would be present for a pure thermoelectric device over these doping concentrations. A similar plot is given in Figure 6.15 for a 22/3nm InGaAs/InP structure, where the theoretical simulation of  $ZT$  from Chapter 2 (Figure 2.11) is also shown. In this case, there is qualitative agreement between the experimental results and predicted theoretical behavior indicating that thermionic effects are present. The expected oscillatory behavior of cooling versus doping is diminished in the experimental results due to non-ideal effects and the bulk thermoelectric effect (metal-semiconductor contact) which should account for a majority of the total cooling in this structure. Ideally, with out the non-ideal effects, the maximum cooling would fluctuate between 3.3K and 7.8K



**Figure 6.14** Maximum cooling versus doping for a 1- $\mu\text{m}$ -thick 10/30nm InGaAs/InGaAsP superlattice.



**Figure 6.15** Maximum cooling versus doping (solid lines) for a 2- $\mu\text{m}$ -thick 22/3nm InGaAs/InP superlattice. The theoretical ZT is shown by the dashed line and is related to  $\Delta T_{\text{max}}$  through Equation 6.6. A similar qualitative behavior is evident indicating thermionic cooling effects are present.

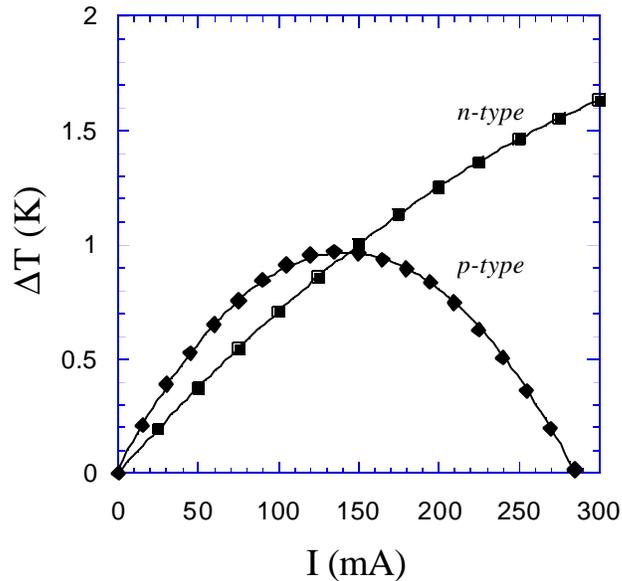
with 2.4K and 1.9K coming from the pure thermoelectric contribution respectively. Sadly, the disastrous effects of quantum transmission probability were realized after the design of this structure. A maximum cooling of up to 28K should be possible for thicker barriers as described in Chapter 2.

Significant cooling beyond bulk InGaAs (~0.3K measured) for very high barrier devices (InAlAs-barriers) has not been observed. Much more work characterizing effects of high doping in these structures is needed. Sb-based samples had problems with the contact layer resulting in very high contact resistances and low maximum cooling differentials of 0.3K [11]. Due to a lack of material-availability, no further investigation of cooling in these structures could be completed.

### 6.2.5 *N- and P-type Coolers*

Through the use of both *n*- and *p*-type thermionic emission coolers connected electrically in series and thermally in parallel, we can avoid making external electrical contacts to the cold side of the cooler and provide larger cooling capacities at smaller operating currents. It is important for these multi-element coolers that the *n*- and *p*- type elements work together under similar bias conditions. This simplifies the integration process and avoids any complicated module geometries. Figure 6.16 shows measured cooling versus current bias for a *n*- and *p*-type device at a heat sink temperature of 70 °C. The *n*-type device was 50×100 μm<sup>2</sup> while the *p*-type device was 100×100μm<sup>2</sup> in size. Both types of devices are still currently limited by the

non-ideal effects of contact resistance, wire bond heating and conduction, and substrate thermal resistance. The *p*-type device in Figure 6.16 has a much larger heating component as can be seen from the faster roll-over of the cooling, and is attributed to a higher contact resistance. The material used in the contact layer of each cooler was InGaAs, and the *p*-type InGaAs was found to have a significantly larger contact resistance as discussed in Chapter 5. The *p*-type device also has a higher cooling component implicit by the steeper slope at low currents. This is due to the larger Seebeck coefficient mentioned in Chapter 4. Even with the differing cooling and heating components, the two types of devices can be made to have the same optimum current values by adjusting the area of the cooler for the optimum current density.

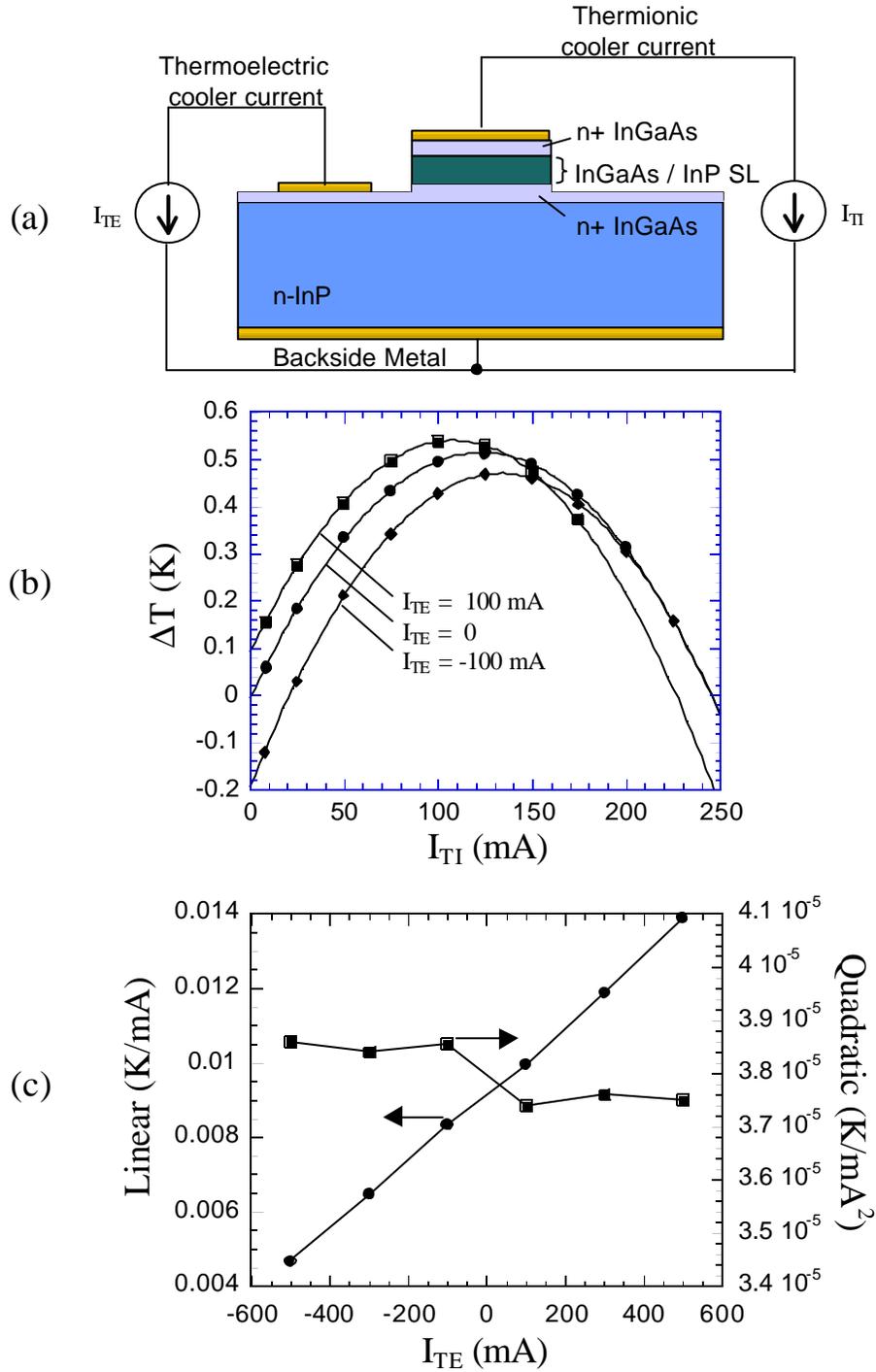


**Figure 6.16** Measured cooling versus current bias for a *p*-type ( $100 \times 100 \mu\text{m}^2$ ) and *n*-type cooler ( $50 \times 100 \mu\text{m}^2$ ) at a heat sink temperature of  $70^\circ\text{C}$ .

### 6.3 Two-Stage TITE Coolers

A simpler way of effectively reducing the limitations of substrate thermal resistance is to use the substrate itself as a thermoelectric cooler. A similar concept has been successfully employed in the tuning of in-plane and vertical cavity lasers by changing the current through a metal-substrate contact [12,13]. In this case, a new type of cooler structure is formed from both thermionic and thermoelectric (TITE) coolers in a multistage, three-terminal configuration.

An example of this structure is illustrated in Figure 6.17a where the mesa defines the thermionic cooler section and the remainder is the thermoelectric cooler section. The  $\mu$ -thermocouple method was used to measure the cooling on top of the mesa as a function of thermionic ( $I_{TI}$ ) and thermoelectric ( $I_{TE}$ ) currents. The temperature on top of the mesa  $T(I_{TE})$  was first measured as a function of  $I_{TE}$  with  $I_{TI}$  set to zero. Next  $I_{TE}$  was set to zero, and the temperature  $T(I_{TI})$  measured as a function of  $I_{TI}$ . Then  $I_{TE}$  was set to various constant values, and the measurement repeated as a function of  $I_{TI}$  resulting in a temperature on top of the mesa that is a function of both currents,  $T(I_{TI}, I_{TE})$ . The cooling seen on top of the mesa from the thermoelectric effect at the bottom contact was much smaller ( $\sim 0.1^\circ\text{C}$ ) than the cooling from  $I_{TI}$ . This is in part due to the fact that the thermoelectric cooling action is occurring further away from the top of the mesa than that of the thermionic cooling, and in part due to the inherently smaller thermoelectric cooling properties of InGaAs and InP compared to the extra thermionic effects. Intuitively when both currents are biasing each section



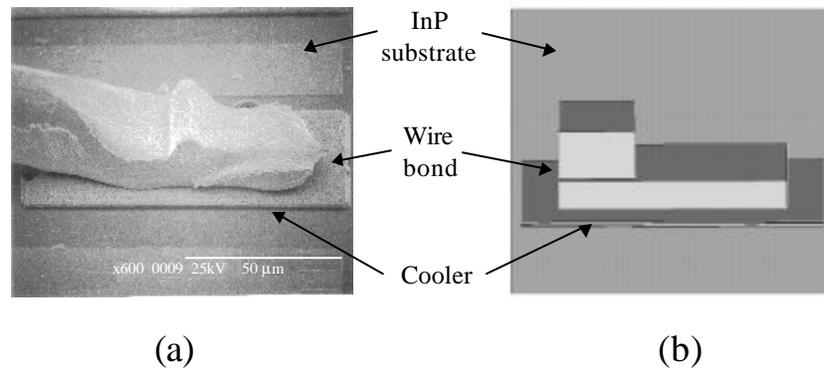
**Figure 6.17** (a) TITE device structure and geometry. (b) Cooling versus thermionic cooler current for three different thermoelectric currents, and (c) the corresponding linear and quadratic coefficients versus thermoelectric current.

of the multistage cooler, it is expected that the resulting temperature,  $T(I_{TI}, I_{TE})$ , would be the sum of the two independent measurements,  $T(I_{TI}) + T(I_{TE})$ , however this is not the case. Figure 6.17b illustrates this point graphically by plotting the cooling on top of the thermionic cooler for constant thermoelectric currents of 100 mA, 0 mA, and -100 mA. If superposition applied, then the three curves would look identical with only a vertical shift due to the constant thermoelectric current. This is obviously not the case as any two curves cross each other at some observable point. Figure 6.17c plots the corresponding linear and quadratic fitting coefficients versus  $I_{TE}$ , and shows that while the heating coefficient remains approximately constant, the linear coefficient is changing linearly with thermoelectric current. Therefore, the constant thermoelectric current not only adds or subtracts a constant amount of cooling, but it also changes the magnitude of the overall cooling term. The reason for this  $I_{TE}$ -dependent linear coefficient is due to both  $I_{TI}$  and  $I_{TE}$  superimposing in the substrate region. If the substrate region has a heating coefficient  $H_{sub}$ , then the quadratic term in that region is multiplied by the square of the sum of the currents flowing through it,  $H_{sub}(I_{TI} + I_{TE})^2$ . Expanding this expression yields the normal heating terms,  $H_{sub}I_{TI}^2$ ,  $H_{sub}I_{TE}^2$ , and a cross term  $2H_{sub}I_{TE}I_{TI}$ . This cross term can be used to further enhance the overall cooling of this two-stage device. From the slope of the linear coefficient in Figure 6.17c,  $H_{sub}$  is measured to be  $4.57 \times 10^{-6}$  K/mA<sup>2</sup>, which corresponds to only 12% of the total quadratic coefficient measured. This result is expected since it is believed that most of the heating is caused by the contact

resistance of the metal-semiconductor contacts and from the current carrying wire bonds. An interesting result of this cross term is that it originates from the heating effects in the substrate. Therefore even with no additional cooling from the thermoelectric stage, there exist optimum currents  $I_{TI}$  and  $I_{TE}$  for which the cooling is maximized.

#### **6.4 Device Simulation**

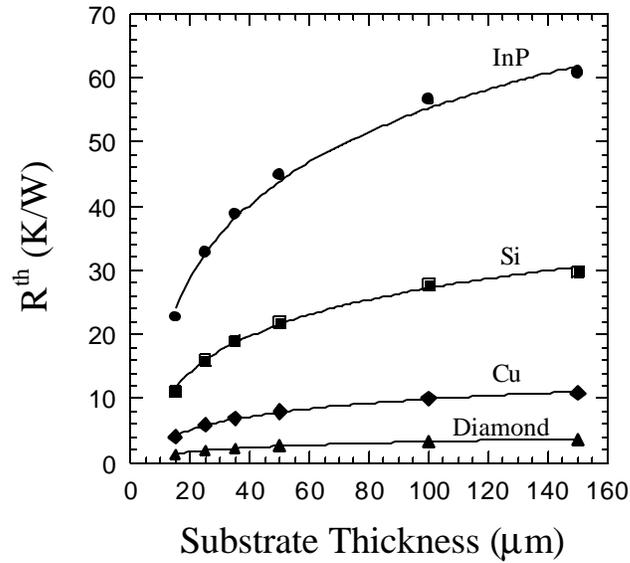
In the previous analyses of experimental results, an approximate expression (Equation 6.1) was used to understand the device behavior. In many cases this simple model made use of values calculated by much more complex three-dimensional simulations. This section first looks at these finite-element 3-D simulations [14] that self-consistently solve for the electrical and thermal current flow. Figure 6.18 shows an SEM photo next to the simulated structure. The 3-D analysis is necessary to accurately model the electrical and thermal spreading resistance, however simulation of 3-D structures is somewhat slow. The 3-D electrical and thermal resistances can be determined for various geometries and used in an effective 1-D model to obtain faster results when several parameters are to be varied. The complete model is much more elaborate than the previous one, and can be used to accurately fit experimental results over wide variations in parameters. Finally, reliable predictions of improved performance for optimized structures can be made.



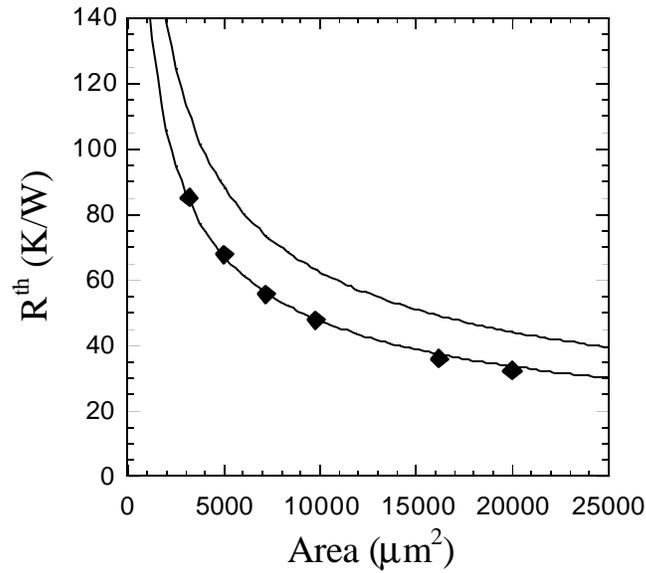
**Figure 6.18** (a) Scanning electron micrograph of a thin-film thermionic cooler and (b) the simulated structure. The cooler mesa is 1.4 μm high, and the uppermost wire bond length is scaled to reduce the element count in the mesh.

#### 6.4.1 Substrate Thermal Resistance

The most evident non-ideal effect for thin film coolers is the substrate and package thermal resistance. Qualitatively speaking, if the distance between the cooling and heating regions is several orders of magnitude smaller than the distance between the heating and heat sink regions, most of the heat will flow back to the cold side of the device if the thermal conductivities of the thin film and substrate are comparable. Figure 6.19a shows simulation results of substrate thermal resistance versus thickness for various substrate materials. The simulation is performed assuming a rectangular etched-mesa ( $5000 \mu\text{m}^2$ ) thin-film cooler on a semi-infinite plane substrate. The boundary conditions imposed assume the sides and top of the substrate to be adiabatic and the bottom isothermal. A uniform heat load on top of the mesa is assumed. The relatively good fit to a  $\ln(x)$  function is indicative of the thermal spreading in two- and three-dimensional heat flow [15, 16]. Below 15 μm,



(a)



(b)

**Figure 6.19** (a) Thermal resistance versus substrate thickness for a device area of  $5000 \mu\text{m}^2$  on various substrates: InP ( $\beta=71 \text{ W/m}\cdot\text{K}$ ), Si ( $\beta=145 \text{ W/m}\cdot\text{K}$ ), Cu ( $\beta=398 \text{ W/m}\cdot\text{K}$ ), and CVD Diamond ( $\beta=1200 \text{ W/m}\cdot\text{K}$ ). The points correspond to 3D simulation results, and the solid curves are the theoretical  $a_i \cdot \log(x) + b_i$  curve fits. (b) Thermal resistance versus device area. The points are simulation results assuming a  $125 \mu\text{m}$  thick InP substrate and the upper solid curve is the theoretical plot assuming the substrate is an entire half-space.

the heat flow becomes dominantly one-dimensional and the thermal resistance scales linearly with substrate thickness. The logarithmic fitting function of the thermal resistance and the corresponding coefficients can be given as,

$$R_{thermal}(h) = a_i \ln(h) + b_i \quad (6.7a)$$

$$a_i = \frac{1167}{b_i [W / mK]} \quad ; \quad b_i = \frac{-1445}{b_i [W / mK]} \quad (6.7b)$$

where  $R_{thermal}$  has units of [K/W],  $h$  is the substrate thickness in microns, and  $a_i$  &  $b_i$  are the fitting coefficients corresponding to the thermal conductivity of the substrate ( $b_i$ ).

Clearly it is beneficial to use substrates with high thermal conductivity and a minimum thickness. However, thin film coolers that are grown on typical substrate materials (InP, Si, etc.) can be lapped only by a limited amount before the material begins to warp and become severely fragile. This warping occurs with InP substrates when they are lapped below 100  $\mu\text{m}$ , which for the device size simulated corresponds to a thermal resistance of 57 K/W. Using a 1  $\mu\text{m}$  film of InGaAsP for the cooler ( $b = 3.3 \text{ W/m}\cdot\text{K}$ ) gives a thermal resistance of 61.6 K/W showing that roughly half the heat flows back to the cold side of the device.

The area of the device also affects the thermal resistance. Figure 6.19b shows simulation results of thermal resistance (points on lower curve) for various device areas assuming a 125- $\mu\text{m}$ -thick InP substrate. The upper curve represents a

theoretical expression that assumes a disk heat source on a half-space denoting a purely three-dimensional heat flow,

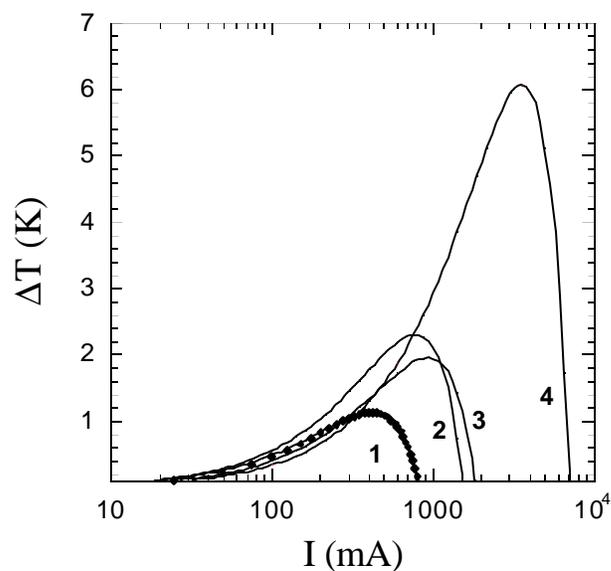
$$R_{thermal} = \frac{\sqrt{P}}{4 \mathbf{b} \sqrt{A}} \quad (6.8)$$

where  $\mathbf{b}$  is the thermal conductivity of the half space, and  $A$  is the area of the disk [15]. The simulation results are fitted with this same expression (solid line), and the resulting expression is equivalent to Equation 6.8 multiplied by a reduction factor of 0.761. As the substrate thickness is increased, the simulation results approach that of the theoretical expression.

#### 6.4.2 Complete Device Simulation

Simulation of complete 3-D device structures with all non-ideal effects included can be used to fit experimental data and determine which areas of the thin film cooler design need to be improved. These simulations model self-consistently the thermal and electrical operation. Once the simulation is in agreement with experimentally measured temperature profiles, particular non-ideal effects can be removed in succession and the dominating ones determined.

Measured cooling for a 1- $\mu\text{m}$ -thick InGaAs/InGaAsP superlattice ( $50 \times 100 \mu\text{m}^2$ ) is shown with the simulated curve in Figure 6.20 (curve 1). Both the thermionic and thermoelectric cooling effects were included in the simulation and the thermal conductivity of the superlattice was taken to be 5 W/m-K. With an accurate model of

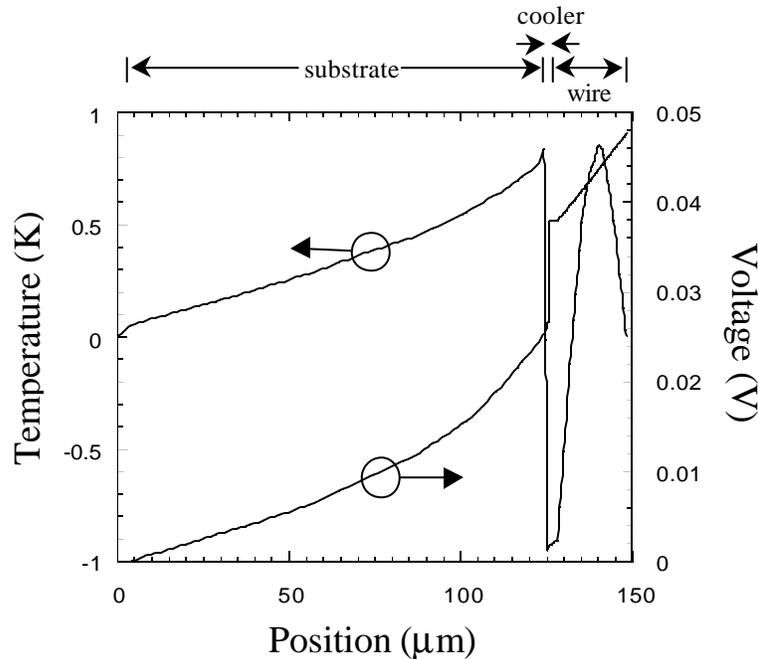


**Figure 6.20** Experimental and simulation results for a  $\mu\text{m}$  thick InGaAs/InGaAsP superlattice cooler. The points and curve 1 correspond to the simulated fit of the experimental data with all non-ideal effects. Curves 2 and 3 are the repeated simulation results when the contact resistance and substrate thermal resistance are taken away respectively. Curve 4 corresponds to both non-ideal effects removed.

the device in hand, the contact resistance was set to zero and the simulation was repeated (curve 2). The maximum cooling temperature increased from 1.14 to 2.3 K. This was repeated with the contact resistance reset to its original value and the 120- $\mu\text{m}$ -thick InP substrate replaced with a 10  $\mu\text{m}$  copper substrate resulting in a similar improvement in performance (curve 3). The simulation was then again performed with the top wire bond removed (not shown), resulting only in a very small increase in cooling. Finally, the simulation was repeated once more with both the contact resistance removed and the copper substrate resulting in a maximum cooling temperature of 6.07 K and a cooling power density of 1821  $\text{W}/\text{cm}^2$  (curve 4).

Therefore in this particular device structure, both the contact resistance and the substrate thermal resistance will need to be reduced to see substantial improvement in performance.

It is insightful to examine the temperature and voltage profiles along a path through the 3-D structure. Figure 6.21 shows simulation results following a line from the bottom of the substrate, traveling through the cooler, and continuing to the end of the wire bond. The current source is applied between the end of the wire bond and the bottom substrate plane, and an ideal heat sink is assumed at these two points. The wire bond (25 $\mu\text{m}$  diameter) was 400  $\mu\text{m}$  long, but was scaled by a factor



**Figure 6.21** Simulated temperature and voltage profiles along a path through the substrate, cooler, and wire bond. The actual wire bond length was 400  $\mu\text{m}$ , but was scaled by 20 $\times$  to reduce the number of elements in the 3-D simulation.

of twenty to reduce the number of elements in the 3-D simulation. This kind of scaling can only be done in regions that are purely 1-D, such as the long narrow Au-wire. A linear voltage drop and quadratic temperature distribution is observed along the wire bond as expected for 1-D behavior. At the cooler, a steep temperature gradient is observed across the 1- $\mu\text{m}$ -thick film indicating a large heat flux. There is also a sharp voltage drop located at the interface of the metal and semiconductor corresponding to the contact resistance which was assumed to be  $6 \times 10^{-7} \Omega \text{ cm}^2$ . This voltage drop is nearly one quarter the total voltage across the entire structure. Inside the substrate the voltage and temperature profiles can be seen to drop off non-linearly due to the three-dimensional spreading. Finally, near the bottom of the substrate there is another change in the slope due to a 4- $\mu\text{m}$ -thick Sn solder layer.

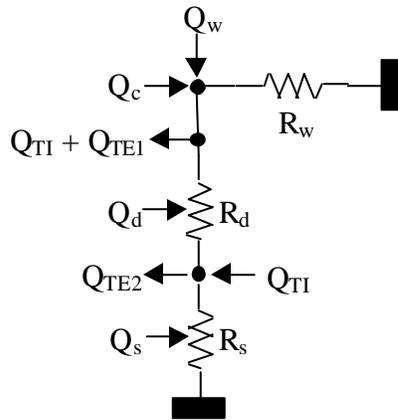
From the 3-D modeling, it is possible to extract the important thermal and electrical spreading resistances similar to Figure 6.19. Using these simulated values it becomes possible to construct an accurate 1-D model. Figure 6.22 shows the updated 1-D circuit diagram model with the appropriate cooling and heating loads, as well as boundary conditions. In each homogeneous region  $x$ , the heat flux equation can be applied,

$$\mathbf{b}_x A_x \frac{d^2 T}{dx^2} = \frac{-I^2}{\mathbf{s}_x A_x} \quad (6.9)$$

which relates the temperature gradient to the Joule heat generation where  $s_x$ ,  $b_x$ , and  $A_x$ , are the electrical conductivity, thermal conductivity, and area respectively. Taking Equation 6.9 and integrating twice with respect to position, an expression for temperature with two unknown constants results.

$$T(x) = \frac{-I^2}{2s_x b_x A_x^2} x^2 + B_x x + C_x \quad (6.10)$$

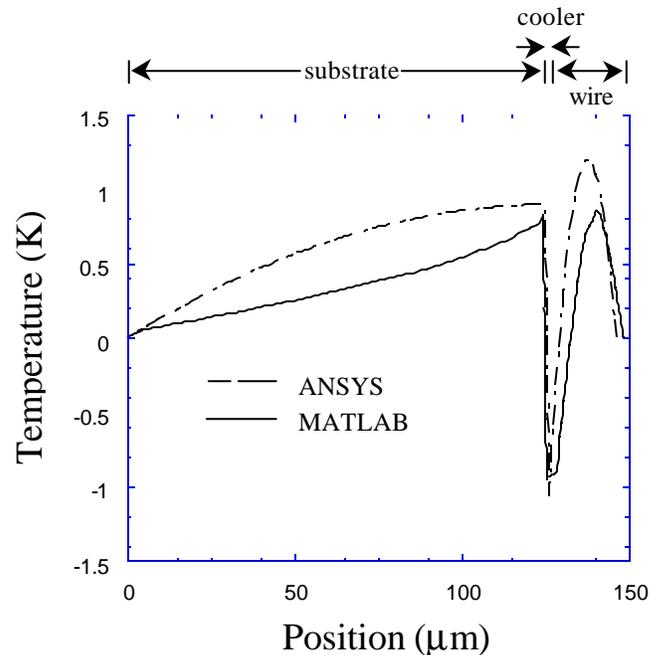
For three regions this gives a total of six unknowns. Four boundary conditions exist for the temperature since it must be continuous across all three regions. Here thermal boundary resistances are neglected. The last two boundary conditions are obtained from the discontinuity of the heat conduction ( $bA \times dT/dx$ ) by the heat generation and absorption on either side of the cooler, resulting in six boundary



**Figure 6.22** Updated 1-D model showing cooling ( $\leftarrow \bullet$ ) and heating ( $\rightarrow \bullet$ ) flux, as well as boundary conditions shown by the blocks. The resistors  $R_n$  represent both electrical and thermal resistances.  $Q_s$ ,  $Q_d$ ,  $Q_c$ , and  $Q_w$  refer to the Joule heating in the substrate, device, contact, and wire bond respectively.  $Q_{TI}$  is the thermionic heating/cooling,  $Q_{TE1}$  the thermoelectric cooling at the metal-semiconductor interface, and  $Q_{TE2}$  the thermoelectric cooling at the InGaAs-InP substrate interface. Not shown is the thermocouple heat load.

conditions and six unknowns. The solution was then manipulated and plotted in MATLAB [17].

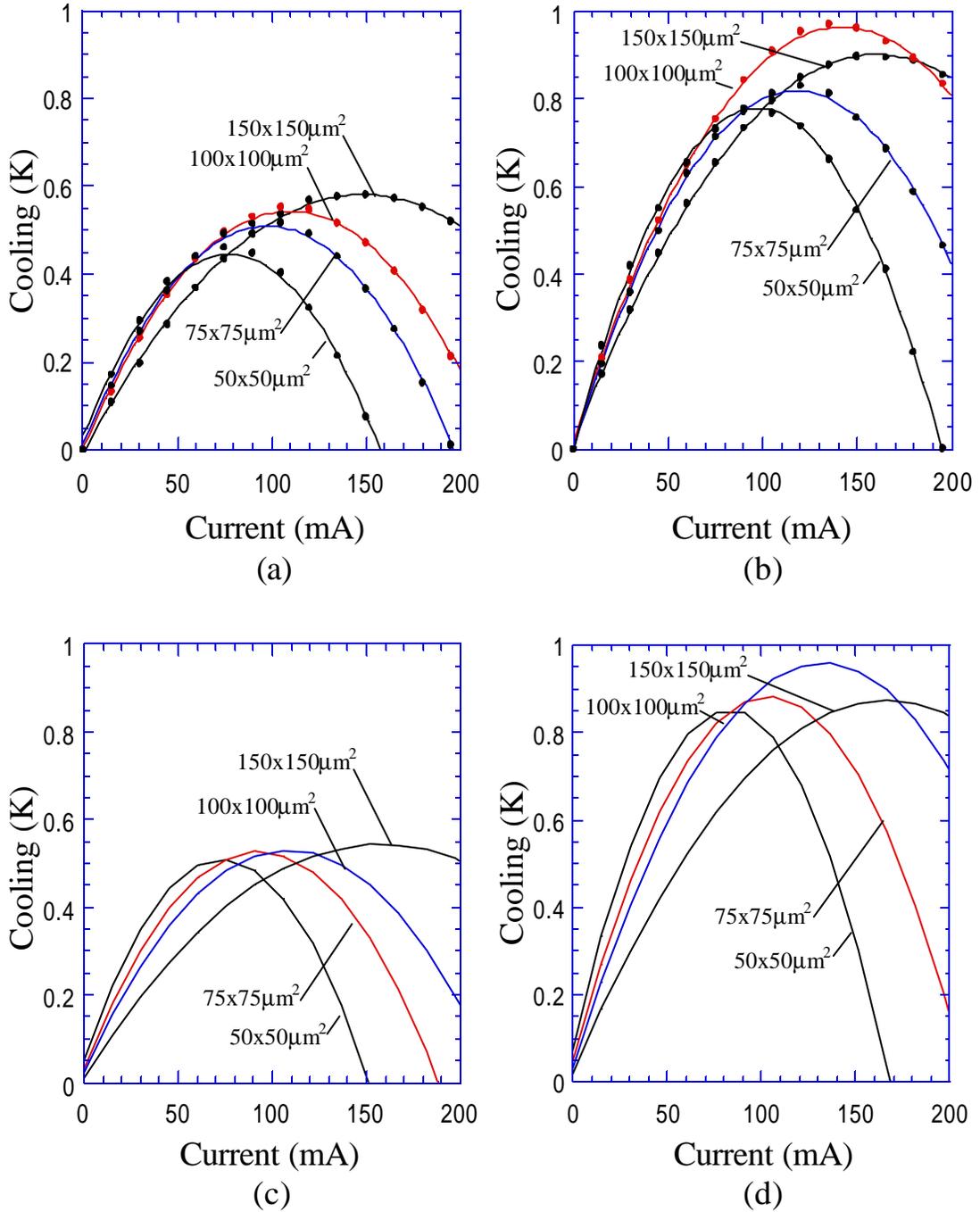
Figure 6.23 compares the results of the 3-D and 1-D models. The two simulations were found to be in good agreement over various changes in parameters. The largest difference can be seen in the temperature profile through the substrate where the 1-D and 3-D distributions are inherently different. The other minor discrepancy is in the temperature distribution of the wire that arises from the additional thermal spreading at the wire-cooler interface. This effect is more difficult to include in the 1-D model.



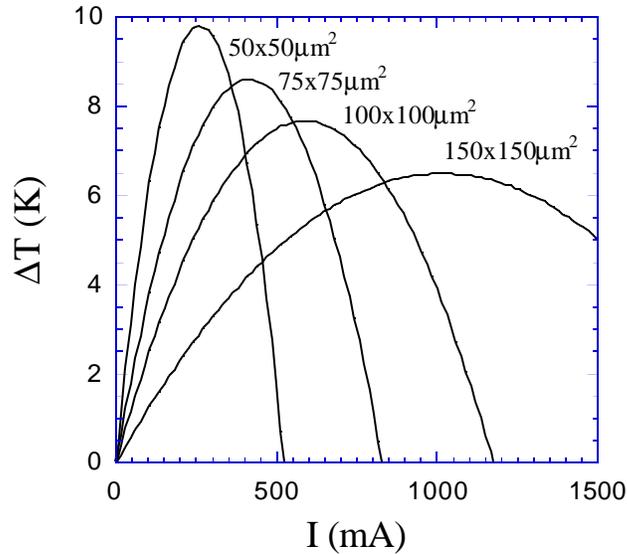
**Figure 6.23** Comparison of simulated temperature profiles through the substrate, cooler, and wire bond for the three-dimensional (ANSYS) and one-dimensional (MATLAB) models. The zero temperature axis is relative to 300 K.

Using this 1-D model, it has been possible to closely match the area dependence of cooling seen experimentally with the simulation. Figure 6.24 shows an example of measured and simulated cooling versus current for several different device sizes and heat sink temperatures of an InGaAs/InGaAsP *p*-type superlattice cooler. These simulations also used a more intricate model for the integrated side contact. Excellent agreement can be seen between the two results, and even the change in optimum device size over heat sink temperature from  $150 \times 150 \mu\text{m}^2$  to  $100 \times 100 \mu\text{m}^2$  was reproduced by the simulation. The temperature dependence of optimum device size stems from the area dependence of thermal conduction through the SL and increased cooling due to the larger energy spread of the carriers. From the simulation, the limiting factors on cooler performance could be determined. Contact resistance and the wire contact were determined to be of greatest concern with a lesser limitation from the substrate thermal resistance. Figure 6.25 shows simulation predictions for minimized side-contact losses and reduced contact resistance ( $5 \times 10^{-7} \Omega\text{cm}^2$ ). Nearly 10 K at room temperature should be possible, corresponding to cooling power densities exceeding  $1000 \text{ W/cm}^2$ .

The advantage of the 1-D model is the speed with which many device parameters can be varied and their affects determined. Figure 6.26a shows a simulation of maximum cooling versus contact resistivity for various cooler thicknesses. To observe just the limitation of contact resistance, the other non-ideal effects were minimized to reasonable values. The substrate thermal resistance was

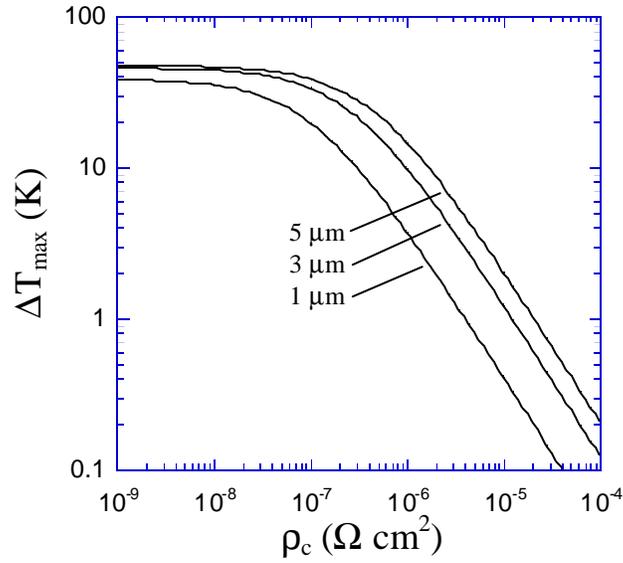


**Figure 6.24** (a) Measured cooling versus current bias at 25°C and at (b) 70°C. (c) Corresponding simulation results at 25°C and at (d) 70°C. Measurement and simulations performed by D. Vashae.

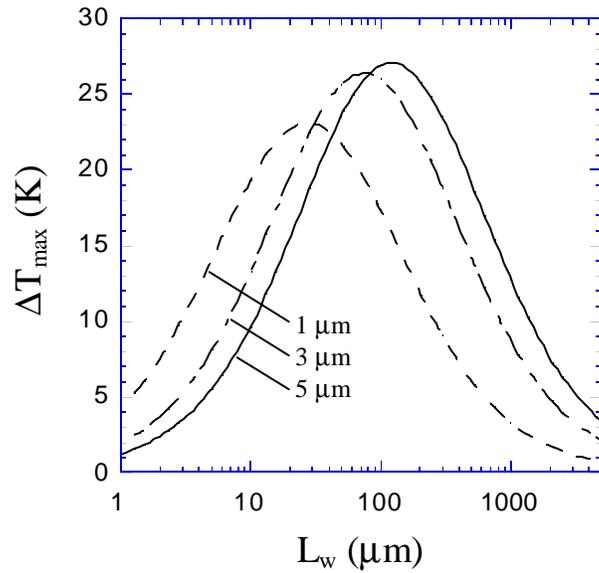


**Figure 6.25** Simulation prediction of cooling versus current for the *p*-type InGaAs/InGaAsP superlattice coolers. The simulation assumes that the side contact losses are minimized and  $r_c$  is reduced to  $5 \times 10^{-7} \Omega \text{cm}^2$ . Simulation by D. Vashaee.

assumed to be 4 K/W, which from Figure 6.19 could represent either a thin 15  $\mu\text{m}$  Cu-substrate or an arbitrarily thick diamond substrate. The wire bond was assumed to be 50  $\mu\text{m}$  long and 50  $\mu\text{m}$  in diameter with no heat conduction through the wire as would be in a *p*- and *n*-type conventional thermoelectric configuration. The maximum cooling drops off significantly for a contact resistivity above  $10^{-7} \Omega \text{cm}^2$ . Also, thicker devices cool more when the contact resistance is substantial. The reason being that the optimum current for the cooler performance scales as one over the device thickness. A lower current results in less Joule heating from the contact resistance. Optimum currents for the thicker devices were less than 1 A, while the



(a)



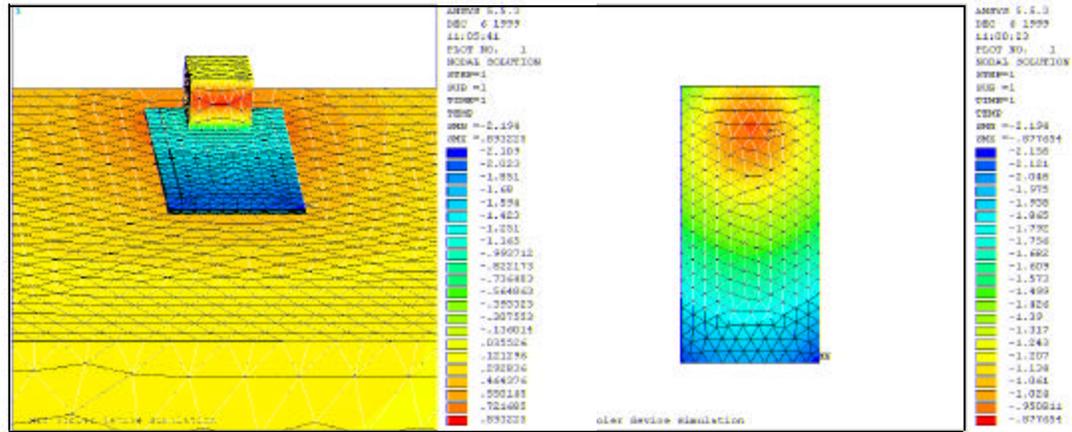
(b)

**Figure 6.26** (a) Simulation of maximum cooling versus contact resistivity for various cooler thicknesses. The Au wire bond was 50  $\mu\text{m}$  long and 50  $\mu\text{m}$  in diameter and zero heat conduction though the wire was assumed as in a  $p$  &  $n$  cooler configuration. (b) Simulation of single stage maximum cooling versus Au wire bond length (25  $\mu\text{m}$  diameter wire) where now heat conduction through the wire is considered. The contact resistance was assumed to be  $10^{-8} \Omega \text{ cm}^2$ . The substrate thermal resistance was 4 K/W in each case.

thinner devices required as much as 5 A. The thicker devices do attain higher absolute cooling in this case, but the cooling power remains approximately unchanged.

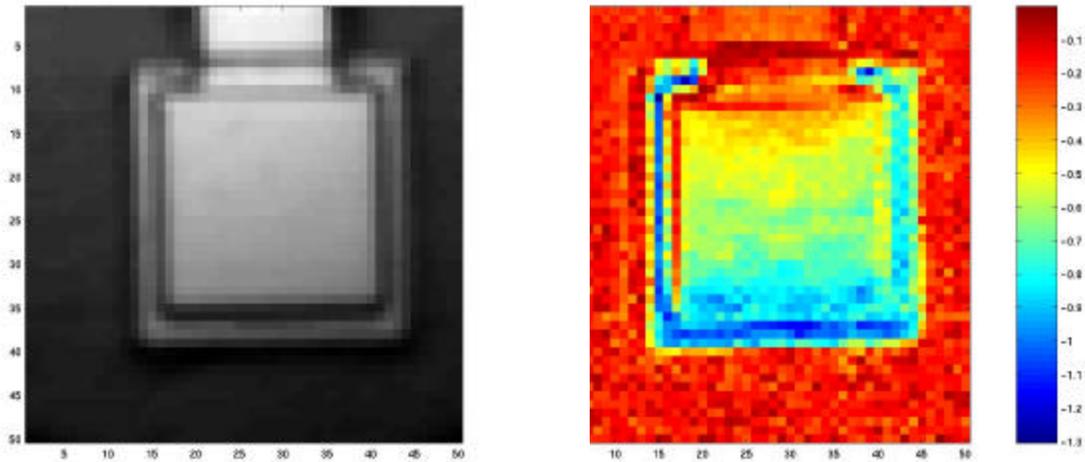
In applications for which single element coolers are monolithically integrated with electronic or optoelectronic devices, it is necessary to have an external wire bond connected directly to the cold side of the cooler. The question arises as to whether useful cooling can still be achieved in this configuration. Figure 6.26b shows a simulation of maximum cooling versus wire bond length (25 $\mu$ m diameter). In this case heat conduction through the wire is considered, and the contact resistivity is assumed to be  $10^{-8}$   $\Omega\text{cm}^2$  in order to study the effects of the wire only. For a given cooler thickness, there exists an optimum wire length resulting from a trade-off between Joule heating in long wires and heat conduction from heat sink to the cold junction in short wires. At longer wire lengths the thicker devices cool better by the same argument made for contact resistance. That is thicker coolers are optimized at a lower current and hence less Joule heating occurs. The cooling power of the thicker devices is somewhat reduced however. For shorter wire lengths the thinner cooler performs best. Since the thinner cooler has a smaller thermal resistance between cold and hot junctions, more heat conduction occurs across the cooler than through the wire.

The temperature dependence of material properties and cooling amount are not taken into account in the above models. For small values of cooling and heating on



(a)

(b)



(c)

(d)

**Figure 6.27** (a) Thermal image from a 3-D ANSYS simulation of a rectangular shaped ( $50 \times 100 \mu\text{m}^2$ ) thin-film cooler. The tall block structure at the far end of the cooler is the scaled wire bond. (b) Top view of the simulated thermal contours on the surface of the cooler. (c) Optical normalization image of a square ( $40 \times 40 \mu\text{m}^2$ ) cooler with integrated wire bond and (d) the thermal image from a thermoreflectance measurement. Both the simulation and measurement show a similar profile on top of the cooler due to the Joule heating and heat conduction from the wire bond. The image is not corrected for the different thermoreflectance coefficient of the InP surface. Only values on top of the cooler are valid. Bottom images from J. Christofferson.

the order of 5-10 K, this is a reasonable assumption. However, these effects should be considered for larger temperature gradients.

Even with the speed and accuracy of the 1-D model, full 3-D simulations are still useful to observe graphically the temperature profiles throughout the device. These simulations can also be used to compare and explain experimentally measured thermal images produced by the thermoreflectance measurements. Figure 6.27 shows an example of simulated and experimental temperature profiles for various devices. In each case, similar temperature distributions on top of the cooler are observed due to the Joule heating and heat conduction from the wire bond. The result is that the maximum cooling occurs at the edge of the cooler, farthest away from the wire bond.

## 6.5 Device Results and Future Direction

A brief summary of the best cooling results for the various material systems described in this work is given in Table 6.2. Currently both the InGaAsP and InP

**Table 6.2** Comparison of best device results for various superlattice designs. All results shown are for  $40 \times 40 \mu\text{m}^2$  size and a  $20^\circ\text{C}$  heat sink. The detailed structures were discussed in Chapter 3.

<i>Superlattice Design</i>	<i>Carrier Type</i>	<i><math>DT_{max}</math> [K]</i>	<i>Measurement Method</i>
InGaAs/InGaAsP	N	2.0	Thermoreflectance
InGaAs/InGaAsP	N	1.15	$\mu$ -Thermocouple
InGaAs/InGaAsP	P	0.97	$\mu$ -Thermocouple
InGaAs/InP	N	1.13	$\mu$ -Thermocouple
InGaAs/InAlAs	N	0.3	$\mu$ -Thermocouple
InGaAs/AlGaAsSb	N	0.3	$\mu$ -Thermocouple

barrier *n*-type devices show the greatest amount of cooling, however the InP-barrier devices possess greater potential as shown theoretically in Chapter 2. Continued work in optimizing the designs to prevent mini-band conduction should allow these devices to realize this predicted potential. While the InAlAs-barrier devices carry even greater prospects, more work is necessary to fully understand the design issues in such highly doped structures, especially in avoiding the mini-band conduction that is more prevalent in these high-barrier short-period superlattices. Sb-based devices are also a good direction to pursue due to their good thermoelectric properties and capability to tailor the barrier heights over a wide range, yet much work is necessary in studying the material issues since this is not a well known material system. Besides the *n*-type devices, the *p*-type InGaAs/InGaAsP structure also performed relatively well. The biggest inhibitor was the high contact resistance which limited the allowable current bias. Reducing the *p*-type InGaAs contact-resistance should immediately result in cooling values of 10K as predicted in Figure 6.25. Moreover, the *p*-type material boasts a much greater Seebeck coefficient than that of its *n*-type counterpart as shown in Chapter 4.

## 6.6 Summary

Numerous practical and effective methods for accurately characterizing temperature over small spatial dimensions have been developed. The most expeditious technique for point measurements has been the  $\mu$ -thermocouple system, but its heat load effects

on small devices must be considered. The foremost method for thermal imaging measurements has been the thermoreflectance system which has far outperformed infrared-based cameras.

A thorough experimental investigation of InP-based thin-film thermionic coolers has been presented. Through modeling of the geometry and temperature dependent cooling, an understanding of device performance has been achieved. Evidence exists to suggest thermionic emission is a significant portion of cooling in some structures, but it has been difficult to quantify. Important parameters and non-ideal effects in thin-film coolers have been discussed through experimental and simulation results. A three-dimensional finite element simulation has been developed and used to determine the dominating non-ideal mechanisms for thin film coolers and the impact of changing device characteristics. A one-dimensional simulation was also developed using three-dimensional spreading resistance values obtained from the three-dimensional model. Contact resistance, finite thermal resistance of substrate and heat sink, and heat generation in wire bonds have all been identified as limitations in thin-film cooler performance. Experimental results in thin-film thermionic emission coolers have demonstrated cooling by 1-2 K at room temperature, and even larger values at elevated heat sink temperatures. This amount of cooling over 1-2  $\mu\text{m}$  thick barriers corresponds to cooling power densities up to  $1000 \text{ W/cm}^2$ . Simulations have predicted cooling of 20-30 degrees with cooling

power densities of many 1000's  $W/cm^2$  for more optimized structures and packaging.

A new type of cooler structure was also discussed, the two-stage three-terminal TITE cooler. Enhanced cooling was demonstrated with an InP-based TITE structure, and the interesting three-terminal effects studied. It is expected that this new design will have greater consequence for more optimally doped InP substrates, or with a different material system for which the substrate possesses better thermoelectric properties.

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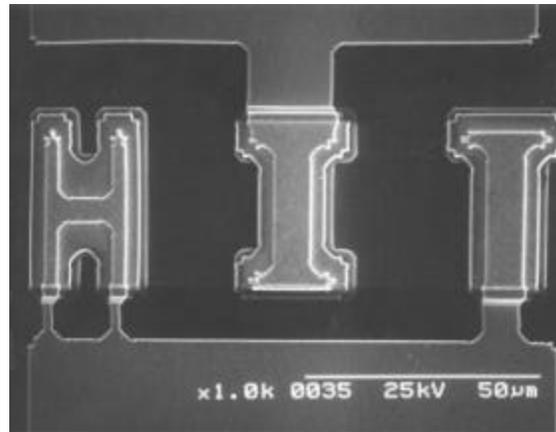
## Chapter 7

### Integration with Optoelectronic Devices

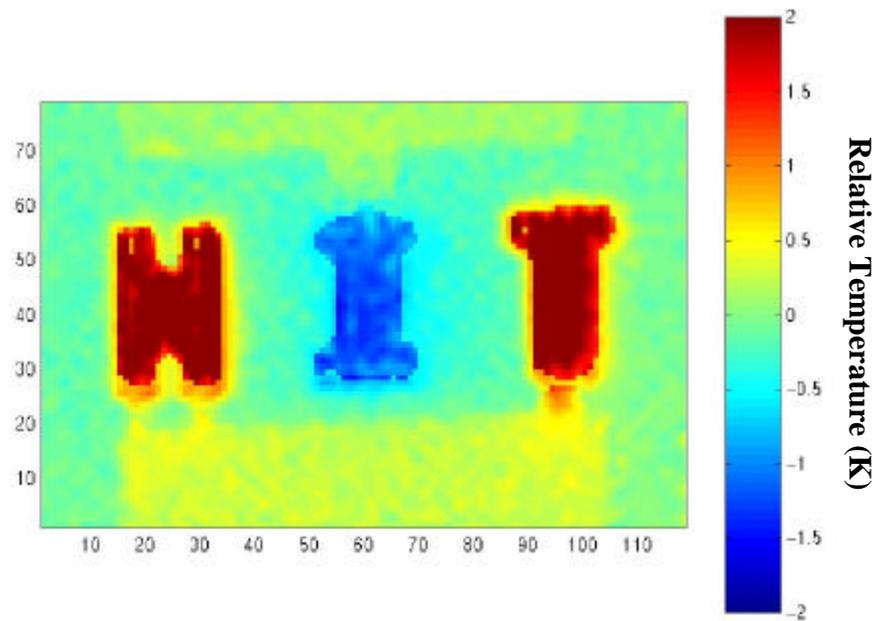
With the thorough discussion of single-stage micro-coolers and related issues presented in previous chapters, we can now turn our attention to integration with optoelectronic devices. Most optoelectronic devices can benefit from some form of cooling or temperature stabilization and for many applications of these devices, such as wavelength division multiplexed (WDM) optical communication systems, it is essential.

While large temperature differences are not yet available with thin-film coolers, they can currently provide very precise localized cooling and heating. They can also provide large cooling or heating power densities, orders of magnitude more than conventional thermoelectric devices. Figure 7.1 shows an example of this microscale temperature control on three patterned coolers with a lateral spacing of 20  $\mu\text{m}$ . Approximately 4 K of temperature differential is seen with no noticeable change in the surrounding surfaces. This temperature change corresponds to 100's of  $\text{W}/\text{cm}^2$  in cooling or heating power density.

In this chapter, we will first investigate the frequency response of cooling as this is an important parameter in the applications discussed later. Three examples of integrated cooling are then described, which include a *p-i-n* photodiode, in-plane laser, and VCSEL structure. Different approaches are utilized for each case, which



(a)



(b)

**Figure 7.1** (a) SEM image of three patterned InGaAs/InGaAsP heterostructure integrated thermionic (HIT) coolers. (b) A thermal image under forward (heating) and reverse (cooling) bias showing approximately 4 K of temperature differential. The spacing between the individual coolers was 20µm. Thermal image from J. Christofferson.

can be categorized as monolithic or heterogeneous integration. Thermionic cooling in heterostructures is shown to match well with the requirements for monolithic integration since the coolers themselves are made from the same materials allowing for lattice-matched structures. While this may still involve a compromise in the optimum design of each structure, the processing is much easier. Heterogeneous integration offers more flexibility as each device is separately optimized and joined afterwards. This can require more complicated packaging as proper alignment is needed and possibly windows for light propagation. Also, a careful choice of joining materials must be made so that a good thermal contact is established.

### 7.1 Transient Operation

In many applications, the speed with which cooling occurs is an important parameter. In thermally tuned devices, the operating characteristics may only be changed as fast as the temperature dictates, as in the wavelength of a laser for instance. The thermal diffusion time can be expressed in terms of the characteristic length  $L$  and thermal diffusivity  $\mathbf{a}$ :

$$\mathbf{t} = \frac{L^2}{\mathbf{a}} \quad (7.1)$$

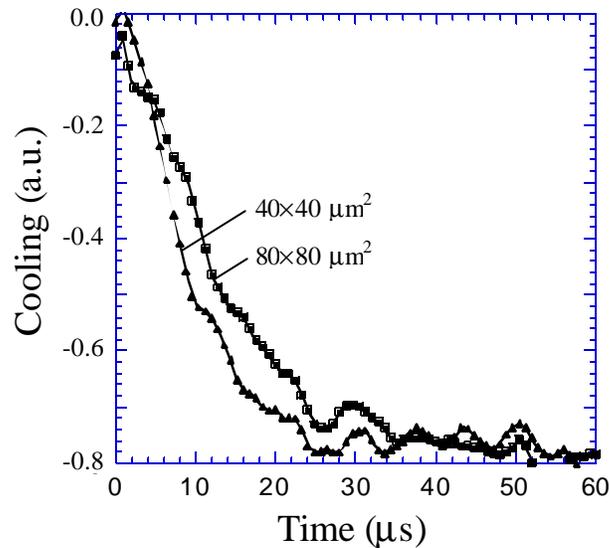
Since the cooling region of integrated thin-film cooler structures can be located so closely to the integrated device ( $\sim$  several  $\mu\text{m}$ ), the intrinsic diffusion time can be sub-microsecond. Comparatively, cooling a device through the substrate as in

conventional thermoelectric configurations takes much longer. For example, cooling a laser through a thinned 100- $\mu\text{m}$  GaAs substrate ( $\alpha = 0.24\text{cm}^2/\text{s}$  [1]) would have an estimated diffusion time of 500  $\mu\text{s}$ .

To experimentally characterize the transient response of the coolers, the thermorefectance system was modified to take single point measurements from a reflected laser source to a photodetector and oscilloscope [2]. The devices were excited with current pulses whose duration was long enough to reach steady state. The measurement results for a 3- $\mu\text{m}$ -thick  $\text{Si}_{0.8}\text{Ge}_{0.2}$  thin film cooler are shown in Figure 7.2 (measurements on InP-based coolers have not yet been performed, but the response should be very similar). A response time of approximately 15-25  $\mu\text{s}$  was measured for these devices, much longer than the sub-microsecond time estimated above. This has been attributed to the substrate effect in impeding the heat flow away from the device. Also, there is some finite thermal mass from the metal side contact, but this is not believed to be the limiting factor. Further measurements have demonstrated that the response time is nearly independent of device size (from 400 to 10,000  $\mu\text{m}^2$ ) and substrate thickness (from 100 to 350  $\mu\text{m}$ ) [2].

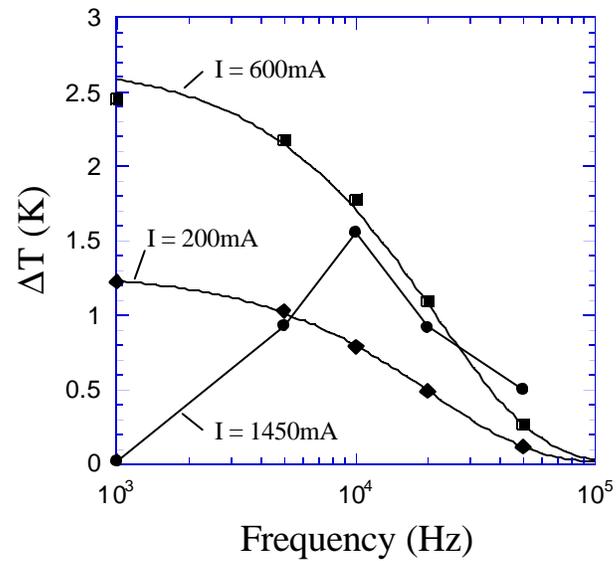
For some applications the stabilization time is of greater importance. This is the time needed for temperature to reach steady state in a cooler. For thin-film micro-coolers, all of the significant cooling and heating sources are located within a few microns of each other, and so the stabilization time is only slightly longer than the thermal response time. However, conventional thermoelectric coolers have

thermoelement lengths of several millimeters resulting in stabilization times of 20 to 30 seconds [3].

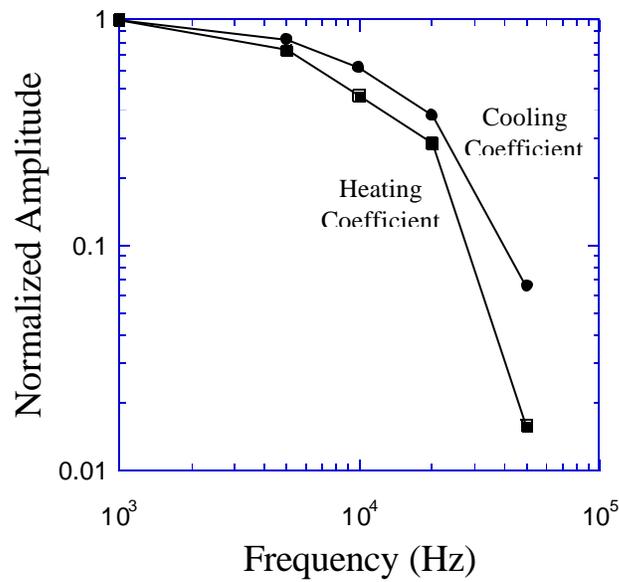


**Figure 7.2** Transient response of two different sized SiGe thin film coolers as a function of time. The response time is on the order of 15-25  $\mu\text{s}$ . Measured by A. Fitting.

In some instances, the cooling requirements are constantly changing, and the concept of cooling frequency-response can be introduced. In this measurement, the coolers are driven by a square-pulse current-signal at a given frequency, and the temperature is measured by the thermoreflectance method. Figure 7.3a shows the large-signal frequency-response of an  $80 \times 80 \mu\text{m}^2$  3- $\mu\text{m}$ -thick SiGe cooler at various zero-to-peak currents. For the first set of points at low current ( $I=200 \text{ mA}$ ), the Joule heating effects can be neglected, and the response is simply dependent on the thermal RC time-constant ( $\tau = 46.3 \mu\text{s}$ ) of the cooling region. As the current is



(a)



(b)

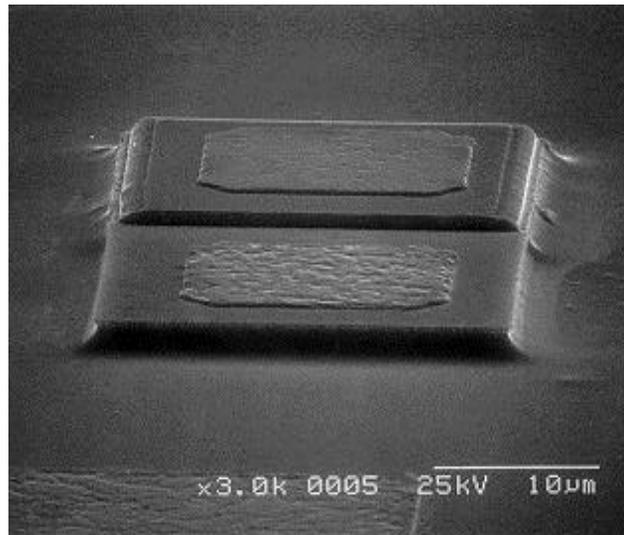
**Figure 7.3** (a) Frequency response of an  $80 \times 80 \mu\text{m}^2$  3- $\mu\text{m}$ -thick SiGe micro cooler. The various currents ( $I$ ) indicated are 0 to peak values of the square-pulse input signal. Exponential curve fits are used for the two lowest currents. (b) Frequency response of the normalized cooling and heating coefficients of the  $\Delta T$  versus  $I$  curves. Measurements by J. Christofferson.

increased and the non-linear heating becomes prevalent, the temperature no longer follows a simple exponential relation with frequency. This is further complicated by the higher order harmonic generation from the square-pulse current-waveform. Interestingly, for current pulse magnitudes that produce no cooling at DC or low frequencies, cooling can still occur at higher frequencies as shown for the 1450 mA curve in Figure 7.3a. Looking more closely in Figure 7.3b, the cooling coefficient is seen to have a faster response than that of the heating coefficient. This can be attributed to the close proximity and localization of the cooling effects versus the more spread out and distributed heating effects. More work is necessary to solve the energy-balance heat-diffusion equations and to accurately simulate the frequency response to fully understand the behavior.

## 7.2 PIN Photodiode

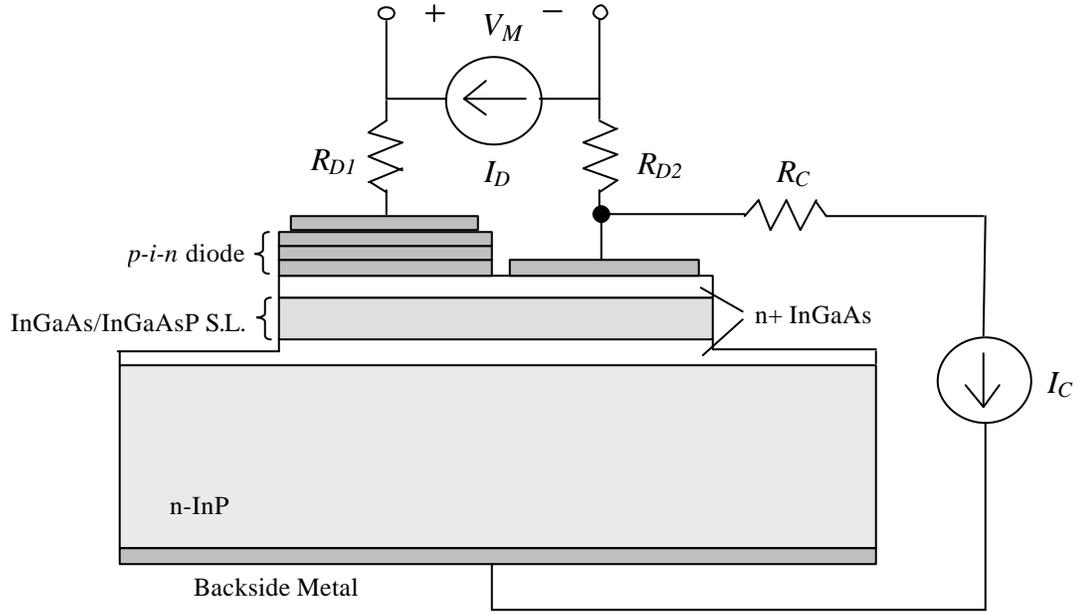
For the first demonstration of monolithically integrated cooling with an optoelectronic device, an InP *p-i-n* diode was chosen. The tested thermionic cooler structure consisted of a 1- $\mu\text{m}$ -thick superlattice barrier (low-barrier design from Chapter 3) surrounded by  $n^+$  InGaAs cathode and anode layers grown by metal organic chemical vapor deposition (MOCVD). The cathode and anode layers were 0.3  $\mu\text{m}$  and 0.5  $\mu\text{m}$  thick, respectively. On top of these layers, the 0.85- $\mu\text{m}$ -thick *p-i-n* diode was grown during the same MOCVD growth. In two wet etching steps, two stacked mesas are defined corresponding to the diode on top of the cooler as

shown in Figure 7.4. The cooler mesas ranged in size from  $20 \times 40 \mu\text{m}^2$  to  $100 \times 200 \mu\text{m}^2$ , and the diode size was one half that of the cooler size. Ti/Pt/Au was used to make ohmic contacts to both the  $p$ - and  $n$ -type material. The substrate was thinned to approximately  $125 \mu\text{m}$  before the backside metal was deposited. The integrated devices were then cleaved, packaged, and wire bonded for testing.



**Figure 7.4** SEM of a processed device showing the monolithically integrated  $p$ - $i$ - $n$  photodiode on top of the  $1\text{-}\mu\text{m}$ -thick InGaAs/InGaAsP thermionic cooler.

The diode served two purposes in the measurement. First, by changing the current through the diode we could effectively change the heat load of the cooler. Second, by monitoring the voltage across the diode, we could measure the temperature [4] on the cold side of the cooler,  $T_C$ . The temperature sensitivity of the diode near room temperature was determined to be  $1.936 \text{ mV}/^\circ\text{C}$  at a bias of  $1 \text{ mA}$ .



**Figure 7.5** Set-up for measuring the temperature of the integrated diode versus the current through the cooler ( $I_C$ ) and the diode ( $I_D$ ).  $R_{D1}$ ,  $R_{D2}$ , and  $R_C$  are the wire bond resistances.

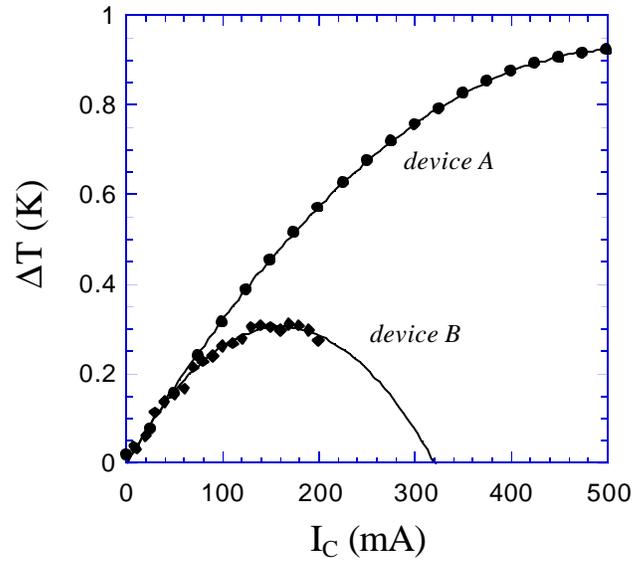
The measurement set-up is illustrated in Figure 7.5. A constant current ( $I_D$ ) was sent through the diode and the diode voltage ( $V_D$ ) was monitored as the cooler current ( $I_C$ ) was varied. The resistors of Figure 7.5 represent the parasitic wire bonds that add to the heat load on the device. The measured voltage can be expressed as:

$$V_M = (R_{D1} + R_{D2})I_D + V_D + \frac{r_c}{A_c}(I_D + I_C) \quad (7.2)$$

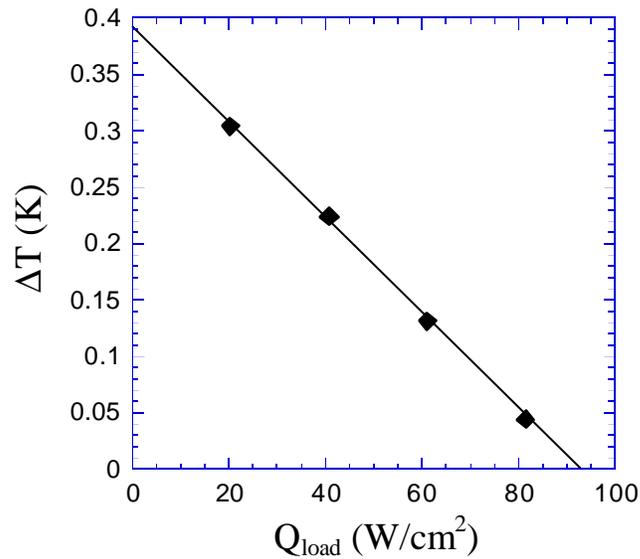
where  $R_{D1}$  and  $R_{D2}$  are the wire bond resistances,  $r_c$  is the contact resistivity, and  $A_c$  is the area of the metal contact on the cooler. If Equation 7.2 is rearranged to solve for  $V_D$  as a function of  $I_C$ , then the resulting expression is equal to the measured voltage minus some constant values, and minus a value that changes with respect to

$I_C$ , that is  $r_c I_C / A_C$ . Therefore to correctly measure the temperature on top of the device, the contact resistivity must be determined. Once  $V_D$  is known, the temperature can be calculated using the temperature dependence of the diode voltage at a constant current given above.

The temperature of the device was also measured with the micro-thermocouple system. Device *A* from Figure 7.6 shows the temperature versus current for the cold side of a  $70 \times 140 \mu\text{m}^2$  cooler that had the integrated diode removed by selective wet etching. The temperature data was curve fit with a second order polynomial resulting in a linear coefficient of 3.53 K/A, and a quadratic coefficient of 3.37 K/A<sup>2</sup>. Since this cooler structure was identical to the one with the integrated diode (device *B*), the two devices should have the same linear coefficient. The quadratic coefficient, on the other hand, may differ since Joule heating is dependent on processing variations such as contact resistance, packaging and wire bonding. Consequently, the contact resistance ( $r_c$ ) can be determined from Equation 7.2 by adjusting its value until the linear coefficients match. Using this method, device *B* from Figure 7.6 also shows the temperature versus current for the cold side of a cooler with an integrated diode biased at 1 mA. The performance is much worse due to poorer packaging and a higher contact resistance. For device *B* the contact resistance is at least doubled since the effective contact area is only one-half that of device *A* due to the space that is taken by the diode. Its value was determined to be  $4.4 \times 10^{-6} \Omega\text{cm}^2$ . Comparatively, the contact resistance for device *A* was measured by



**Figure 7.6** Measured cooling versus cooler current using a micro-thermocouple for a well packaged device (*device A*), and using the integrated *p-i-n* diode with poorer packaging (*device B*). Both device areas were  $70 \times 140 \mu\text{m}^2$ .



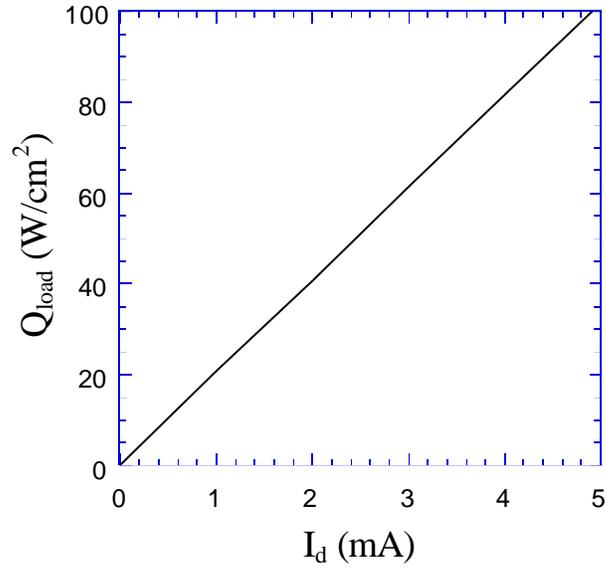
**Figure 7.7** Cooling versus applied heat load density from the integrated photodiode. The points are experimental data while the linear curve fit corresponds to Equation 7.3.

the transmission line model [5] and was estimated to be roughly  $5 \times 10^{-7} \Omega \text{cm}^2$ . Knowing the contact resistance, the current through the diode was increased, and the temperature versus cooler current was again measured. Each time the diode current was changed, the temperature sensitivity was re-calibrated. By changing the diode current, the heat load is changed. Figure 7.7 shows the maximum cooling on top of the device as a function of applied heat load density from the integrated photodiode. The dependence of cooling on the heat load density can be described in a similar manner to that of a thermoelectric device [3],

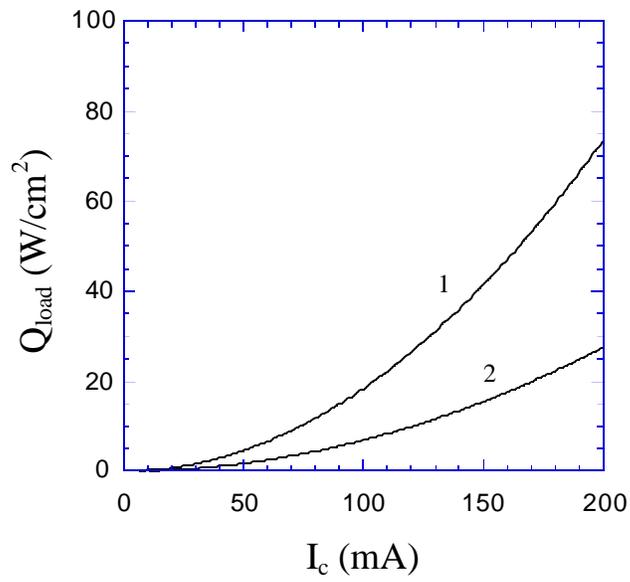
$$T_C = T_{C-\max} \cdot \left(1 - \frac{Q_l}{Q_{l-\max}}\right) \quad (7.3)$$

where  $T_C$  is the cold side temperature,  $Q_l$  is the heat load density, and  $T_{C-\max}$  &  $Q_{l-\max}$  are the corresponding maximum values. From Figure 7.7 we find that the maximum cooling was  $0.39 \text{ }^\circ\text{C}$ , and the maximum heat load density was  $93 \text{ W/cm}^2$  considering only heat generation by the diode. In addition to the diode there is a constant heat load due to the two wire bonds attached to the diode ( $R_{D1}$  and  $R_{D2}$ ), and another heat load from the wire bond to the cooler ( $R_C$ ) which changes with changing cooler current. In fact, some of the improvement from device *B* to device *A* in Figure 7.6 can be attributed to the shorter wire bonds.

It is useful to examine the magnitudes of the various sources of heat that are contributing to the total thermal load. Figure 7.8 shows the heat load density versus the respective current bias for the dominating sources of heat. For small temperature



(a)



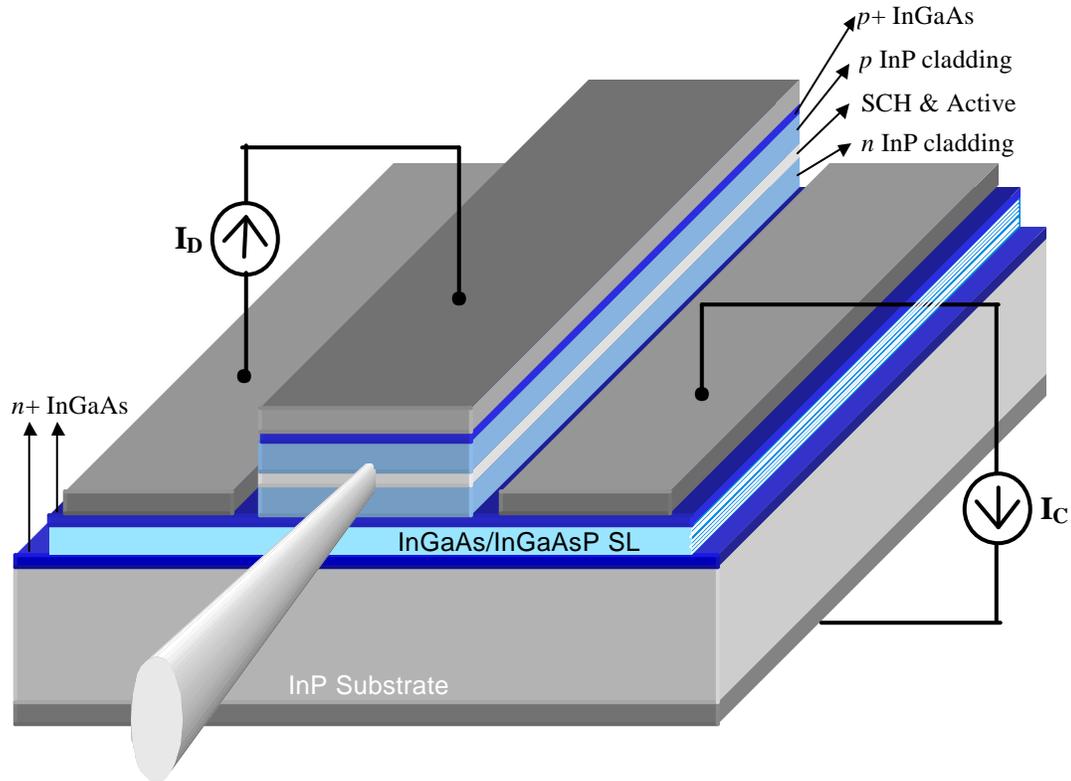
(b)

**Figure 7.8** (a) Heat load density for the diode versus diode current. (b) Heat load density from the wire bond (curve 1) and from the contact resistance (curve 2) versus cooler current.

differences, it was assumed that approximately one half the heat generation in the wire bonds arrives at the device while the other half goes to the heat sink. The heat generation due to the diode contact resistance and wire bonds connected to the diode is not shown since it was several orders of magnitude smaller because of the small value of diode current. At the optimum cooler current bias of 160 mA (device *B* from Figure 7.6), there is 47 W/cm<sup>2</sup> of heat load density due to the wire bond connected to the device and an additional 18 W/cm<sup>2</sup> due to the contact resistance. Using these values, the actual maximum heat load density was 158 W/cm<sup>2</sup>. This result is more than a factor of ten better than the best bulk thermoelectric cooler.

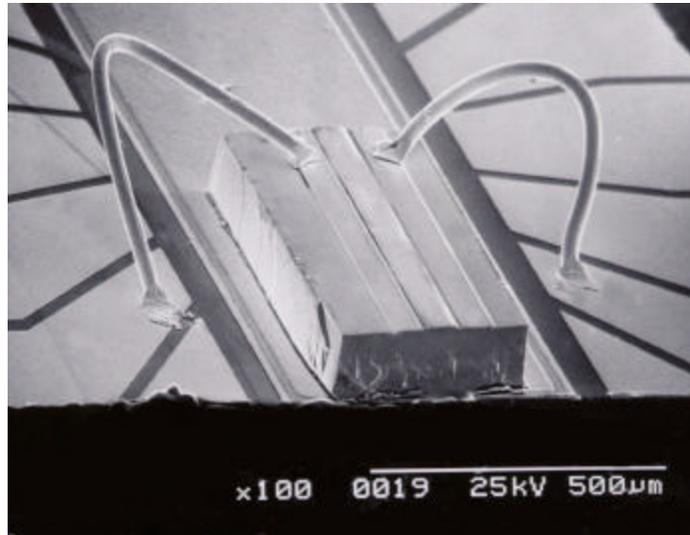
### 7.3 1.55 μm InGaAsP Ridge Waveguide Laser

The next device investigated for monolithic integration of cooling was a 1.55-μm InGaAsP ridge-waveguide laser. A schematic of the structure used is given in Figure 7.9. The growth was performed by MOCVD on a *n*-InP substrate. The thermionic cooler structure was again the low barrier design (1-μm-thick superlattice, 25 periods of 10/30nm InGaAs/InGaAsP,  $\lambda=1.3\mu\text{m}$ ) surrounded by *n*<sup>+</sup> InGaAs emitter and collector layers that were 0.3μm and 0.5μm thick respectively. The laser structure consisted of a 2-μm-thick *n*-InP cladding layer, an undoped InGaAsP active region consisting of five quantum wells ( $\lambda=1.64\mu\text{m}$ ) with a 0.3μm thick confinement layer ( $\lambda=1.15\mu\text{m}$ ) above and below, a 1.5μm thick *p*-InP cladding layer, and a 0.15μm



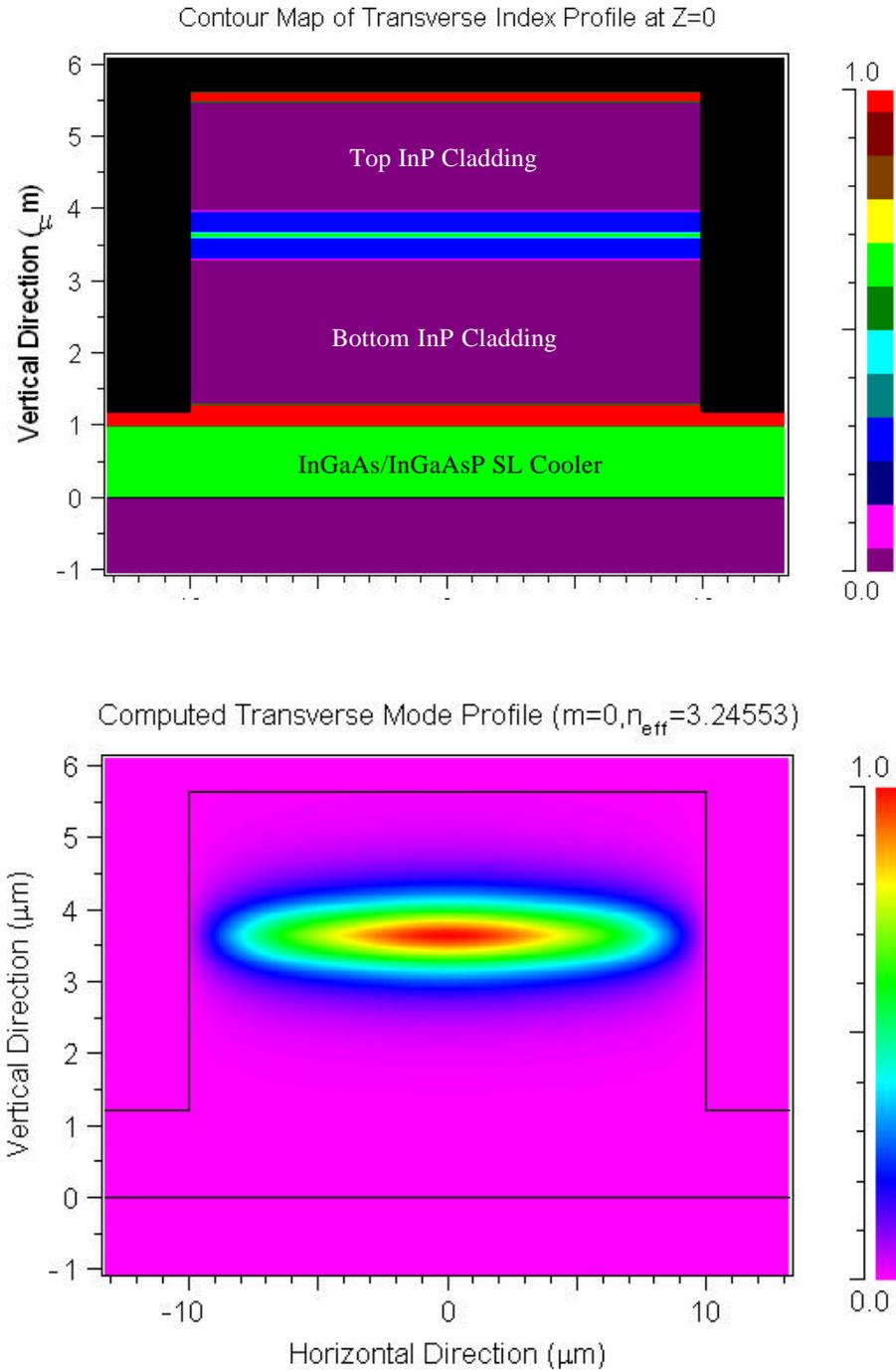
**Figure 7.9** Schematic of thermionic cooler integrated with a ridge waveguide laser showing the laser ( $I_D$ ) and cooler ( $I_C$ ) bias.

thick  $p$ -InGaAs contact layer. The ridge widths were varied from 20 to 50  $\mu\text{m}$ , and the metal contacts to the cooler were 50  $\mu\text{m}$  wide and 10  $\mu\text{m}$  from the edge of the laser mesa. The lasers were cleaved to various lengths (100-300 $\mu\text{m}$ ), mounted on fabricated silicon packages, and wire bonded for testing. Two current sources were used to independently control the current through the laser and cooler sections. An SEM of the processed and packaged device is shown in Figure 7.10.

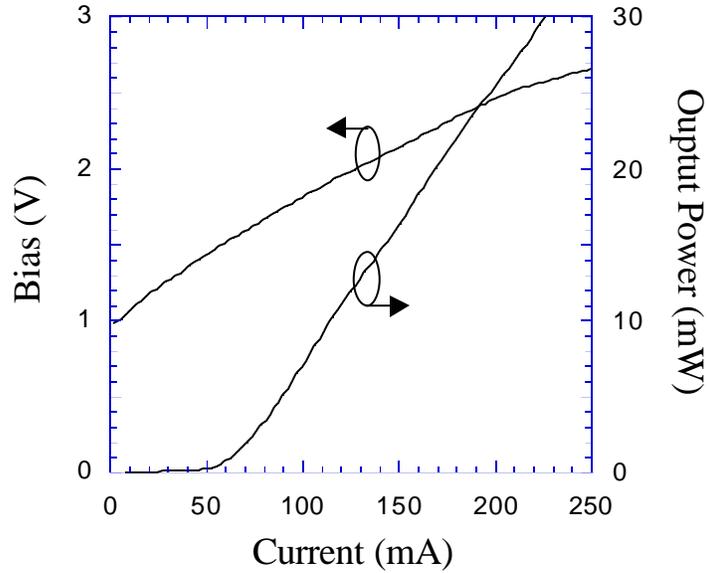


**Figure 7.10** SEM of a processed and packaged ridge laser and monolithically integrated cooler. The laser was mounted at the edge of a cleaved Si package to allow for coupling to a fiber probe. The wire bond for the center stripe  $p$ -contact is not shown.

When designing the integrated structure, it was necessary to consider the optical waveguiding properties of the cooler. The use of high refractive index InGaAs material ( $n=3.587$ ) in the superlattice barrier and contact layers results in an excellent waveguide which must be isolated from the laser active region and separate confinement heterostructure (SCH) region. A two-dimensional waveguide simulation [6] was used to predict the necessary thickness of the lower  $n$ -InP cladding region to eliminate mode leakage into the layers comprising the cooler. Figure 7.11 shows a contour map of the normalized transverse-index profile and corresponding simulation result of the modal confinement in the ridge waveguide.



**Figure 7.11** Contour map of transverse index profile and corresponding simulation of modal confinement in the ridge waveguide. A bottom InP cladding thickness of 2  $\mu\text{m}$  was sufficient to prevent modal leakage into the cooler superlattice.



**Figure 7.12** *L-V-I* characteristics of a ridge waveguide laser integrated with a thermionic cooler. Data is shown for a 100  $\mu\text{m}$  long cavity with a 20  $\mu\text{m}$  wide ridge.

To allow reasonable simulation run times, effective index values were calculated for the active region and cooler superlattice from:

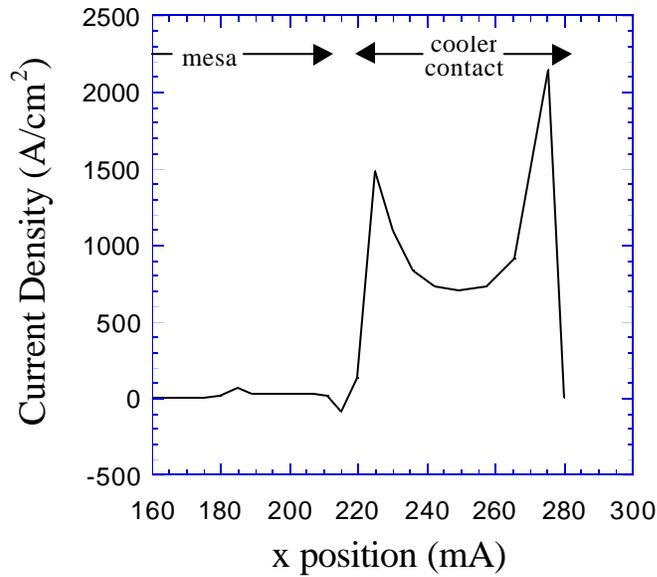
$$n_{eff}^2 = \frac{n_w^2 t_w + n_b^2 t_b}{t_w + t_b} \quad (7.4)$$

where  $n_w$  and  $n_b$  are the index values for the well and barrier, and  $t_w$  and  $t_b$  are the respective thicknesses. The effective index was 3.49 for the active region, and 3.43 for the cooler superlattice. A bottom InP cladding thickness of two microns was determined to sufficiently confine the mode.

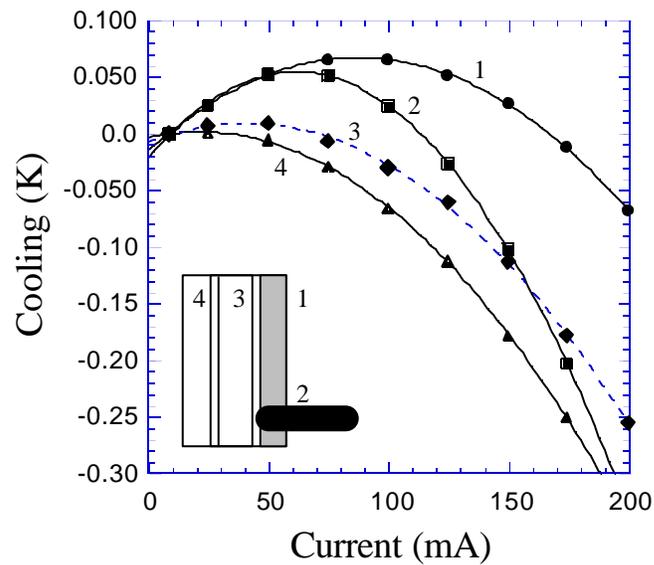
The lasers were first tested with no current to the cooler section (Figure 7.12). Comparing to similar laser structures grown without the extra cooler layers, the lasers operated as expected under pulsed conditions indicating that the addition of

the thermionic cooler structure did not significantly impact the quality of the growth. The emission wavelength was around 1.55  $\mu\text{m}$ , and the temperature sensitivity was measured to be approximately 0.1 nm/ $^{\circ}\text{C}$ . This was then used to monitor the temperature change of the laser versus cooler current. It was determined that the laser would only heat for either current bias direction. To explain the observed experimental results, a commercial laser diode simulator [7] was used to model the integrated device. Simulation results indicated that the current injected from the cooler contact was not spreading underneath the laser mesa negating any superlattice barrier cooling effects (Figure 7.13). It was also determined that the InGaAs region between the laser and cooler was not sufficiently thick enough to prevent a substantial amount of laser current to penetrate into the cooler structure. This reverse current through the cooler superlattice actually causes heating instead of cooling. Figure 7.14 indicates the measured amounts of cooling at various points on the device when there is no bias to the laser section. Only small amounts of cooling are seen on the side contact, and hardly any cooling is measured on the laser mesa.

Surprisingly, the cooling results are in stark contrast to previously published experiments with monolithically-integrated Peltier-cooled lasers [8-11]. In all of the structures described, a metal contact was placed next to the laser and used to pass an additional current through the substrate creating a simple thermoelectric cooler. In these reports, cooling as large as 3 K was reported for InP substrates. Ignoring the cooling properties of the superlattice in our structure, there should still remain a



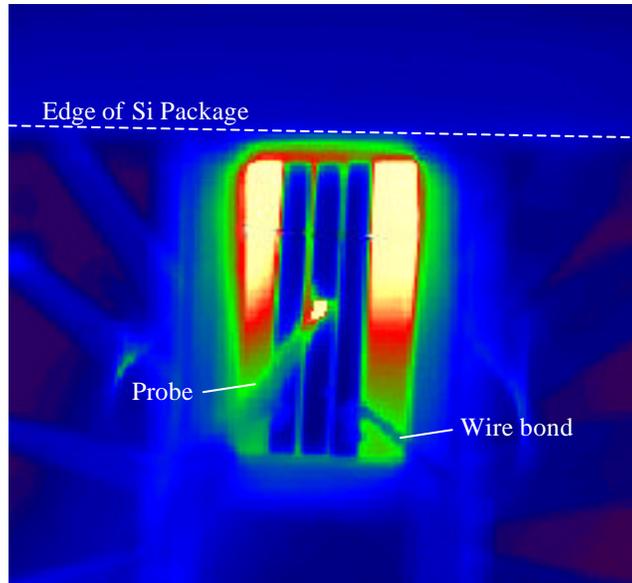
**Figure 7.13** Simulation of current density perpendicular to the cooler at the interface of the InGaAs and cooler superlattice regions. The current does not spread to cool underneath the laser mesa. Simulation by D. Oberle.



**Figure 7.14** Cooling versus cooler current at different points on the laser and cooler. Only small amounts of cooling are seen on the side contact (1&2), and nearly zero cooling on the laser mesa (3). Measurements were taken with the  $\mu$ -thermocouple system.

metal-semiconductor thermoelectric effect that would produce similar results. One explanation is that our structures used more highly doped substrates and epi layers resulting in a smaller Seebeck coefficient. This however, would at most result in a factor of two reduction of cooling. The other possibility was discussed in detail in Chapter 6 (Section 6.2.6). In this previous discussion of two-stage cooling, it was shown that there exists an optimum ratio of currents, one through the side contact and one through the substrate, that minimize heating effects. This minimization is more crucial in lower doped structures where Joule heating in the substrate plays a more involved role. Furthermore, even with no Peltier effects, the temperature versus current through the side contact can still follow the second order polynomial shape that is usually associated with cooling. Further investigation is needed to clearly explain the discrepancies.

The packaging of the laser was also briefly examined. The IR Camera system described in Chapter 6 (Section 6.1.4) was used to generate thermal images of a packaged device under bias. Figure 7.15 shows an image for a laser current of 200 mA and zero cooler current. While quantitative data was not possible due to the poor reproducibility of values, qualitatively more heating is observed on the topmost side of the device. This temperature distribution is due to an increased thermal resistance at the boundary of the Si package. More symmetric heat distributions were seen when the device was mounted away from the edge of the package.



**Figure 7.15** Thermal image of a packaged laser with integrated cooler. The blue regions on the device are the metal contacts and the other regions InP. Larger color changes are seen in the InP due to the larger emissivity constant. Less thermal spreading at the edge of the Si package causes increased heating on one side of the laser chip. The IR-camera measurement system was described in Chapter 6.

While the devices discussed in this section did not perform well, more optimized designs should allow for improved cooling as in the case for the photodiode. Unfortunately, the laser and cooler cannot be operated electrically in series since this current bias would have the cooler heating the laser. The main challenge with these monolithically integrated structures is with the current paths. The contact between the laser and cooler must successfully act as a common terminal without current from each penetrating into either device. An alternative that circumvents this problem is to design a cooling medium that possesses opposite cooling properties for the standard bias direction (discussion of Chapter 2, Section 2.3.4). These types of

materials could exhibit *p*-type cooling properties with *n*-type doped structures, and visa versa. Another possibility is to use heterogeneous integration which is discussed further in the next section.

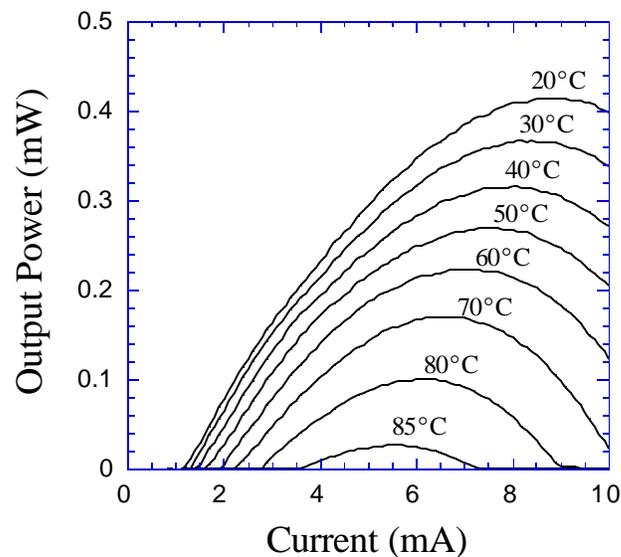
#### **7.4 Long Wavelength VCSELs**

In this section, the most recent ongoing work with integrated cooling for VCSEL structures is presented. Many different approaches have been considered, but we will mainly focus on heterogeneous integration to draw comparisons between the monolithic integration work that was described in the last two sections. Heterogeneous integration allows for more flexibility in material choice and better optimization of the separate VCSEL and cooler structures, but still maintains some constraints on design such as in the optical path.

We begin this section by discussing some of the relevant thermal issues in long wavelength (1.55 $\mu$ m) VCSELs and VCSEL arrays. The arrays are primarily intended for use in wavelength division multiplexed (WDM) short-reach optical links since this wavelength corresponds to the loss minimum of optical fiber [12,13]. Following the discussion of VCSELs, SiGe-based thin-film micro-coolers are examined. This material system currently provides the best available cooling, and also lends itself well to the necessary processing and packaging steps. Finally, the preliminary work on heterogeneous integration by Au-Au bonding is presented.

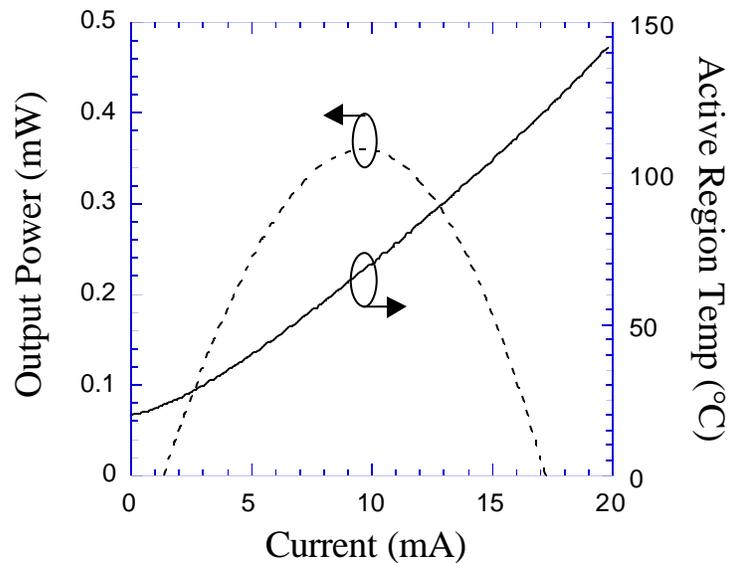
### 7.4.1 VCSEL Thermal Issues

There are two major obstacles to high temperature performance for VCSELs. The first is the development of a suitable mirror in the 1.3-1.55  $\mu\text{m}$  range that is compatible with the active region of choice. The mirrors used must be highly-reflective while still possessing good thermal conduction properties. The second obstacle is in the design of active regions that can provide ample gain at elevated temperatures. The VCSEL structure examined here attempts to satisfy both of these requirements by using an InP/InGaAsP strained multiple-quantum-well (MQW) active region and GaAs/AlAs distributed Bragg reflector (DBR) mirrors [14]. These material systems are not naturally compatible due to lattice mismatch, and so wafer fusion is employed to join the different materials [15].



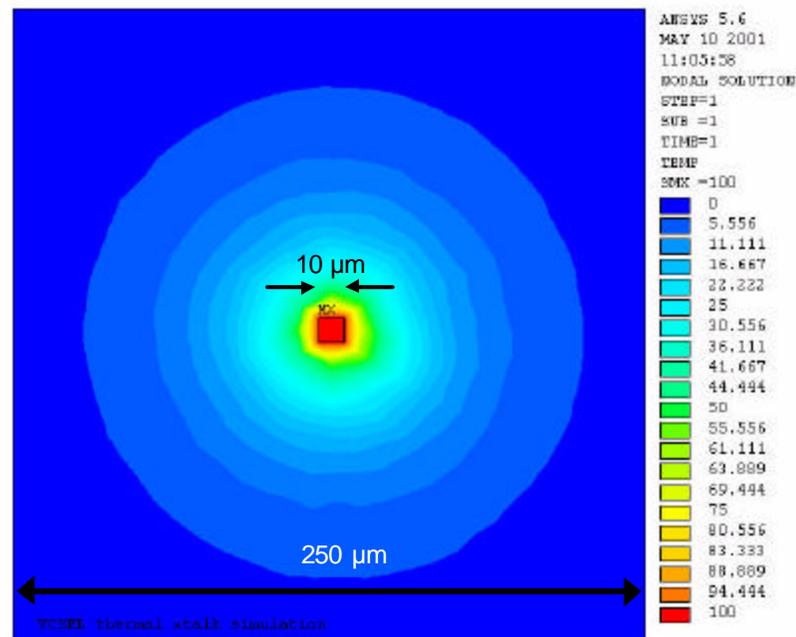
**Figure 7.16** Continuous wave output power versus current for the 1.55  $\mu\text{m}$  VCSELs considered for micro-cooler integration. From A. Karim.

Figure 7.16 shows typical continuous-wave light versus current curves from room temperature up to 85 °C. As the temperature is raised, threshold current increases and differential efficiency decreases until the device no longer lases. The overall reduction in output power over this temperature range is more than 12 dB. Lasing ceases when the active region reaches a temperature for which it can no longer provide the necessary gain to overcome cavity and mirror losses. Unfavorably, the active region typically operates at a substantially higher temperature than that of the heat sink, owing to the considerable thermal resistance between the heat source and sink. Figure 7.17 plots the internal active region temperature over current for a heat sink temperature of 20 °C. For moderate output powers, the active region can be more than 30 °C above the heat sink temperature.



**Figure 7.17** Active region temperature versus current plotted alongside output power for a heat sink temperature of 20 °C. From A. Karim.

Therefore, even with a thermoelectric cooler beneath the substrate, the device temperature can be significantly higher. This can be even greater for structures that include mirrors with a larger thermal resistance.



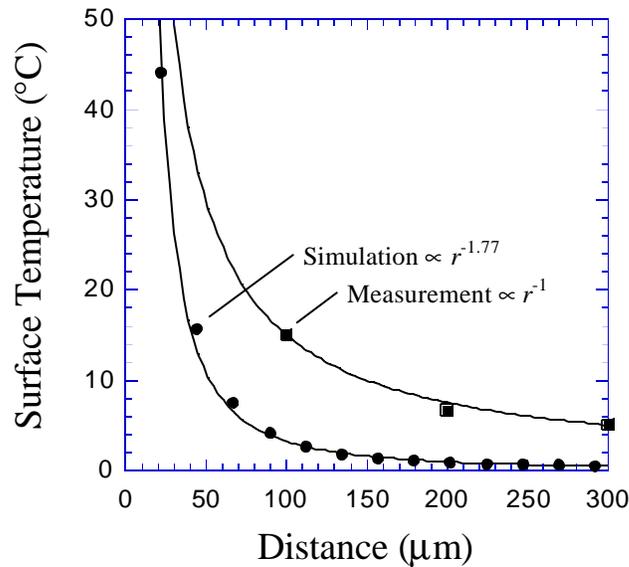
**Figure 7.18** Thermal image of surface temperature from a 3-D ANSYS simulation of substrate heat flow for the long wavelength VCSEL structure. The pillar diameter was  $10\ \mu\text{m}$ , the bottom DBR was  $7.7\ \mu\text{m}$  thick, and the GaAs substrate was  $300\ \mu\text{m}$  thick.

The heat generated by a single VCSEL can also impact the operation of other devices in the array in the form of thermal crosstalk. To evaluate the crosstalk theoretically, a 3-D ANSYS thermal simulation [16] was used to solve the surface temperature surrounding a VCSEL. Figure 7.18 shows such a result for a  $10\ \mu\text{m}$  pillar diameter sitting on a  $7.7\text{-}\mu\text{m}$ -thick GaAs/AlAs DBR and  $300\text{-}\mu\text{m}$ -thick GaAs

substrate. A worse case condition of a 100 °C operating temperature was assumed. The temperature can be seen to drop off very quickly within 20 to 30 μm. An approximate analytical formula for the temperature fall off can be expressed as:

$$T(r) = \frac{P}{2pb_{lat}r} \quad (7.5)$$

where  $P$  is the power of the heat source,  $b_{lat}$  is the effective lateral thermal-conductivity, and  $r$  is the distance from the source [17,18]. Figure 7.19 compares the simulation result to experimentally measured surface temperatures. While the experimental values fit well to Equation 7.5, the simulation values dropped off more steeply showing a stronger inverse dependence on area. This can be explained by the

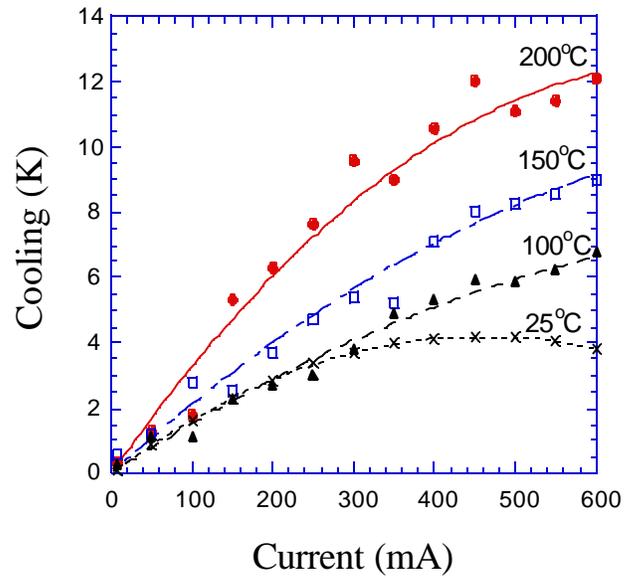


**Figure 7.19** Comparison of simulated and measured surface temperature versus distance from the VCSEL heat source. The two curves show differing area dependence.

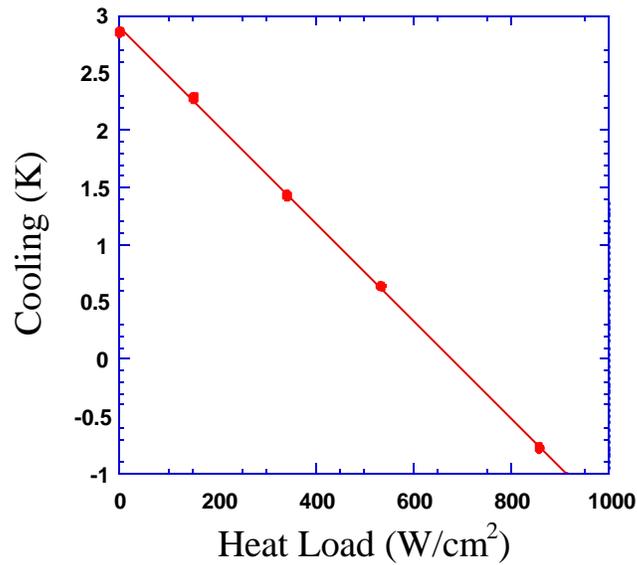
presence of a boundary thermal resistance at the bottom of the heat sink which was not included in the simulation. Evidently, the thermal floor in Figure 7.19 depends on the mounting of the sample to the heat sink. In any case, the experimental values show about 5% of the VCSEL's peak temperature is present 300  $\mu\text{m}$  away from the sample. If another device in the array was also operating, the elevated temperature would affect the output power and emission wavelength. As an example, if a single VCSEL in an array with 300- $\mu\text{m}$ -pitch employing a wavelength spacing of 0.2 nm requires a temperature stabilization of  $\pm 0.5$   $^{\circ}\text{C}$ , the nearest operating device could not heat up beyond 5  $^{\circ}\text{C}$  unless some other active tuning mechanism is used. Thermal crosstalk may be even more of an issue for structures that employ lateral heat spreading layers such as in all-epitaxial long wavelength VCSELs [19]. Reduction in crosstalk is possible by short-circuiting the lateral heat spreading by flip-chip bonding to a good heat sink, but there would still be no control over emission wavelength. Flip chipping to Si-based micro-coolers would allow for integration with both cooling elements and drive electronics.

#### 7.4.2 SiGe Micro-Coolers

Since heterogeneous integration allows for the use of dissimilar materials, the best available thin-film micro-cooler should be used. Recent work on  $\text{Si}_{1-x}\text{Ge}_x/\text{Si}$  [20] and  $\text{SiGeC}/\text{Si}$  [21] superlattice structures have shown impressive cooling performance. Fan *et. al.* have demonstrated maximum cooling values of 4 to 12 K



**Figure 7.20** Cooling versus current and heat sink temperature for a 3- $\mu\text{m}$ -thick,  $50\times 50\ \mu\text{m}^2$ , 12/3nm SiGe/Si superlattice cooler [20]. From X. Fan and G. Zeng.



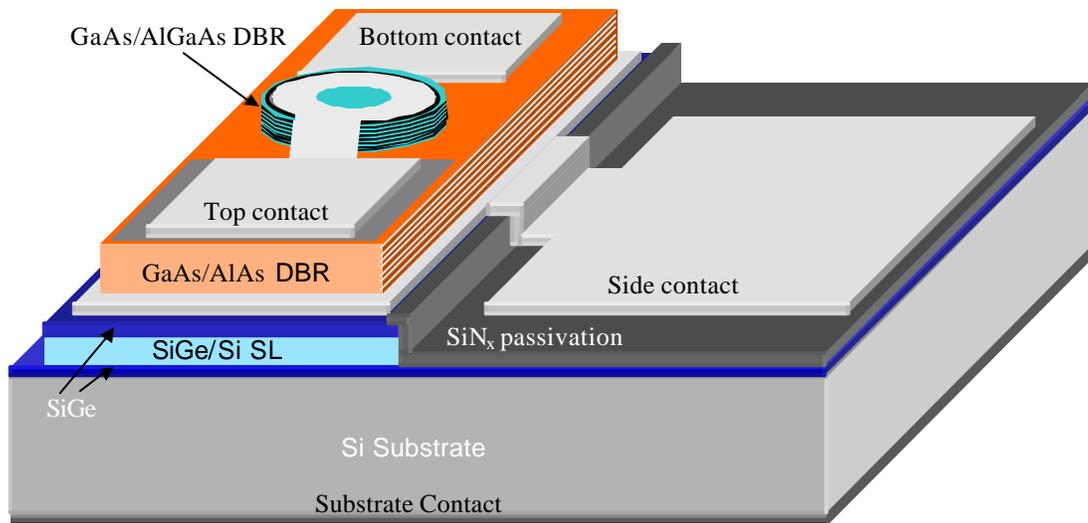
**Figure 7.21** Measured maximum cooling versus heat load for a 2- $\mu\text{m}$ -thick  $40\times 40\ \mu\text{m}^2$  SiGeC thin film cooler [21]. The heat sink temperature was  $70\ ^\circ\text{C}$ . From X. Fan and G. Zeng

with SiGe/Si superlattices (Figure 7.20), and cooling power densities exceeding 900 W/cm<sup>2</sup> for SiGeC/Si superlattices (Figure 7.21). These devices are currently being investigated for integration with Si-based microelectronics, and work is underway to further improve performance with thermionic emission in heterostructures [22].

### *7.4.3 Heterogeneous Integration*

Two procedures have been investigated for heterogeneous integration of coolers with optoelectronic devices. In the first process, blanket evaporation of Ti/Pt/Au (200/1000/5000Å) onto both the unprocessed cooler and optoelectronic wafer is first performed. Then, under the Au-Au bonding conditions outlined in Chapter 5, the two samples are fused together. Finally, a series of etches and metallization steps are completed to define the device and cooler stages. Successful attempts at bonding VCSELs in this manner have been reported [23], but a 1.5- $\mu$ m-thick layer of In was used as well. This is best avoided to keep the thermal conductivity as high as possible at the bonded interface. Previous reports on pure Au-Au bonding have been successful for in-plane micro-strip lasers [24]. Our results for this procedure, which were discussed in Chapter 5 (Section 5.4), showed roughly a 50% yield with test structures. If this method is used for cooler integration with VCSELs, the design must be top emitting due to the underlying metal layers.

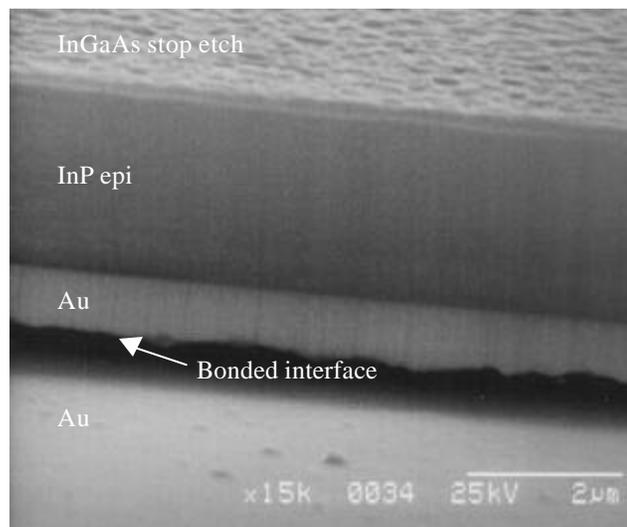
In the second procedure considered, the VCSELs and cooler wafers are first separately processed, and then flip-chip bonded to each other. It is still desirable to



**Figure 7.22** Proposed structure for heterogeneous integration of VCSELs and SiGe/Si superlattice coolers by Au-Au bonding. The laser bias can be applied between the top and side contact, or be made intracavity with two different etch steps. The cooler bias is applied between the side and substrate contacts.

remove the substrate for better thermal isolation between devices, and bottom emitting structures are necessary. Alternatively, the VCSEL could be semi-processed into large mesas before the bonding, and then further etch steps and contact metallization performed afterwards. This structure is illustrated in Figure 7.22. The Au-Au bonding of processed samples should be more reproducible since only small areas need to be joined. Additional test structures were first processed into square mesas and bonded together using the same procedure outlined in Chapter 5. For a  $1.5 \times 1.5 \text{ cm}^2$  sample, only devices on the outer edge of the sample remained attached with an estimated yield of 10%. Smaller sized samples ( $0.75 \times 0.75 \text{ cm}^2$ ) showed the same tendency for poor bonding of mesas near the center, but the yield

increased to roughly 50%. An SEM of a bonded sample is shown in Figure 7.23. While the quality of the bond is difficult to see visually, the mesas that did remain attached survived violent agitation with solvents. Further electrical and thermal evaluation of the test structures or of integrated devices should indicate the quality and uniformity of the Au-Au bond. While it may be justified to include thin layers of In or Sn to accommodate imperfections in the smooth metal surface, the trade-offs between thermal resistance, bond uniformity, and yield should be optimized. A thorough investigation of Au-Sn eutectic thermal conductivity would also be useful.



**Figure 7.23** SEM of a Au-Au bonded test structure. While the quality of the bond is difficult to see visually, the mesas remained attached after violent agitation with solvents.

In either of the two procedures considered, the problems of isolation between the device and cooler current are solved. The metal between the integrated devices

serves as an ideal electrical common, and even intracavity contacts could be used in some of the integrated geometries described.

## 7.5 Summary

There are many issues to consider for integration of cooling with optoelectronic devices. While conventional thermoelectric coolers currently provide larger temperature differences, they can only control the temperature of the substrate and are limited in their cooling power density. Thin-film thermionic and thermoelectric coolers can be integrated with optoelectronic devices to provide active temperature stabilization, wavelength tuning, and large cooling power densities far beyond bulk Peltier coolers. Several integration examples have been described, and the issues with monolithic versus heterogeneous integration have been discussed. Precise spatial control of temperature as well as fast transient times have been demonstrated. With further improvement in cooling performance and integration methods, thermionic cooling can be a viable supplement, and even replacement for conventional thermoelectric coolers.

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## **Chapter 8**

### **Conclusions and Future Work**

This thesis presents the first comprehensive examination of a novel type of micro-cooler for integrated cooling applications with optoelectronic devices. Through the use of thermionic emission in semiconductor heterobarriers, enhancements in the material cooling properties can greatly exceed that of the constituent bulk material values. Throughout the preceding chapters, the theory, design, processing, characterization, and analysis of single-stage and integrated structures has been discussed in detail. The first experimental demonstration of cooling was completed, as well as the first demonstration of integrated cooling. While a great deal of progress was made in the development of these devices, we are still far from realizing their full potential. Continued work in this area is expected to meet much success.

#### **8.1 Summary**

Throughout the first five chapters, the evolution of thermionic cooler development was described step-by-step from basic theory through to the processing and packaging. The introduction of Chapter 1 outlined the current technologies for solid-state cooling of optoelectronics and provided the motivation for this research. The fundamental goal of improving the cooling figure-of-merit  $ZT$  was also defined, as

well as the advantages of integrated cooling versus passive thermal management or conventional thermoelectric coolers. Chapter 2 explained the physics behind thermionic emission cooling, and theoretical calculations were developed to predict an order of magnitude improvement in  $ZT$  for InP-based heterostructures. From these theoretical models and calculations, design guidelines were assembled and applied to the material structures described in Chapter 3. Several different InP-based heterobarrier designs were investigated, each with a different barrier height. Material characterization was described in Chapter 4, where the focus was on the parameters that make up  $ZT$ . The material values measured were also essential in creating the device simulations used in later chapters. The processing procedure was given in Chapter 5, followed by the packaging evolution. The optimization of packaging was a crucial step in analyzing cooler performance since poor packaging can dominate the device non-ideal effects, and mask any differentiation from sample to sample. Chapter 6 provided a thorough look at single-stage cooling performance and analysis. The enabling contributors to this section were the development of new micro-scale thermal measurement systems and accurate device simulation programs. Also in this chapter, another new type of cooler structure was presented, the two-stage three-terminal TITE cooler. The work described in the first six chapters was then finally brought together and applied toward integrated cooling structures with several different optoelectronic devices.

## 8.2 Future Work

Since this is such a novel device, the possibilities for future work are endless. Even the general concept of micro-cooling is in its infancy, and an infinite number of research projects exist in this field. From just a materials perspective, the sheer number of material combinations that could implement the concepts described in this work are impressive. Likewise, countless optoelectronic and microelectronic devices could benefit from integrated cooling. Keeping this in mind, this section considers only a few of the most logical and attractive directions for future work.

### 8.2.1 Further Cooler Development and Integration

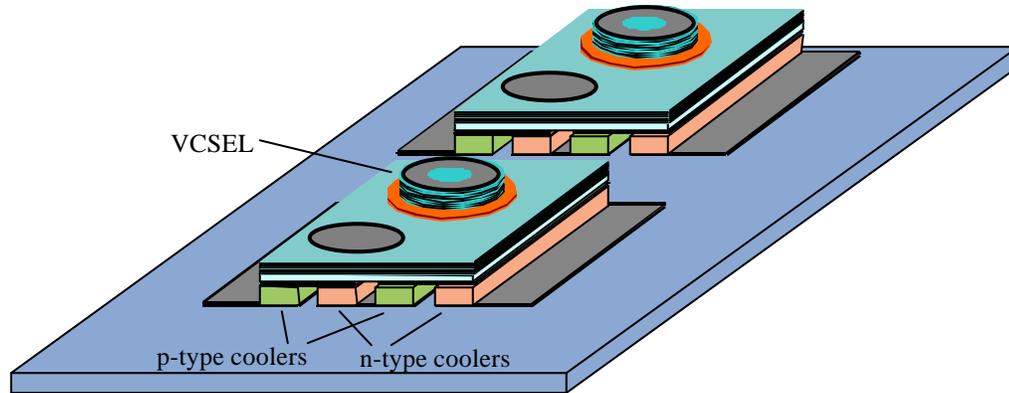
As stated above, the thermionic coolers are still far from being fully optimized in the InP-based material system, and continued work is necessary to approach the performance predicted by the simulations of Chapter 6. The non-ideal effects of contact resistance, side contact Joule heating and heat conduction, and substrate thermal resistance are all still limiting the maximum achievable cooling. The Joule heating and heat conduction from the side contact have already been minimized for single-stage coolers, however, by integrating  $p$ - and  $n$ -type coolers together, this effect can be completely eliminated (see Section 8.2.2). Ways to reduce the substrate thermal resistance have already been described in Chapter 5, but a reliable process for substrate transfer still needs to be developed. Once the non-ideal effects

are further minimized, evaluation of different heterobarrier designs will be clearer, and optimization easier.

The shortcomings of the integrated structures were clearly defined in Chapter 7. From this work, better designs for monolithic integration should be considered, keeping in mind the need to control the electrical current and thermal heat flow. Probably the quickest path to success would be from further work on heterogeneous integration since it is more straightforward to optimize each device separately, and the careful control of current paths is not an issue.

### 8.2.2 *Multi-element Coolers*

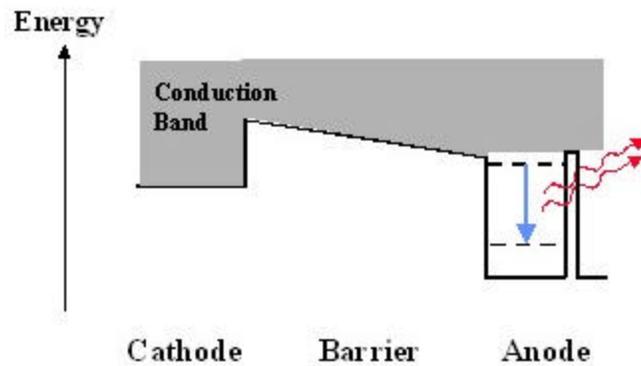
The integration of *n*- and *p*-type thermionic coolers allows for the removal of parasitic external electrical contacts, and can provide larger cooling capacities with smaller currents. This could be done on a small scale with just a few elements, or on a larger scale with the maximum cooling area limited only by the growth wafer diameter. It was already shown in Chapter 6 that *n* and *p* devices could operate under similar conditions, and the work on substrate transfer and heterogeneous integration should provide the basis for making multi-element coolers. Large sized modules would be expected to compete with conventional thermoelectric coolers, while small area devices would retain their niche as micro-coolers for small-scale integrated cooling (Figure 8.1).



**Figure 8.1** Example of  $n$ - and  $p$ -type cooler integration for small scale cooling of individual VCSELs

### 8.2.3 Heat-to-Light Energy Conversion

The greatest detriment to the cooling efficiency of heterostructure thermionic emission coolers is the heat conduction across the thin material between the cold and hot side of the device. What if, however, the hot carriers arriving to the anode junction were to lose their excess energy in the form of light instead of heat? Figure 8.2 shows such a structure with an intersubband light-emitting thermionic cooler [1,2]. The idea of a refrigerator without a hot side at first appears to violate the 2<sup>nd</sup> law of thermodynamics by reducing the total entropy. However, by emitting incoherent light, the increased disorder of the photons can maintain entropy conservation.



**Figure 8.2** An intersubband light-emitting thermionic cooler. Light emission must be incoherent to not violate the 2<sup>nd</sup> law of thermodynamics. From A. Shakouri

#### 8.2.4 Miniband Superlattice Coolers

This concept of *n*-type devices behaving as *p*-type for thermoelectric purposes was discussed at the end of Chapter 2. Theoretical calculations of an *n*-type superlattice showed that if the Fermi level was placed at an optimum level above a miniband, and the barrier above the Fermi level effectively blocked transmission of hot electrons, then the *n*-type material could exhibit *p*-type cooling properties. This would make it possible to make *n*- and *p*-type cooling elements with an all majority carrier structure. It would also allow for the integration of a laser and cooler that was electrically in series, avoiding the problems encountered with the monolithic integration design. The laser would effectively be self-cooled, as any increase in laser current would also increase the cooling at the same time. The main challenge in designing such structures is maintaining a sufficient electrical conductivity to keep

$ZT$  as high as possible. For this, the miniband should be as wide in energy as possible while still providing a barrier to electrons above the Fermi level.

### 8.2.5 Vacuum Thermionics

In Section 8.2.3, heat-to-light energy conversion was suggested as a means to reduce the amount of heat coming from the hot side of the device, thus increasing the efficiency. The ultimate solution to eliminating this back flow of heat is to remove the conducting medium completely, leaving only vacuum. Vacuum thermionics were mentioned in Chapter 2, but because of the large work functions involved, only high temperature applications exist. However, with current high-precision epitaxial growth techniques and semiconductor processing technology, close and uniform spacing of the cathode and anode can be achieved with atomic resolutions. By growing a three layer structure with materials that have a known selective etch, the center layer can be removed leaving an air gap between the two remaining materials. Some form of mechanical support with good electrical and thermal insulation would of course be needed. The close spacing of the electrodes should allow for efficient cooling at room temperature with efficiencies approaching the ideal Carnot value.

## 8.3 Final Comments

Research on thermionic emission cooling in heterostructures has made great progress in a short period of time. This quick progress has supported the drive to apply these

devices in integrated structures for optoelectronic devices. Already, significant improvements beyond the cooling capabilities of bulk InP-based materials have been demonstrated. While these unique coolers serve a certain niche of high cooling-power-density microscale cooling, much more work is necessary before they can compete with traditional thermoelectric coolers in terms of attainable temperature differentials. Finally, while the concepts developed throughout this work were for InP-based materials, they are also universally applicable to any material system for which band structure engineering is possible.

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## Appendix A

### General Thermoelectric Device Theory

While a detailed discussion of thermoelectric theory is beyond the scope of this thesis, the purpose of this section is to familiarize the reader with some of the basic concepts that will apply in many cases to thermionic emission cooling as well. A more detailed source of thermoelectric theory can be found elsewhere [1,2].

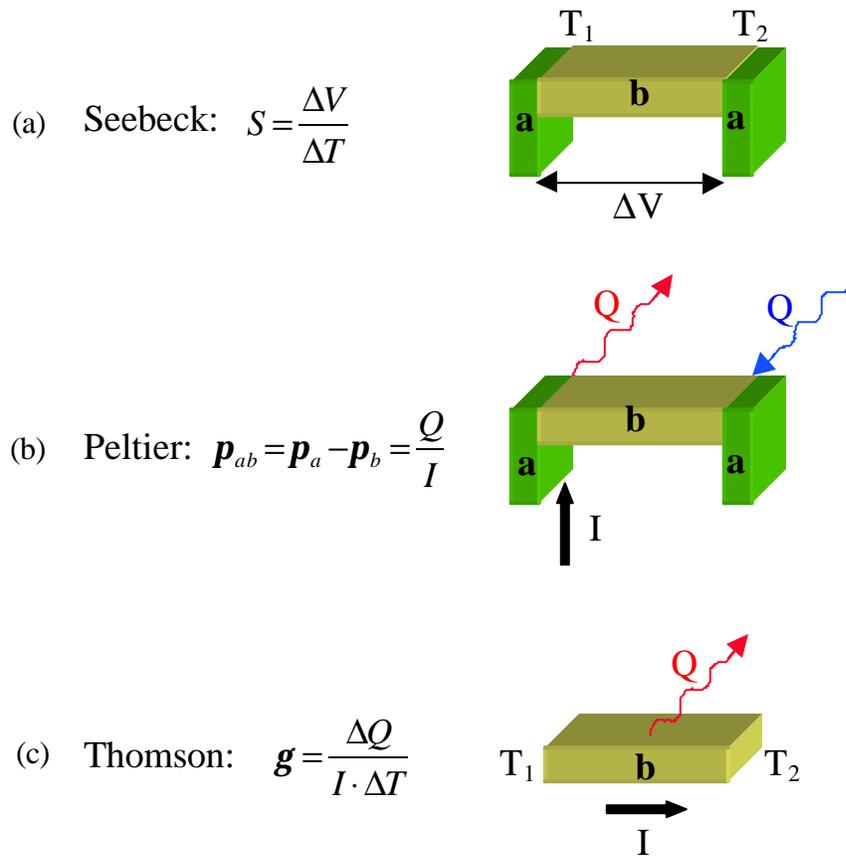
To discuss the basic concepts in thermoelectric theory, consider two junctions between two dissimilar thermo-elements as shown in Figure A.1a. At given temperatures  $T_1$  and  $T_2$ , a voltage is generated. The change in voltage,  $DV$ , is proportional to the change in temperature,  $DT=T_1 - T_2$ , by the Seebeck coefficient  $S$ . This electrical potential is generated as a result of the temperature gradient in the material.

If we now pass a current  $I$  through the same elements as in Figure A.1b, a heat current of  $+Q$  will be generated at one interface, and a heat current of  $-Q$  will be absorbed at the other. This relationship between heat and electrical current is the Peltier coefficient,  $p$ , which results from the change in entropy of the electrical charge carriers as they cross a junction.

The last effect to present is the Thompson effect which is illustrated in Figure A.1c. In any non-isothermal homogeneous conductor with an electrical current, heat is either absorbed or generated and can be described by the Thompson

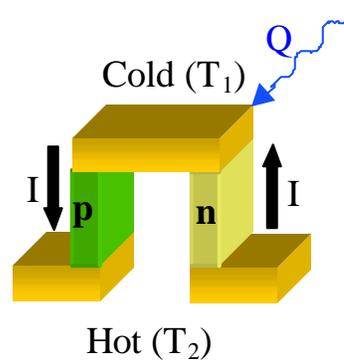
coefficient  $g = \frac{DQ}{I \cdot \Delta T}$ . This phenomenon is a consequence of the direction of electrical carriers with respect to a temperature gradient within a conductor.

Finally it is important to note the relationship between the Seebeck and Peltier coefficients,  $p = S \times T$ . This relation plays an important role in thermoelectrics and will be used below in the expression for cooling capacity.



**Figure A.1** Physical description of thermoelectric phenomenon of interest, (a) Seebeck effect, (b) Peltier effect, and (c) Thomson effect.

Starting from the structure presented above for  $n$ - and  $p$ -type elements, and optimizing the geometry for cooling, we arrive at the conventional thermoelectric configuration shown in Figure A.2. In this arrangement, both  $n$ - and  $p$ -type elements are placed electrically in series and thermally in parallel. When a current is passed through the structure, a net cooling occurs on the top of the elements and a net heating at the bottom. This is due to the fact that the Peltier effect is reversed for  $n$ - and  $p$ -type elements with the same direction of current flow.



**Figure A.2** Single element of a cooler in a conventional thermoelectric configuration, with  $n$ - and  $p$ -type thermoelements electrically in series and thermally in parallel.

The operation of the device can be described quantitatively by the expression for cooling capacity,

$$Q = ST_c I - \frac{1}{2} I^2 R - \mathbf{b} \Delta T \quad (\text{A.1})$$

where  $S$  is the Seebeck coefficient,  $T_c$  is the cold side of the cooler,  $I$  is the electrical current,  $R$  is the electrical resistance,  $\mathbf{b}$  is the thermal conductivity, and  $\mathbf{DT}$  is the

temperature difference between the hot and cold side junctions. The first term describes the Peltier cooling, the second term describes the amount of Joule heat in the legs that arrives back to the cold junction, and the third term relates to the heat conduction between the hot and cold junctions.

The coefficient of performance (COP) of a TE cooler is the ratio of cooling capacity to the amount of input power, and can be expressed as,

$$COP = \frac{Q}{W} = \frac{ST_c I - \frac{1}{2} I^2 R - b \Delta T}{S \cdot \Delta T \cdot I + I^2 R} \quad (A.2)$$

For given material parameters, geometries, and hot and cold junction temperatures,  $Q$  and  $COP$  have their optimum values at different currents. The current,  $I_{max\ cool}$ , gives the maximum cooling, and  $I_{max\ COP}$  the maximum coefficient of performance:

$$I_{max\ cool} = \frac{ST_c}{R} \quad (A.3)$$

$$I_{max\ COP} = \frac{S(T_c - T_h)}{R(\sqrt{1 + T_c Z} - 1)} \quad (A.4)$$

$$Z = \frac{S^2}{\left\{ \left( \frac{b_p}{s_p} \right)^{1/2} + \left( \frac{b_n}{s_n} \right)^{1/2} \right\}^2} \quad (A.5)$$

In practical TE cooling applications, the current is typically chosen in the range between the maximum efficiency and the maximum cooling power. From Equation

A.1 it can be seen that a positive cooling effect ( $Q \geq 0$ ) can not be achieved if the temperature difference between the junctions is too great. The maximum temperature difference is found by setting  $Q = 0$ , and substituting Equation A.3:

$$\Delta T_{\max} = \frac{1}{2} Z T_{\text{cold}}^2 \quad (\text{A.6})$$

From this result, the relevance of the  $Z$  parameter is obvious as it describes both the maximum temperature difference achievable and the  $COP_{\max}$ . Expressing  $Z$  of a single branch as  $S^2 \mathbf{s}/\mathbf{b}$ , it specifies how “good” the material is for thermoelectric cooling applications and is therefore called the thermoelectric *figure-of-merit*.

While in this discussion we have concentrated on the cooling applications of thermoelectrics, it is also possible to operate these devices in reverse and generate power from a given temperature gradient. The optimization is slightly different as it is the power factor,  $S^2 \mathbf{s}$  that needs to be optimized.

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